# Beginning Algebra

**MATH 100B** 

## <sup>2</sup> Preface

This math book has been created by the BYU-Idaho Math Study Center for the college student who needs an introduction to Algebra. This book is the product of many years of implementation of an extremely successful Beginning Algebra program and includes perspectives and tips from experienced instructors and tutors.

Videos of instruction and solutions can be found at the following url: <u>https://youtu.be/YKgyvSq42j8</u>

We hope that it will be helpful to you as you take Algebra this semester.

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	Chapter 5 Review Exercises	
Shape Formulas	Beginning Algebra Final Review Exercises	
1	Shape Formulas	

## Section R-1 Factoring and Least Common Multiple

LCM and Factoring	Find Factors	Find LCM
Fractions	Addition/ Subtraction	Multiplication/ Division
Decimals	Addition/ Subtraction	Multiplication/ Division
Rounding	Nearest Place Value	
Percents	Change fraction and decimals to percents	Find percents of totals
Exponents, Roots	Expand and evaluate exponentials	Find roots that are whole numbers
Order of Operations	Use the order of operations correctly	
Variables and Formulas	Translate words to variables	Replace numbers and use formulas

## CHAPTER OVERVIEW (Video Instruction and Solutions Link)

#### Factoring

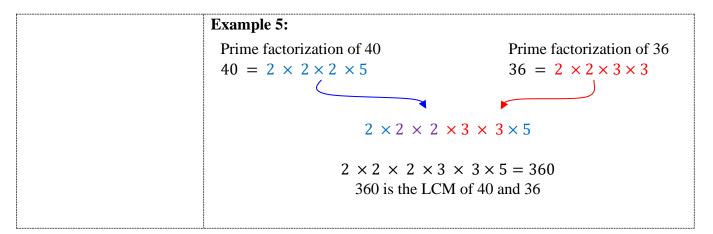
Main Topics	Examples	
	Example 1: Find all fac	ctors of 48
Find all Factors	$1 \times 48 = 48$	Step 1: Find all factors that
	$2 \times 24 = 48$	multiply to be the product 48,
Steps:	$3 \times 16 = 48$	starting with the number 1 and
1. Start with 1 and	$4 \times 12 = 48$	48, and moving up the number
move up finding	$6 \times 8 = 48$	line
numbers that are	$8 \times 6 = 48$	
factors.		Note: In the last row we see
2. List the numbers		$8 \times 6 = 48$ . The 8 has
you have found.		already been used in the
These are all the		factors, so we know that all of
factors.		the factors have been found.
	1, 48, 2, 24, 3, 16, 4,	Step 2: Now we will list all the
	12, 6, 8	numbers we used until we saw
		the repeated number, and these
		will be our factors
	1, 2, 3, 4, 6, 8, 12, 16,	To make them a little easier to
	24, 48	see, we can put them in
		numerical order from smallest
		to largest

6	7	
2	٩	

Prime Factorize	Example 2: Find the prime factorization for 60 and 72.			
<i>Prime:</i> A number with exactly two factors.	$\begin{array}{c} 60\\ 10 & 6\\ 5 & 2 & 3 & 2 \end{array}$	Step 1: Break up the number into two factors.	$\begin{array}{c} 72\\ 2 & 36\\ 2 & 18 \end{array}$	
<ul> <li>Steps</li> <li>1. Find a factor, break the number up.</li> <li>2. Repeat until all factors are prime</li> </ul>		Step 2: Repeat for each factor until prime numbers are reached.	$ \begin{array}{c}  \\  \\  \\  \\  \\  \\  \\  \\  \\  \\  \\  \\  \\ $	
factors are prime.	$60 = 2 \times 2 \times 3 \times 5$		$72 = 2 \times 2 \times 2 \times 3 \times 3$	

### Least Common Multiple

Least Common Multipl	
Main Topics	Examples
Find the LCM	Example 3: Find the LCM of 4 and 5
(Observation)	
<ol> <li>Steps:         <ol> <li>Write out the multiples for 4 and 5.</li> <li>The first number that both multiples hit is 20.</li> <li>The LCM of 4 and 5.</li> </ol> </li> </ol>	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
5 is 20. Find the LCM (Prime	Example 4:
Factorization)	Prime factorization of 4 Prime factorization of 6
<ol> <li>Steps:         <ol> <li>Prime Factorize</li> <li>Write the smallest number that contains all of the numbers.</li> <li>Multiply it out = LCM.</li> </ol> </li> </ol>	$4 = 2 \times 2$ $6 = 2 \times 3$ $2 \times 2 \times 3 = 12$ 12 is the LCM of 4 and 6
Note: the LCM contains the largest set of each prime factor.	



#### **Section R-1 Exercises**

10

#### Find the factors for each number

1.	30	<b>2.</b> 150	3.	37	
4.	12	<b>5.</b> 75	6.	81	
-	factorization of each nur		0		
7.	50	<b>8.</b> 16	9.	,	27
10.	100	<b>11.</b> 99	12	2.	13

#### Find the least common multiple (LCM) of each set of numbers.

13.	3,8	14.	20, 75	15.	5, 7	16.	12,120
17.	4,16	18.	8,12	19.	6,14	20.	17,10
21.	12, 15	22.	3, 5, 10	23.	2, 6, 9	24.	4, 8, 10

#### Preparation.

After reading some of section R.2, find:

**25.** 
$$\frac{3}{5} + \frac{1}{10}$$
  
**26.** 2.38 ÷ .75

#### Section R-1 Answers

- 1, 2, 3, 5, 6, 10, 15, 30 1. **22.** 30 2. 1, 2, 3, 5, 6, 10, 15, 25, 30, 50, 75, 150 **23.** 18 1,37 3. 24. 40 4. 1, 2, 3, 4, 6, 12 In Class. 25. In Class. 5. 1, 3, 5, 15, 25, 75 26.
- **6.** 1, 3, 9, 27, 81
- 7.  $2 \times 5 \times 5$
- $8. \quad 2 \times 2 \times 2 \times 2$
- 9.  $3 \times 3 \times 3$
- 10.  $2 \times 2 \times 5 \times 5$
- **11.** 3 × 3 × 11
- **12.** 13
- **13.** 24
- **14.** 300
- **15.** 35
- **16.** 120
- **17.** 16
- **18.** 24
- **19.** 42
- **20.** 170
- **21.** 60

## <sup>12</sup> Section R-2 Fractions and Decimals

	deo mistraetton ana Solations En	
LCM and Factoring	Find Factors	Find LCM
Fractions	Addition/ Subtraction	Multiplication/ Division
Decimals	Addition/ Subtraction	Multiplication/ Division
Rounding	Nearest Place Value	
Percents	Change fraction and decimals to percents	Find percents of totals
Exponents, Roots	Expand and evaluate exponentials	Find roots that are whole numbers
Order of Operations	Use the order of operations correctly	
Variables and Formulas	Translate words to variables	Replace numbers and use formulas

#### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

#### **Arithmetic of Fractions**

Main Topics	Examples
Key Terms	<b>F</b>
Denominator	Denominator - The bottom of the fraction. To denominate means to name or label.
Numerator	<b>Numerator</b> – The top of a fraction. A numerator counts how many of the denominators there are. $\frac{5}{7}$ is read five sevenths.
Simplify	<b>Simplify</b> - Fractions are simplified when the numerator and denominator have no factors in common. You can also say that the fraction is <i>reduced</i> .
One Common Denominators	One - Any number divided by itself is $1.\frac{5}{5}, \frac{7}{7}, \frac{120}{120}$
Least Common Denominator	<b>Common Denominators</b> - Addition and subtraction require like things. In the case of fractions, "like things" means common denominators.
(LCD)	<ul> <li>Least Common Denominator (LCD) - As the name indicates, this is the lowest possible common denominator between two or more fractions. There are an infinite number of possible common denominators, but usually the easiest one to choose is the lowest or least one.</li> <li>*Finding the LCD is the same process as finding the LCM</li> </ul>

Addition and Subtraction of Fractions	Example 1: Add $\frac{13}{30} + \frac{7}{12}$	
Steps 1. Get a common denominator between the fractions.	$\frac{13}{30} + \frac{7}{12}$ $30  12$ $6  5  4  3$	Step 1: Common denominator. Let's use prime factorization to find the LCD. Prime factorization of 30: $2 \times 3 \times 5$ Prime factorization of 12: $2 \times 2 \times 3$
<ol> <li>Add or subtract the numerators.</li> <li>Simplify.</li> </ol>	$3 \ 2 \ 2 \ 2$ $\frac{13}{30} \times \frac{2}{2} = \frac{26}{60} \qquad \frac{7}{12} \times \frac{5}{5} = \frac{35}{60}$ $\frac{26}{60} + \frac{35}{60} = 61$ $\frac{26}{60} + \frac{35}{60} = \frac{61}{60}$	We need a number whose factors include each of these: $2 \times 2 \times 3 \times 5 = 60$ Step 2: Add the numerators
	Answer: $\frac{61}{60}$	
	Example 2: Subtract $\frac{5}{9} - \frac{1}{3}$ $\frac{5}{9} - \frac{1}{3}$ $\frac{5}{9} - \frac{1}{3} \times \frac{3}{3}$ $\frac{5}{9} - \frac{3}{9} = \frac{2}{9}$ Answer: $\frac{2}{9}$	Step 1: The common denominator is 9, so change the $\frac{1}{3}$ to a $\frac{3}{9}$ . Step 2: Subtract the numerators

14		
Multiplication of Fractions	Example 3: Multiply $\frac{5}{6} \times \frac{1}{3}$	
Steps: 1. No common denominators.	$\frac{5}{6} \times \frac{1}{3}$	Step 1: For multiplication, don't worry about getting common denominators
<ol> <li>Multiply numerators.</li> <li>Multiply denominators.</li> <li>Simplify.</li> </ol>	$\frac{5}{6} \times \frac{1}{3} = \frac{5}{?}$	Step 2: Multiply the numerators straight across
Note: three expressions of multiplication:	$\frac{5}{6} \times \frac{1}{3} = \frac{5}{18}$	Step 3: Multiply the denominators straight across
<ul> <li>Times × 5 × 3 = 15</li> <li>Dot · 5 · 3 = 15</li> <li>Next to 5(3) = 15</li> </ul>	Answer: $\frac{5}{18}$	
Division of Fractions	Example 4: Divide $3\frac{4}{7} \div \frac{2}{3}$	
<ul><li>Steps:</li><li>1. Change any fractions into improper fractions.</li><li>2. Keep it, change it, flip it.</li></ul>	$\frac{\left(\frac{21}{7} + \frac{4}{7}\right) \div \frac{2}{3}}{4}$ $\frac{\frac{25}{7}}{7} \div \frac{2}{3}$	Step 1: Change the first term into an improper fraction. (Whole numbers just get common denominators like others.)
<ol> <li>Multiply straight across.</li> <li>Simplify</li> </ol>	$\frac{25}{7} \times \frac{3}{2}$	Step 2: Keep the first fraction the same, change the division sign to multiplication, and flip the second fraction
	$\frac{25 \rightarrow 3}{7 \rightarrow 2} = \frac{75}{14}$	Step 3: Multiply the numerators and the denominators straight across
	Answer: $\frac{75}{14}$	Step 4: Simplify (if necessary)

Example 5: Divide $\frac{2}{5} \div 1\frac{3}{4}$ $\frac{2}{5} \div (\frac{4}{4} + \frac{3}{4})$ $2 \div 7$	Step 1: Change the first term into an improper fraction. (Whole numbers just get common denominators like others.)
	Step 2: Keep the first fraction the same, change the division sign to multiplication, and flip the second fraction's numerator and denominator
$\frac{2 + 4}{5 + 7} = \frac{8}{35}$	Step 3: Multiply the numerator across and the denominator across
<b>Answer:</b> <sup>8</sup> / <sub>35</sub>	Step 4: Simplify (if necessary)

#### Using a Calculator

After learning to do these by hand, and practicing a few of them, you should learn to use a calculator to do the problems as well. Most scientific calculators have a key that will allow you to input fractions as well as receive the answer as a fraction as well. Have your teacher or a tutor point out which buttons on your calculator are for fractions. Then practice it.

#### **Arithmetic of Decimals**

Main Topics	Examples
Key Terms	
Place Values	Place Values - Every place on the left or right of the decimal holds a certain value. To the left of the decimal, the values are ones, tens, hundreds, thousands, and so forth. On the right of the decimal, the place values are tenths, hundredths, thousands, and so forth.
	$3, 4, 5, 1, 9, 7, 2$ ${}^{thous}_{00} {}^{tens}_{00} {}^{tens}_{00} {}^{tens}_{00} {}^{tens}_{00} {}^{thous}_{00} {}^{thous}$
Decimal	Decimal - Deci- is a prefix meaning 10. Since every place value is either 10 times larger or smaller than the place next to it, we call each place a decimal place.

16	
Process:	Use your calculator! If you need help using your calculator, contact your tutor
	and/or instructor.

### Turn a Fraction into a Decimal

A fraction bar, $\frac{a}{b}$ and a division sign $\div$ are the same thing.				
Trite $\frac{5}{11}$ as a decimal.				
he same as 5 ÷				
545				
s a repeating pattern				
545				

#### **Section R-2 Exercises**

Fine	d Factors.									
<b>R-1</b>	1.	16			<b>2.</b> 48				3.	110
Fine	d the prime	e factorization.								
	4.	60	5.	630	6	<b>).</b>	225			
Fine	_	common multij	ple (1							
	7.	3 & 13		8.	8 & 22			9.	35 8	& 21
	10.	108 & 32		11.	1500 & 180					

**12.** If two planets are aligned with the sun and one planet goes around the sun every 12 years and the other planet takes 22 years, how long will it be before they are in alignment again?

Perform the o	perations by hand. Simp	lify.			
P 2 13	• $\frac{1}{6} + \frac{1}{3}$		$8 + \frac{2}{3}$	15.	$\frac{5}{8} - \frac{1}{2}$
R-2 16	• $3\frac{6}{7} - 1\frac{2}{3}$	17.	$3 \times \frac{1}{12}$	18.	$\frac{4}{5} \times \frac{1}{6}$
19	$\frac{5}{12} \div \frac{1}{3}$	20.	$\frac{6}{9} \div 6$		
Compute with	ı calculator.				
21	• $\frac{4}{7} + \frac{1}{9}$	22.	$\frac{14}{19} + \frac{2}{17}$	23.	$\frac{8}{13} - \frac{11}{26}$
24.	$\frac{11}{12} - \frac{1}{21}$	25.	$\frac{45}{3} \times \frac{4}{19}$	26.	$\frac{15}{23} \times \frac{11}{9}$
27.	$\frac{34}{37} \div \frac{2}{7}$	28.	$\frac{22}{33} \div \frac{17}{21}$		
Perform the i	ndicated operation (with	or wi	thout a calculator).		
29.	186.4 + 57.06	30.	58.93 <u>-17.986</u>	31.	2,578 <u>+ 389.4</u>
32.	365.8 × 0.5	33.	5,968.4 ÷ 9	34.	$0.07 \div 0.006$
	action as a decimal.		7	~-	7
35.	$\frac{4}{11}$	36.	$\frac{7}{2}$	37.	$\frac{7}{9}$

#### **Preparation.**

After reading some of section R.3, find the following:

**38.** What percent did Jotham get if he had 7 out of 8 questions correct on his quiz? **39.** Evaluate  $3 + 8 \times 2^4$ 

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#### Section R-2 Answers

1.	1, 2, 4, 8, 16	22.	276 323
2.	1, 2, 3, 4, 6, 8, 12, 16, 24, 48	23.	<u>5</u> 26
3.	1, 2, 5, 10, 11, 22, 55, 110	24.	<u>73</u> 84
4.	$2 \times 2 \times 3 \times 5$	25.	$\frac{60}{19}$ or $3\frac{3}{19}$
5.	$2 \times 3 \times 3 \times 5 \times 7$	26.	55 69
6.	$3 \times 3 \times 5 \times 5$	27.	$\frac{119}{37}$ or $3\frac{8}{37}$
7.	39	28.	$\frac{14}{17}$
8.	88	29.	243.46
9.	105	30.	40.944
10.	864	31.	2,967.4
11.	4500	32.	182.9
12.	132 years	33.	$663.1\overline{5}$ or $663.156$
13.	$\frac{1}{2}$	34.	11.6 <i>or</i> 11.667
	$\frac{26}{3}$ or $8\frac{2}{3}$	35.	. 36
15.	$\frac{1}{8}$	36.	3.5
16.	$2\frac{4}{21}$ or $\frac{46}{21}$	37.	.7
17.	$\frac{1}{4}$	38.	In Class.
18.	<u>2</u> 15	39.	In Class.
19.	$\frac{5}{4}$ or $1\frac{1}{4}$		
20.	$\frac{1}{9}$		

21.  $\frac{43}{63}$ 

## Section R-3 Rounding, Percents, Exponents, Roots, and Order of Operations

LCM and Factoring	Find Factors	Find LCM
Fractions	Addition/ Subtraction	Multiplication/ Division
Decimals	Addition/ Subtraction	Multiplication/ Division
Rounding	Nearest Place Value	
Percents	Change fraction and decimals to percents	Find percents of totals
Exponents, Roots	Expand and evaluate exponentials	Find roots that are whole numbers
Order of Operations	Use the order of operations correctly	
Variables and Formulas	Translate words to variables	Replace numbers and use formulas

#### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

#### Rounding

Main Topics	Examples			
Key Terms Rounding	<ul> <li>In rounding, we decide to not keep the exact number. For example: If I have \$528.37 in the bank, I might easily say that I have about \$500. I have just rounded to the nearest hundred.</li> <li>On the other hand, I might be a little more specific and say that I have about (still not exact) \$530. I have just rounded to the nearest ten.</li> </ul>			
	Example 1: Round \$4,278.23 (	to the nearest hundred		
Steps:	▼\$4,300.00	Decide if our number is closer to		
1. Look at the digit to the right of	\$4,278.23	the nearest hundred above the number or below the number		
where the rounding is.		Since 7 is greater than 5, we round the 2 up to a 3.		
2. Less than 5 goes down. 5 or	\$4,278.23 ≈ \$4,300.00	I I I I I I I I I I I I I I I I I I I		
greater goes up.	Answer: \$4,300.00			

Percents							
Main Topics	+	nples					
Key Terms	Exa	mple 2: T	urn the following f	ractions into decima	ls and percents.		
Percent - The word			Divide Two decimal pla	aces			
"percent" comes from							
two words: PER means		Fraction	Decimal/Number	Percent (rounded)			
divide, and CENT means		$\frac{3}{8}$	.375	37.5%			
100.		$\frac{7}{10}$	.7	70%			
When we divide by 100		$2\frac{1}{2}$	2.5	250%			
and move from a percent		$\frac{15}{18}$	.8333	83.3%			
to a decimal, the decimal		$\frac{5}{11}$	.4545	45.5%			
moves two places to the		8	8	800%			
left. Decimal to percent moves the decimal two		$\frac{51}{73}$	.698630137	69.9%			
			imals $\Leftrightarrow$ place value $.23 = \frac{23}{100}$ $.4 = \frac{4}{10} = \frac{2}{5}$ $5.327 = \frac{5327}{1000}$				
	Exa	mple 3:		Example 4:			
Percent of something - A percent doesn't represent an amount when it is alone. "Of" means to		0.2( 0.2(3	% <i>of</i> 358 358) = ? 58) = 71.6	7.2% of 0.072(50 0.072(500	0) = ?		
multiply		mple 5:		Example 6: 550 people attended a meeting. If 26% of them were driving green cars how many people drove green cars? 26% of 550 0.26(550) = ? 0.26(550) = 143			
<ul><li>Steps</li><li>1. Change to decimal.</li><li>2. Multiply.</li></ul>	chai wha tax?	at is the an	\$25 purchase, nount of sales 25 = \$1.75				
Note: three expressions of multiplication: • Times × $5 \times 3 = 15$ • Dot · $5 \cdot 3 = 15$ • Next to $5(3) = 15$				Answer: 143 cars			

#### Percents

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#### **Exponents**, Roots

Hyomplog			
Examples	<b>D</b>		E1
—	Expanded	Notation	Evaluated
	2		Notation
$\frac{2^{1}}{2^{2}}$			2
			4
			8
			16 32
<b>Example 7:</b> Write 4 <sup>3</sup> in expan		Write $2 \times 2 >$	
		-	orm
Answer: $4 \times 4 \times$	4	Answer: 2 <sup>4</sup>	
Evaluate. Example 9:	Exampl		Example 11:
4 <sup>3</sup>	2 <sup>5</sup>	$m^3$	where $m = -3$
$4 \times 4 \times 4 = 64$	$2 \cdot 2 \cdot 2 \cdot 2 \cdot 2$	2 = 32 (-	-3)(-3)(-3) = -27
Answer: 64	Answer: 32		nswer: -27
repeated base. Th	lly multiplied is the base can consist	he bt of	The little number up high is the <mark>exponent</mark> .
Enormals 10.	alvata 04		
Example 12: Evaluate $8^4$ $8^4 = 8 \cdot 8 \cdot 8 \cdot 8$ $= 64 \cdot 8 \cdot 8$ $= 512 \cdot 8$ = 4096 Answer: 4096			e bases, and then multiply.
	Write $4^3$ in expan Answer: $4 \times 4 \times 4$ Evaluate. Example 9: $4^3$ $4 \times 4 \times 4 = 64$ Answer: 64 The big repeated base. Th number Example 12: Evaluate $8^4 = 8 \cdot = 64 \cdot = 51$ = 40	Notation $2^1$ $2$ $2^2$ $2 \times 2$ $2^3$ $2 \times 2 \times 2$ $2^4$ $2 \times 2 \times 2$ $2^5$ $2 \times 2 \times 2$ $2^5$ $2 \times 2 \times 2$ $2^5$ $2 \times 2 \times 2$ Example 7:Write $4^3$ in expanded formAnswer: $4 \times 4 \times 4$ Evaluate.Example 9:Example $4^3$ $2^5$ $4 \times 4 \times 4 = 64$ $2 \cdot 2 \cdot 2 \cdot 2 \cdot 2$ Answer: $64$ Answer: $32$ Answer: $64$ Answer: $32$ The bigger number being repeatedly multiplied is the base. The base can consist numbers and/or variablesExample 12:Evaluate $8^4$ $8^4 = 8 \cdot 8 \cdot 8 \cdot 8$ $= 64 \cdot 8 \cdot 8$ $= 512 \cdot 8$ $= 4096$	Notation $2^1$ 2 $2^2$ $2 \times 2$ $2^3$ $2 \times 2 \times 2$ $2^4$ $2 \times 2 \times 2 \times 2$ $2^5$ $2 \times 2 \times 2 \times 2 \times 2$ $2^5$ $2 \times 2 \times 2 \times 2 \times 2 \times 2$ $2^5$ $2 \times 2 \times 2 \times 2 \times 2 \times 2$ Write $4^3$ in expanded formWrite $2 \times 2 $

Common Mistakes	1. Mistaking exponents for multiplication		Incorrect: $2^4 = 2 \times 4 = 8$ Correct: $2^4 = 2 \times 2 \times 2 \times 2 = 16$
	notation out loud: 2 <sup>4</sup>		Incorrect: "Two four" Correct: "Two to the fourth"
			Incorrect: $2 + 2 + 2 + 2 = 2^4$
	terms with the same base, not in addition.		Correct: $2 \times 2 \times 2 \times 2 = 2^4$
Evaluating Roots			
	Example 13: Evaluate $\sqrt{196}$		
A square root is the	√ <b>196</b>	Eithe	r recognize that $14 \times 14 = 196$ or
opposite of squaring	Answer: 14	find t	he $\sqrt{x}$ button on your calculator
(raising to the $2^{nd}$ power).			

### **Order of Operations**

Main Topics	Examples	
Getting the right order	Example 14: Simplify $2 + 3 \cdot 4$	- 5
Steps: Parentheses (Grouping)	$2 + 3 \cdot 4 - 5$	There are no parentheses or exponents, so first we multiply
Exponents (Roots) Multiplication Division	2+12-5 14-5	Because addition and subtraction are on the same level, we do them from left to right.
Addition Subtraction	9	
	Answer: 9	
	Example 15: Simplify $4 \times 3^2$ – $4 \times 3^2$ – $7 \times 2 + 4$	Because there are no parentheses, we first do exponents
Note: a fraction bar groups	$4 \times 9 - 7 \times 2 + 4$	Next, we do multiplication
like parentheses: $\frac{5+7}{3} = \frac{12}{3} = 4$	36 - 14 + 4     22 + 4     Answer: 26	Add and subtract left to right
$\frac{3}{3} - \frac{3}{3} - 4$ Common Mistakes	Remember that multiplication and	l division are on the same level, so ute from left to right. Similarly, add

#### **Section R-3 Exercises**

Per	rform th	e indicated operation.					
R-1	<b>1.</b>	Find the prime factorization	n of 2	16. <b>2.</b>	LCM (75, 9	90)	
		a distant solar system, two year orbit. How many year	-	-	-	year or	bit and the other has a
R-2	4.	$\frac{6}{25} + \frac{5}{8}$ <b>5.</b> $\frac{3}{5} - \frac{1}{1}$	8 20	6.	$\frac{4}{25} \times \frac{5}{8}$	7.	$\frac{1}{3} \times \frac{2}{12}$
Per	rform th 8.	<b>e indicated operation (ro</b> 9.83 – 5.635		9 <b>three decima</b> . 18 × .63	l places whe	n need	led).
Co	nvert fra	action to decimal.					
	10.	<u>5</u> 16	11.	<u>24</u> 5			
R-3		10		0			
Ro	und to t	he nearest tenth.					
	12.	42.142956 <b>13.</b> .4	7937	<b>14.</b> 13,	693.639	15.	284.359432
Ro		he nearest hundred. 23,978.74 <b>17.</b> 56	574.90	<b>18.</b> 14	9.99	19.	3,499,599.99
Wr	ite each	fraction as a percent.					
		$\frac{22}{25}$	21.	$\frac{23}{30}$		22.	<u>3</u> 50
Wr	rite each	percent as a fraction. Sir					
	23.	175%	24.	28%		25.	60%
Fin	nd the fo	llowing:					
	26.	0	27.	17% of 85		28.	.3% of 365
	29.	The amount of a 7% tax on pants that cost \$25	30.	The amount of on a \$36 mea	-	31.	The amount saved with a 30% discount of a coat with a cost of \$85

24									
Write		ollowing expon		-	ed no				
	32.	4 <sup>3</sup>	33.	45 <sup>2</sup>		34.	7 <sup>4</sup>	35.	2 <sup>5</sup>
Find tl	36.	$\sqrt{36}$		√3025		38.	√ <u>256</u>	39.	√9216
Follow	orde	er of operation	s to ev	valuate.					
40.	210	$6 \cdot 6^3 \div 6^2$			41.	$\frac{30+18\div}{3}$	3	42.	$5^2 + (11 - 6) \cdot 7$
43.	26	$-11 + 27 \div 3$			44.	$\frac{6}{8} \cdot \frac{8}{3} +$	2	45.	$3^3 - 5 \cdot 3 + 8 \cdot 10/2$
46.	8 ÷	- 4 + 35 - (23	- 16)	× 4	47.	1+1-	+1+1+1	· 0	

#### Preparation.

After reading some of section R.4, find the following if x = 7 and a = 2:

**48.**  $3x + a^3$ 

#### Section R-3 Answers

1.	$2 \times 2 \times 2 \times 3 \times 3 \times 3$ or $2^3 \times 3^3$	29.	\$1.75
2.	450	30.	\$5.40
3.	270 years	31.	\$25.50
4.	$\frac{173}{200}$	32.	$4 \cdot 4 \cdot 4; 64$
5.	8 15	33.	45(45); 2025
6.	$\frac{1}{10}$	34.	$7 \times 7 \times 7 \times 7;$ 2401
7.	$\frac{1}{18}$	35.	$2 \cdot 2 \cdot 2 \cdot 2 \cdot 2;$ 32
8.	4.195	36.	6
9.	. 113	37.	55
10.	. 3125	38.	16
11.	4.8	39.	96
12.	42.1	40.	1296
13.	.5	41.	12
14.	13,693.6	42.	60
15.	284.4	43.	24
16.	24,000	44.	4
17.	5700	45.	52
18.	100	46.	9
19.	3,499,600	47.	4
20.	88%	48.	In class.
21.	$76.\overline{6}\%$ or $76.7\%$		
22.	6%		
23.	$1\frac{3}{4}$ or $\frac{7}{4}$		
24.	<u>7</u> 25		
25.	<u>3</u> 5		
•	-		

- **26.** 22.08
- **27.** 14.45
- **28.** 1.095

## Section R-4 Variables and Formulas

HAFTER OVERVIEW ( <u>VIdeo II</u>	· · · · · · · · · · · · · · · · · · ·	
LCM and Factoring	Find Factors	Find LCM
Fractions	Addition/ Subtraction	Multiplication/ Division
Decimals	Addition/ Subtraction	Multiplication/ Division
Rounding	Nearest Place Value	
Percents	Change fraction and decimals to percents	Find percents of totals
Exponents, Roots	Expand and evaluate exponentials	Find roots that are whole numbers
Order of Operations	Use the order of operations correctly	
Variables and Formulas	Translate words to variables	Replace numbers and use formulas

#### **CHAPTER OVERVIEW (Video Instruction and Solutions Link)**

#### Variables

Examples			
	· •		
Substitution - Stick i	n the number for the l	letter. Then do the oper	ations.
Example 1:	Example 2:	Example 3:	
Find 7b if $b=3$	Find 7 <i>b</i> if $b = 9$	Find 7 <i>b</i> if $b = 13$	]
7 <i>b</i> =	7b =	7b =	
7(3) = 21	$7 \cdot 9 = 63$	7(13) = 91	
Evaluate $5t + s$ if $t =$	=(3) and $s =(36)$		
<b>F</b> 1 . <b>F</b> <sup>1</sup>	*********************************		
51			
	Variables - These synchange from time to Substitution - Stick i Example 1: Find 7b if $b=3$ 7b = 7(3) = 21 Example 4: Evaluate $5t + s$ if $t = 5 \cdot 3 + 36 = 15 + 36 = 15 + 36 = 15$	Variables- These symbols or letters, representation of the symbols of letters, representation of the symbols of vary. Thus, the substitution of the symbols of t	VariablesVariablesThese symbols or letters, represent numbers, but the rechange from time to time, or vary. Thus, they are called variablesSubstitution - Stick in the number for the letter. Then do the operExample 1: Example 2: Example 3:Find 7b if b=3Find 7b if b = 9Find 7b if b=9Find 7b if b = 9Find 7b if b = 137b =7b =

	Example 5:					
		2y  if  x = 9  and  y = 1				
	6x - 2y =					
	6(9) - 2(11) =					
	54 - 22 = 32					
Translation –	32					
Language						
Dictionary	+	-	•	•	—	
	plus	minus	times	divide	totals	
	add	subtract	twice	half	is	
Note: Switch	bigger than	smaller than (switch)	double	third	will be	
2 less than 20 is 18 20 - 2 = 18	more than	less than (switch)	triple	out of	am	
20 2 - 10	increase	decrease	of	quotient	are	
	warmer	colder	percent of		equals	
	interest	discount	product			
	gained	sale				
	tip	difference				
	sum					
	Example 6:					
	The cost is 5 less than the product of the width and length					
	C = wl - 5					
	<b>Example 7:</b> 25% of the sum of the warmest and coldest temperatures is 5 times the quotient of my height and 4.					
		.25(w + a)	$f(z) = 5 \cdot \frac{h}{4}$			

## Formulas

Main Topics	Examples					
Key Terms	Formulas - These are patterns in the form of equations and variables, often with numbers, which help us find something we want to know.					
	onen with humbers, w	men help us find something we want to kn				
	Formula	Practical Use				
Formulas	$x = vt + x_o$	Physics – finding position				
Formulas	$P = 4v^2$	Medicine – pressure in the heart				
	$A = P\left(1 + \frac{r}{n}\right)^{nt}$	Finances – bank account balance with compound interest				
Distance, Rate, and Time		aveled 3 hours while going 27 mph. using t nine the distance that she traveled.				
Formula: $d = rt$	d = rt t = 3 hours	Write down the information				
r = rate, t = time, d = distance	r = 27  mph					
	d = ? d = (27)(3)	What are we trying to find? Plug in what is known				
	$d = \frac{(27)(3)}{d} = \frac{81}{3}$	Simplify for what we are looking for.				
	Answer: 81 miles					
Calculating Taxes and Discounts	how much tax will you	nt to buy a \$759 computer with 8% sales ta a end up paying?				
Formulas:	T = rP	Write down the information				
Tax	r = 8% P = \$759	Write down the information.				
	T = ?	What are we trying to find?				
T = rP	T = (0.08)(759)	Plug in what is known.				
	T = (0.08)(759) $T = 60.72$	Plug in what is known. Simplify for what we are looking for.				

	up a savings plan that gives her simple she invests \$750, how much interest will she
I = Prt r = 7% P = \$750 t = 10 years I = ? D = (750)(0.07)(10) T = 525 Answer: Mindy will earn \$525	Write down the information. What are we trying to find? Plug in what is known. Simplify for what we are looking for.
what is that temperature is $C = \frac{5}{9}(F - 32)$	mometer in your car says it is 94° Fahrenheit, n Celsius? Write down the information.
C = ? $C = \frac{5}{9}(94 - 32)$	What are we trying to find? Plug in what is known.
$C = \frac{5}{9}(62)$	Simplify for what we are looking for.
Answer: 34.4° Celsius	
	interest of 7% per year. If earn in 10 years? I = Prt $r = 7%$ $P = $750$ $t = 10  years$ $I = ?$ $D = (750)(0.07)(10)$ $T = 525$ Answer: Mindy will earn \$525 Example 12: If your therm what is that temperature in $C = \frac{5}{9}(F - 32)$ $F = 94$ $C = ?$ $C = \frac{5}{9}(94 - 32)$ $C = \frac{5}{9}(62)$ $C = 34.4$

Celsius to Fahrenheit $F = \frac{9}{5}C + 32$	<b>Example 13:</b> If it is 4° Ce Fahrenheit?	Example 13: If it is 4° Celsius outside, what is the temperature in Fahrenheit?				
5 F=Fahrenheit, C=Celsius	$F = \frac{9}{5}C + 32$ $C = 4^{\circ}$ F = ? $F = \frac{9}{5}(4) + 32$ F = 7.2 + 32 F = 39.2 Answer: 39.2° F	Write down the information. What are we trying to find? Plug in what is known. Simplify for what we are looking for.				

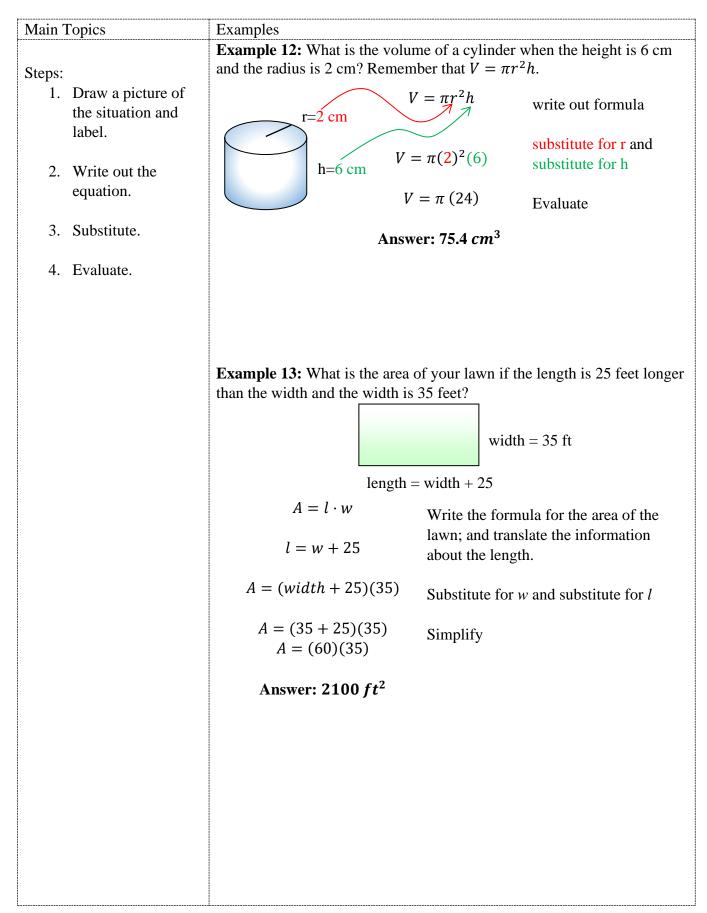
## Common Geometry Formulas

<i>l</i> <i>w</i> Rectangle	P = 2l + 2w $A = lw$	<ul> <li><i>P</i> is the Perimeter</li> <li><i>l</i> is the length</li> <li><i>w</i> is the width</li> <li><i>A</i> is the Area</li> </ul>
<i>a b h h</i> Parallelogram	P = 2a + 2b $A = bh$	<ul> <li><i>P</i> is the Perimeter</li> <li><i>a</i> is a side length</li> <li><i>b</i> is the other side length</li> <li><i>h</i> is height</li> <li><i>A</i> is the Area</li> </ul>
a h d B Trapezoid	$P = b + a + B + d$ $A = \frac{1}{2}h(B + b)$	<ul> <li><i>P</i> is Perimeter</li> <li><i>b</i> is the little base</li> <li><i>B</i> is the big Base</li> <li><i>a</i> is a leg</li> <li><i>h</i> is height</li> <li><i>d</i> is a leg</li> <li><i>A</i> is the Area</li> </ul>
h h Triangle	$P = s_1 + s_2 + s_3$ $A = \frac{1}{2}bh$	$P$ is the Perimeter $h$ is height $b$ is base $A$ is the Area $s_1$ is one side $s_2$ is a second side $s_3$ is the third side
<i>b</i> <i>c</i> Triangle	a+b+c=180	<ul> <li><i>a</i> is one angle</li> <li><i>b</i> is another angle</li> <li><i>c</i> is another angle</li> </ul>
h l Rectangular Solid	SA = 2lw + 2wh + 2lh $V = lwh$	<ul> <li><i>l</i> is the length</li> <li><i>h</i> is the height</li> <li><i>w</i> is the width</li> <li><i>SA</i> is the Surface Area</li> <li><i>V</i> is Volume</li> </ul>

r	$C = 2\pi r$
/	12

r Circle	$C = 2\pi r$ $A = \pi r^2$	<ul> <li>C is the Circumference or perimeter</li> <li>π is a number, about 3.14159 (it has a button on your calculator)</li> <li>r is the radius of the circle</li> <li>A is the area inside the circle.</li> </ul>
r	$LSA = 2\pi rh$	LSA is Lateral Surface Area = Area just on the sides h is the height
h	$SA = 2\pi rh + 2\pi r^2$	SA is total Surface Area $\pi$ is a number, about 3.14159 (it has a button on your calculator)
Cylinder	$V = \pi r^2 h$	<i>r</i> is the radius of the circle <i>V</i> is Volume
	$LSA = \pi rl$	<ul> <li><i>h</i> is the height</li> <li><i>r</i> is the radius of the circle</li> <li><i>l</i> is the slant height</li> </ul>
r	$SA = \pi r^2 + \pi r l$	$\pi$ is a number, about 3.14159 (it has a button on your calculator) SA is total Surface Area
Cone	$V = \frac{1}{3}\pi r^2 h$	LSA is Lateral Surface Area = Area just on the sides V is Volume
r	$SA = 4\pi r^2$	<i>r</i> is the radius <i>SA</i> is the Surface Area
Sphere	$V = \frac{4}{3}\pi r^3$	<i>V</i> is the Volume

Note: LSA and SA are single quantities and do not represent L·S·A or S·A (multiplication of individual variables). The designations in the third column identify what quantities are represented.



<b>Example 14:</b> The depth of a rectangular pool is 17 feet less than half of the length and the width is 20 feet less than the length. If the pool is 54 feet long, how much water would you need to fill up a rectangular pool? Remember that $V = lwh$ .		
depth $= \frac{1}{2}l - \frac{1}{2}l$ width $= l - 20$ $V = l(l - 20)\left(\frac{1}{2} \cdot l - 17\right)$ $V = 54(54 - 20)\left(\frac{1}{2} \cdot 54 - 17\right)$ V = 54(34)(10)	<ul> <li>- 17</li> <li>- Write out an equation of the volume in terms of what you know - in our case "<i>l</i>."</li> <li>- Substitute for <i>l</i>.</li> <li>- Evaluate.</li> </ul>	
Answer: 18360 <i>ft</i> <sup>3</sup>		

## **Units for Geometry Answers**

1 – Dimensional	2 – Dimensional	3 – Dimensional	
length, width, radius, height, distance	Area	Volume	
ft, m, yd, mi, in, cm,	$ft^2$ , $m^2$ , $yd^2$ , $mi^2$ , $in^2$ , $cm^2$ ,		
mm, km, etc.	$mm^2$ , $km^2$ , etc.	$mm^3$ , $km^3$ , etc.	

Perform the indicated operation.								
<b>R-2</b>	<b>1.</b> 7.2 + 13.258	<b>2.</b> 237.58 – 18.6794	<b>3.</b> .298 × 1.4					
Pe	Perform the indicated operation.							
	4. $\frac{4}{5} \times \frac{15}{16}$	<b>5.</b> $\frac{15}{21} \div \frac{5}{42}$	<b>6.</b> $\frac{7}{120} \div \frac{21}{40}$					
Ev	valuate.							
<b>R-3</b>	<b>7.</b> √196	<b>8.</b> 65 <sup>3</sup>	<b>9.</b> $\sqrt{7^6}$					
Co	onvert to decimal notation (ro	und to four decimal places) a	and then to a percent.					
	<b>10.</b> $\frac{6}{19}$	11. $\frac{15}{4}$	12. $\frac{126}{3150}$					
Ro	ound to the nearest hundredth	L.						
	<b>13.</b> 163.69387	<b>14.</b> .01982465						
Ro	ound to the nearest thousand.							
	<b>15.</b> 235,724.98	<b>16.</b> 98,482.994						
Ev	valuate.							
<b>17.</b> $3^4 + (5 \times (8 \div 4) - 3)$ <b>18.</b> $4 \times (8 + 15 \div (26 - 23) \times 5)$								
Evaluate the expression with the given variables.								
D 4								

**R-4** 

**19.** 4x + t: when x = 4 and t = 16 **20.** 19x + 47y: when x = 4 and y = 3

**21.** x + 2y - z: when x =18; y = 3; z = 20 **22.**  $\frac{4}{5}x + \frac{2}{7}y$ : when x = 5 and y = 7

#### Translate the following into math.

**23.** John is 5 years older than Maria.

- 24. Kris is 17 years older than twice Charlotte's age.
- **25.** The radius is 5 less than 4 times the height.
- **26.** Twice the number of nickels is equal to 3 less than the number of pennies.
- 27. There are four times as many horses as cows.
- **28.** The sum of the numbers of pigs and chickens is equal to 17.
- **29.** A number increased by 30% of the number is equal to 75.
- **30.** Twice the difference between Mark's height and Nick's is equal to 38.

Find the missing variable. (Note: If you don't use the  $\pi$  button on your calculator for the formulas that use it, your answer may differ slightly)

31.	For a triangle	<b>32.</b> For a cone	33.	For a sphere
	b = 4 in	r = 3.8 m		r = 16  cm
	h = 7 in	l = 5.1  m		V = ?
	A = ?	SA = ?		

**34.** I have a rectangular sand box whose length is 4 more than its width. If the width is 12 ft, what is the perimeter of the sand box?

35. What is the volume of a cylinder whose height is 3 cm less than twice its radius? The radius is 4 cm.

#### Find the missing variable.

36.	Distance r = 75  mph t = 5  hrs d = ?	37.	Tax r = 6% P = \$29.95 T = ?	38.	<b>Discount</b> r = 30% P = \$48 D = ?
39.	<b>Simple Interest</b> P = \$2500 r = 3.5% t = 2 years I = ?	40.	<b>Temperature</b> F = 88° C = ?	41.	<b>Temperature</b> C = 12° F = ?

### Section R-4 Answers

1.	20.458	29.	n + .3n = 75
2.	218.9006	30.	2(M-N)=38
3.	0.4172	31.	$14 \text{ in}^2$
4.	$\frac{3}{4}$	32.	106.25 m <sup>2</sup>
5.	6	33.	17157.28 cm <sup>3</sup>
6.	$\frac{1}{9}$	34.	56 ft
7.	14	35.	251.33 cm <sup>3</sup>
8.	274,625	36.	375 miles
9.	343	37.	\$1.80
10.	. 3158, 31.58%	38.	\$14.40
11.	3.75, 375%	39.	\$175
12.	.04, 4%	40.	31.11° C
13.	163.69	41.	53.6 ° F
14.	. 02		
15.	236,000		
16.	98,000		
17.	88		
18.	132		
19.	32		
20.	217		
21.	4		
22.	6		
23.	J = 5 + M		
24.	K = 17 + 2C		
25.	r = 4h - 5		
26.	2n = p - 3		
27.	h = 4c		
28.	p + c = 17		

### **Chapter R Review Exercises**

**1.** Create a visual chart of the methods, formulas, and examples from studying how to evaluate and simplify the operations used in this chapter. (<u>Video instruction and example</u>)



**2.** Find the prime factorization of 132.

**3.** Find the LCM of 18 and 24.

**4.** In a distant solar system three planets are lined up. Their orbits are 12 years, 25 years, and 30 years. How long until they are lined up again?

#### Perform the indicated operations.



5. Simplify 
$$\frac{27}{45}$$
 6.  $\frac{3}{8} + \frac{1}{6}$ 
 7.  $\frac{9}{10} - \frac{4}{13}$ 

 8.  $\frac{4}{25} \div \frac{3}{5}$ 
 9.  $\frac{13}{22} + \frac{2}{11}$ 
 10.  $\frac{5}{7} \cdot \frac{4}{3}$ 

#### Perform the indicated operations.

11.	241.32	12.	$24 \div (0.8)$	13.	112.3
	+ 413.86				× 12.1
14.	58.46 - 2.974	15.	$4 \div .0002$	16.	3.6(1.4)

#### Convert the following fractions to decimals.

**17.**  $\frac{15}{24}$  **18.**  $\frac{16}{33}$  **19.**  $\frac{87}{25}$ 

**20.** Convert 0.323 to a fraction.

- **21.** Convert 115% to decimal notation.
- **22.** Round 385.241 to the nearest hundredth.

**23.** Round 385.241 to the nearest hundred.

#### Change the following to percents.

24.	12	25.	0.021	26.	2.16
	15				

**R-3** 

#### Write in exponential notation and evaluate.

**Evaluate.** 

**Evaluate.** 

**31.** 
$$34 \cdot 2 + 12 \div 2 + \frac{55 - 13}{3}$$
 **32.**  $4^2 + 3 \cdot (2 + 4) - 2 \times 7$ 

**R-4** 

**33.** A large rug has a width of 6 ft, and its length is 1 ft less than twice the width. What is the area of the rug?

**34.** A fence has to go around the perimeter of a rectangular area of my lawn that measures 20 *ft by* 28 *ft*. If fencing costs \$5.10 per foot, how much will it cost to fence this part of my lawn?

35. The weather forecast in Brazil is 33° Celsius. How warm is that in degrees Fahrenheit?

#### Evaluate the expression with the given variable(s).

**36.**  $2\pi rh$ : when r = 3, h = 6**37.**  $\sqrt{a^2 + b^2}$ : when a = 5, b = 12

#### Translate the following into math.

**38.** Bethany will be 12 years older than twice Richard's age.

**39.** There are twice as many students as tutors.

**40.** A price decreased by 19% of the price is equal to 250.

### **Chapter R Review Answers**

mapt			
1.	Grid format, one side, full of steps and examples from this chapter. Submit.	25.	2.1%
2.	$2 \cdot 2 \cdot 3 \cdot 11$	26.	216%
3.	72	27.	7 <sup>4</sup> , 2401
4.	300 years	28.	8 <sup>3</sup> , 512
5.	$\frac{3}{5}$	29.	27.36
6.	$\frac{13}{24}$	30.	610.85
7.	<del>77</del> 130	31.	88
8.	$\frac{4}{15}$	32.	20
9.	$\frac{17}{22}$	33.	$66 ft^2$
10.	<u>20</u> 21	34.	\$489.60
11.	655.18	35.	91.4° F
12.	30	36.	113.1
13.	1358.83	37.	13
14.	55.486	38.	B = 12 + 2R
15.	20,000	39.	s = 2t
16.	5.04	40.	P19P = 250
17.	.625		

- **18.** . 48<del>48</del>
- **19.** 3.48
- **20.**  $\frac{323}{1000}$
- **21.** 1.15
- **22.** 385.24
- **23.** 400
- **24.** 80%

# Section 1-1 Negatives, Inequalities, Addition, Subtraction

(video instruction and Solutions Elink)					
Number Line	Positives	Negatives			
Inequality	Greater than	Less than			
Negatives	Add/Subtract	Absolute Value			
Negatives	Multiplication	Division			
Laws of Simplifying	Combining Like Terms	Identity/Inverse			
	Associative/Commutative	Distributive			

# CHAPTER OVERVIEW (Video Instruction and Solutions Link)

# Number Line

Main Topics	Examples
Key Terms	
Negative	the negative sign means "opposite direction," as seen on the number line below.
	-5 -4 -3 -2 -1 0 1 2 3 4 5
	Example : $-\frac{7}{8}$ is just $\frac{7}{8}$ in the opposite direction.
	Addition goes to the right
	Subtraction goes to the left A negative sign means the other direction
	Example 1: Graph the points -5, 7, $-\frac{2}{3}$ , 3.7, and $\sqrt{28}$ on a
	number line.
	-7 -6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6 7

# Inequalities

Main Topics	Examples	
Symbols of Inequalities	< Less than	> Greater than
The line underneath the symbol represents when quantities could be	$\leq$ Less than or equal to	$\geq$ Greater than or equal to
equal or greater/less than.		

42					
Extra help:	sma	aller <	BIGGER		
The symbol always points to the	You can always flip the sign as long as the numbers on either side are				
smaller number.					
	flipped too! S	So:			
The lines are farther apart on the					
BIGGER side		7 > -	-8 is the SAME as $-8 < 7$		
"The alligator eats the bigger					
number."					
number.	Example 2:				
Mneumonic helps:		quality t	hat has the same meaning as $38 > 14$	•	
<ess sreater<="" td=""><td>38 &gt; 14</td><td>20</td><td>flip the sign and the numbers: 29 stays</td><td></td></ess>	38 > 14	20	flip the sign and the numbers: 29 stays		
		30	flip the sign and the numbers; 38 stays bigger		
	Answer: 14	l < 38			

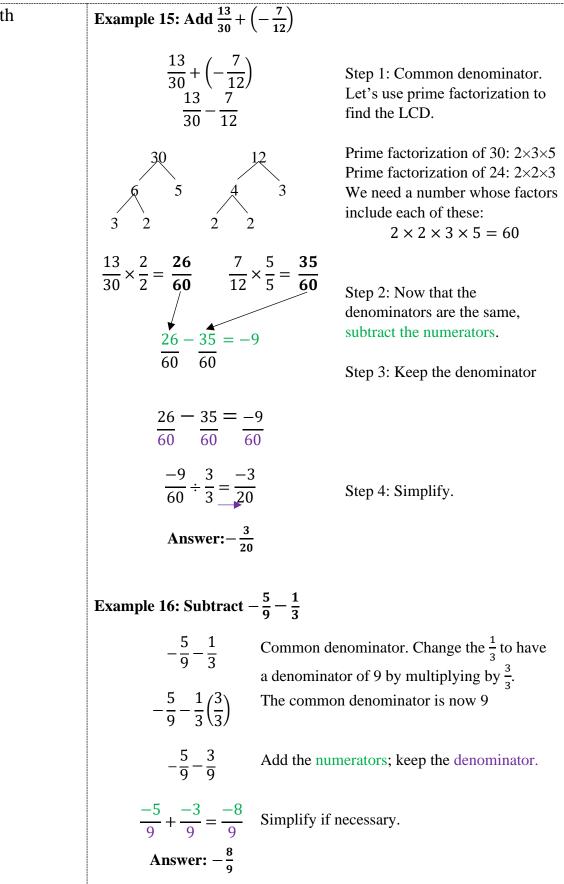
# **Absolute Value**

Main Topics	Examples	Examples					
Key Terms	Absolute Value - Me on a number line.	Absolute Value - Means to find how far away a number is from zero, like on a number line.					
Absolute Value Symbol is    .	Find the absolute va	Find the absolute value of the following					
	Example 3:	Example 4:	Example 5:				
	8  = 8	-16  = 16	5 - 18  =  -13  = 13				
	Answer: 8	Answer: 16	Answer:13				

# Adding/Subtracting Negatives

Main Topics	Examples		
Opposite Signs Subtract	Example 6:	Example 7:	Example 8:
and the Stronger Wins	7 - 11	-3 + 8	-12 + 3
	7 - 11 = -4	-3 + 8 = 5	-12 + 3 = -9
Note: Subtraction is the same as	Subtract to get 4 and	Subtract to get 5 and	Subtract to get 9 and
adding a negative.	the negative is	the positive is	the negative is
	stronger	stronger	stronger
Numbers with Same Signs	Example 9:	Example 10:	Example 11:
will add in that same	-7 - 11	-3-8	12 + 3
direction	-7 - 11 = -18	-3 - 8 = -11	12 + 3 = 15
	Add in the negative	Add in the negative	Add in the positive
	direction	direction	direction
Subtracting a Negative is	Example 12:	Example 13:	Example 14:
Addition	-7 - (-11)	-3 - (-8)	12 - (-3)
	-7 - (-11) =	-3 - (-8) =	12 - (-3) =
	-7 + 11 = 4	-3 + 8 = 5	12 + 3 = 15
	-7 + 11 = 4 Change to a plus,	-3 + 8 = 5 Change to a plus,	12 + 3 = 15 Change to a plus,
	-7 + 11 = 4	-3 + 8 = 5	12 + 3 = 15
	-7 + 11 = 4 Change to a plus,	-3 + 8 = 5 Change to a plus,	12 + 3 = 15 Change to a plus,
	-7 + 11 = 4 Change to a plus,	-3 + 8 = 5 Change to a plus,	12 + 3 = 15 Change to a plus,
	-7 + 11 = 4 Change to a plus,	-3 + 8 = 5 Change to a plus,	12 + 3 = 15 Change to a plus,
	-7 + 11 = 4 Change to a plus,	-3 + 8 = 5 Change to a plus,	12 + 3 = 15 Change to a plus,

# Examples with Fractions



Common Mistakes				
Do two negatives make a	False in Addition and Subtraction negatives and positives work against one is stronger will win.	- With addition and subtraction each other in a tug of war. Whichever		
positive?	Examples:			
	Debt is negative and income is positive. If there is more debt than income, the net result is debt.			
	If we are \$77 in debt and get	If we have \$77 and \$66 of debt,		
	income of \$66 then we have a net	then the net is a positive \$11:		
	debt of \$11:			
	-77 + 66 = -11	77 - 66 = 11		
	Falling is negative a	nd rising is positive.		
	An airplane rises 307 feet and	If, however, the airplane falls 307		
	then falls 23 feet, then the result is	feet and then rises 23 feet, then		
	a rise of 284 feet:	the result is a fall of 284 feet:		
	307 - 23 = 284	-307 + 23 = 284		
	<u> </u>			

# Section 1-1 Exercises

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**R-4** 

#### Perform the indicated operation.

**R-3** 1. 
$$3^3 - 2 \cdot 4 + \sqrt{81} \cdot 10 \div 2$$
 2. 17% of 84

#### Evaluate each formula with the given variables.

3. Evaluate 
$$\frac{5x+2}{t}$$
  
when  $x = 6$  and  $t = 4$   
4. For a cone  
 $r = 4.6$  m  
 $1 = 5.3$  m  
 $SA = ?$ 

5. I have a rectangular sand box whose length is 4 more than three times its width. If the width is 13 ft, what is the area covered by the sand box?

#### Translate into math.

- 6. Bill is 5 years older than twice the sum of Jenny's and Penny's ages.
- 7. Dave's income is 25 dollars less than 3 times Rebecca's.
- 8. There are 8 times as many bunnies as turtles.

**9.** Locate 7, -2.3, 4, -8, 
$$\pi$$
,  $\frac{9}{5}$ , and  $-\frac{3}{4}$  on a number line.  
-8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6 7 8  
For each pair of numbers write the correct increasity between them

#### For each pair of numbers write the correct inequality between them.

**10.** -2\_\_\_1.5 **11.** -3\_\_\_ - 7 **12.** 27\_\_\_13

#### Write an inequality that has the same meaning.

**13.**  $6 \ge 1.5$  **14.** 2,349 < 4,991 **15** -16 > x

Find the absolute value.

**16.** |-17| **17.** |8-14| **18.** |3(4-2)|

Perform the indicated operation by hand, and then check your answers with your calculator.

	-3 + 5	,	-4 - 7	•	5 - 18 - 3
22.	5 - (-18) + (-17)	23.	6 + (-15) - 12 - (-5)	24.	$-\frac{5}{8}+\frac{1}{4}$
25.	$-\frac{3}{20}-\frac{13}{16}$	26.	-5.7 - (-14.8)	27.	15 – 18.4

**28.** At 6:00am in Rexburg it was  $-13^{\circ} F$ . By the warmest part of the day, the temperature had risen 38 degrees. By 8:00pm it has cooled down 12 degrees. What was the temperature at 8:00pm?

**29.** Clifford is on a bridge 47 feet above the Salmon River. The fish are 15 feet below the surface of the water. How much fishing line does he need to let out to reach them?

#### **Preparation.**

**30.** Read some of 1.2 and then evaluate -2(-3)(-4)

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### **Section 1-1 Answers**

1.	64	16.	17
2.	14.28	17.	6
3.	8	18.	6
4.	$143.07 m^2$	19.	2
5.	$559 ft^2$	20.	-11
6.	B = 5 + 2(J + P)	21.	-16
7.	D = 3R - 25	22.	6
8.	b = 8t	23.	-16
9.	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	24.	$-\frac{3}{8}$
	-2 < 1.5	25.	$-\frac{77}{80}$
11.	-3 > -7	26.	9.1
12.	27 > 13	27.	-3.4
13.	$1.5 \le 6$	28.	13° F
14.	4,991 > 2,349	29.	62 ft
15.	x < -16	30.	In class

# Section 1-2 Negatives in Multiplication and Division

(VICCO Instruction and Solutions Link)				
Number Line	Positives	Negatives		
Inequality	Greater than	Less than		
Negatives	Add/Subtract	Absolute Value		
Negatives	Multiplication	Division		
Laws of Simplifying	Combining Like Terms	Identity/Inverse		
	Associative/Commutative	Distributive		

# CHAPTER OVERVIEW (Video Instruction and Solutions Link)

Main Topics	Examples		
Multiplying or	Example 1:	Example 2: Exam	ple 3:
Dividing Opposite Signs Gives a	7(-11)	-3.8	$\frac{12}{7} \times \left(-\frac{3}{5}\right)$
Negative	7(-11) = -77	$-3 \cdot 8 = -24$	$\frac{12}{7} \times \left(-\frac{3}{5}\right) = -\frac{36}{35}$
	Example 4:	Example 5:	Example 6:
	33 ÷ (-11)	$-32 \div 8$	$\frac{3}{8} \div \left(-\frac{1}{6}\right)$
	$33 \div (-11) = -3$	$-32 \div 8 = -4$	$\frac{\frac{3}{8} \div \left(-\frac{1}{6}\right)}{\frac{3}{8} \div \left(-\frac{6}{1}\right) = -\frac{18}{8} = -\frac{9}{4}}$
Multiplying or	Example 7: E	xample 8: Examp	le 9:
Dividing two negatives will be	-7(-11)	$-3 \cdot (-8) -\frac{1}{-3}$	$\frac{2}{7} \times \left(-\frac{3}{5}\right)$
positive	-7(-11) = 77 -	$-3 \cdot (-8) = 24 - \frac{12}{7}$	$\times \left( -\frac{3}{5} \right) = \frac{36}{35}$
	Example 10: E	Example 11: Examp	ole 12:
		$-32 \div -8$	$\frac{3}{8} \div \left(-\frac{1}{6}\right)$
	$-33 \div (-11) = 3$	$-32 \div -8 = 4 \qquad -\frac{3}{8}$	$\frac{56}{8} \div \left(-\frac{1}{6}\right)$ $\times \left(-\frac{6}{1}\right) = \frac{9}{4}$
Division by Zero is impossible	Example 13:	Fyamnle 14.	
(undefined)	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	$0 \qquad \frac{13}{0}$	$-\frac{3}{0}$ is undefined

Main Topics	Examples			
Common Mistakes –				
Two negatives make a	True in Multiplication and Div	vision - Since a negative sign		
positive.	simply means other direction, w	hen we switch direction twice,		
	we are headed back the way we	we are headed back the way we started.		
	Example 15:			
	-(-5	) = 5		
	Example 16:			
	-(-2)(-1)(-3)(-5) =	= 30 = -30		
	Example 17:			
	$-(-40 \div -8) =$	-(-5) = -5		
	False in Addition and Subtrac			
	subtraction negatives and positives work against each other in a			
	sort of tug of war. Whichever or	ie is stronger will win.		
	Falling is negative a	nd rising is positive.		
	An airplane rises 307 feet and	If, however, the airplane falls		
	then falls 23 feet, then the	307 feet and then rises 23		
	result is a rise of 284 feet:	feet, then the result is a fall of 284 feet:		
	307 - 23 = 284	-307 + 23 = -284		
	Other Examples:			
	Debt is negative and income is p	positive.		
	Discount is negative and markup	o or sales tax is positive.		
	Warmer is positive and colder is	negative.		
	Whichever is greater will give y	ou the sign of the net result.		

#### **Section 1-2 Exercises**

Evaluate each formula with the given variables.

**R-4** 

1. Evaluate  $\frac{3m^2+2}{n}$ when m = -4 and n = 102. For a cylinder r = 4 m h = 5.7 m SA = ?

**3.** I have a rectangular sandbox whose length is 2 more than three times its width. If the width is 13 ft, what is the area of the sand box?

#### Translate into math.

4. Chelsea is 5 years older than twice the difference between Kaitlyn's and Becca's ages.

5. Dave's speed is 15 miles per hour less than 4 times Rebecca's.

6. A population increased by 23% of the population to a level of 13,204.

#### Find the absolute value.

I ma me abbonate value.		
<b>1-1 7.</b>   - 27	<b>8.</b>   18 – 14	<b>9.</b>   80 ÷ (4 – 12)
Perform the indicated operation.		
<b>10.</b> $-4 - 17$	<b>11.</b> 5 + 18 - 3	<b>12.</b> $-6 + (-15) + 12 - (-5)$
13. $-\frac{5}{9}-\frac{1}{3}$	<b>14.</b> -5.7 - (-24.8)	<b>15.</b> -25 - 18.4

**16.** Rick went bungee jumping. After jumping off the bridge, he fell 83 feet before the bungee cords pulled him back up. On the first recoil he ascended 42 feet before starting to fall again. On his final bounce, he finally came to rest 14 feet lower than that. How far below the bridge did he come to rest?

**17.** A kite is flying above a tree when the string of the kite gets caught on a branch of the tree. There is 15 feet of string below where the string is caught and 37 feet from the tree branch up to the kite. How many total feet of string is extended?

Perform the indicated operation by hand, and then check your answers with your calculator.

1-2	18.	-5(3)	19.	3 · (-11)	20.	(-42) ÷ 6	21.	-28 ÷ (-7)
	22.	$-(6 \cdot 4)$	23.	-16 ÷ (-2)	24.	$-7(-3) \cdot (-1)$	25.	6 - 5(-9.7)
	26.	-(-8)(-6)	27.	$-\frac{5}{8}\cdot\left(-\frac{1}{3}\right)$	28.	$\frac{7}{40} \div \left(-\frac{3}{10}\right)$	29.	$-\frac{5}{44} \div \left(-\frac{1}{4}\right)$
	30.	0 ÷ 7	31.	$-\frac{13}{0}$	32.	15 ÷ 0	33.	<u>0</u> 296

#### **Preparation.**

**34.** Read some of 1.3 and then simplify the following: **a**) 2x + 4x **b**) 8 - 4 + 3y + 8y

52 Section 1-2 Answers

1.	5	18.	-15
2.	$243.79 m^2$	19.	-33
3.	$533 ft^2$	20.	-7
4.	C = 5 + 2(K - B)	21.	4
5.	D = 4R - 15	22.	-24
6.	p + .23p = 13,204	23.	8
7.	27	24.	-21
8.	4	25.	54.5
9.	10	26.	-48
10.	-21	27.	5 24
11.	20	28.	$-\frac{7}{12}$
12.	-4	29.	5 11
13.	$-\frac{8}{9}$	30.	0
14.	19.1	31.	Undefined
15.	-43.4	32.	Undefined
16.	-55 ft or $55 ft$ below the bridge	33.	0
17.	52 <i>f t</i>	34.	In class.

# Section 1-3 Laws of Simplifying

Number Line	Positives	Negatives		
Inequality	Greater than	Less than		
Negatives	Add/Subtract	Absolute Value		
Negatives	Multiplication	Division		
Laws of Simplifying	Combining Like Terms	Identity/Inverse		
	Associative/Commutative	Distributive		

#### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

### Laws of Simplifying

Main Topics	Examples
Key Terms	Simplify – No "=" signs (or >, <, etc)
Simplify	-To change the form of a number to the standard way that one usually accepts and uses numbers
Solve	<b>Solve</b> – Uses "=" signs (or >, <, etc), find out what x equals

Name	What it does	Operation	Examples
Commutative	Switch order	Addition	5 + 7 = 7 + 5
			2x + 3y = 3y + 2x
		Multiplication	7xtzy = x7tzy
Associative	Move parentheses.	Addition	7 + (5 + 1) = (7 + 5) + 1
			(x+5)+9 = x + (5+9)
		Multiplication	$7 \cdot (3 \cdot 2) = (7 \cdot 3) \cdot 2$

Associative and Commutative together allow us to move stuff around and (if we take care of multiplication before addition) add things up in any order we desire.

Identity	The invisible number	Additive: 0	6 + 0 = 6 $x + 0 = x$
		Multiplicative: 1	$6 \cdot 1 = 6$ $57y \cdot 1 = 57y$
		$\frac{7}{7}, \frac{3}{3}, and \frac{x}{x}$ are all examples of 1.	$\frac{3}{8} \cdot \frac{x}{x} = \frac{3x}{8x}$

Inverse	Cancels, or undoes the number	Additive Inverse: opposite	6 + (-6) = 0 3t + (-3t) = 0
			-17 + 17 = 0
		Multiplicative Inverse: reciprocal	$5 \cdot \frac{1}{5} = 1$
			$-17p \cdot \frac{1}{-17p} = 1$
			$\frac{2}{3} \cdot \frac{3}{2} = 1$
Distributive	Jump numbers into parentheses	Both	6(43) = 6(40 + 3) = 6(40) + 6(3) 240
			7(2x-5) = 14x - 35

## Factoring

Examples
Common Factor – a factor that two or more terms have in common
<b>Example 1:</b> Two terms: 24 and 36. Factors of 24 are 1, 2, 3, 4, 6, 8, 12, 24 Factors of 36 are 1, 2, 3, 4, 6, 9, 12, 18, 36 The numbers in boxes are the common factors between 24 and 36
Greatest Common Factor - This is the biggest factor that all terms share in common.
<b>Example 2:</b> The Greatest Common Factor of 24 and 36 is <b>12</b> , because it is a factor that they share and it is also the greatest
To factor an expression just means to pull out the greatest common factor of each term in the expression. It's like the distributive property in reverse.

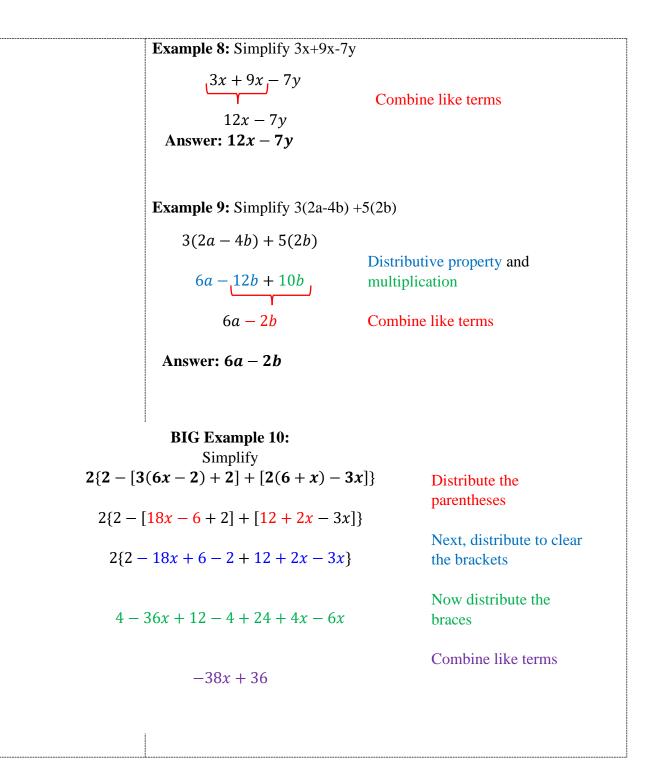
Steps to Factor:	<b>Example 3:</b> Factor 20x+4	8	
1. Identify the factors of the terms (and their coefficients).	Factors of 20: 1,2,4,5,10, Factors of 48: 1,2,3,4,6,8		List the factors of each number
<ol> <li>Choose the greatest common factor.</li> <li>Rewrite the expression having factored.</li> </ol>	Factors of 20: 1,2,4,5,10, Factors of 48: 1,2,3,4,6,8 20x + 48 4(5x + 12)	,12,16,24,48	Identify the factors in common, and choose the greatest Undistribute the 4
	Answer: 4(5x+	12)	
	<b>Example 4:</b> Factor 3x+6		
	Factors of 3: 1,3 Factors of 6: 1,2,3,6 3x + 6	C	test common factor
	$\frac{3x+6}{3}$	common facto	• •
	3(x+2) -Write the expression with th common factor on the outsid		
	Answer: 3(x+2)	the parenthese overs" inside	es and the "left-

# Simplifying with Variables

Key Terms				
Like things	Like things – in addition and subtraction we must only deal with like things. Adding and subtracting like terms works the same way with variables as it does with sheep, penguins, fractions with common denominators, and other quantities with like terms.			
	<b>Example 5:</b> 5 sheep + 2 sheep =7 sheep.			
	<b>Example 6</b> : 5 sheep + 2 penguins = ? We really can't add them together, because they aren't like things.			
	Example 7: $\frac{1}{3}$ cups of flour $+\frac{2}{3}$ cups of flour $=\frac{3}{3}$ or 1 cup of flour.			

\_\_\_\_\_

\_\_\_\_\_



#### **Section 1-3 Exercises**

#### Translate into math.

**1.** The number of quarters plus twice the number of nickels is equal to 4 less than the number of dimes.

#### Find the absolute value.

1-1

**R-4** 

**2.** |28 - 34 |

**3.** The elevation of Jericho is -846 ft. Jerusalem has an elevation of 2428 ft. If Ben travels from Jericho to Jerusalem, how much total vertical elevation will he have gained?

#### Perform the indicated operation.

1-2

1	-9 - 15 + 12 - (-5)	5.	7	(	3)
4.	=9 = 13 + 12 = (-3)	5.	$\frac{12}{12}$		8/

Use the commutative properties of addition and multiplication to rewrite each expression.

**1-3 6.** 3 + x **7.**  $27 \cdot 36$  **8.**  $x \cdot 15$  **9.** 17x - 23y

Use the associative properties of addition and multiplication to rewrite each expression.

**10.** (5+2t) + 7p **11.** 5(3x)

Create each fraction with a denominator of 15x.

**12.** 
$$\frac{4}{5x}$$
 **13.**  $\frac{7}{15}$  **14.**  $-\frac{2}{3}$ 

Find the additive inverses of each number.

**15.** 7 **16.** -4 **17.**  $-\frac{7}{3}$  **18** .05

Find the multiplicative inverses of each number.

**19.** 7 **20.** -4 **21.**  $-\frac{7}{3}$  **22.** .05

Use the distributive property.

**23.** 3(x+7) **24.** -2(x+5) **25.** 4(2x-7y+3)

Factor.

<b>20.</b> $10y + 3$ <b>21.</b> $20t + 275$ <b>20.</b> $7t = 00 + 12t$	26.	10y + 5	<b>27.</b> $20t - 24s$	28.	4a - 6b + 12c
--	-----	---------	------------------------	-----	---------------

Combine like terms and simplify.

**29.** 
$$8a + 25a$$
 **30.**  $21m^2 + 85 - 15m^2 + 16$  **31.**  $x - 37y + 16x + 13y$   
**32.**  $2(5x + 6) + 3x$  **33.**  $2(11z - 2a) + 27a - 3z$  **34.**  $-\left(\frac{1}{3}a + \frac{2}{5}\right) + 2$   
**35.**  $2^3 - 5(3x + 8) - 10$  **36.**  $23 + 5t + 7y - t - y - 27$   
**37.**  $2\{[6 - 3(2x - 3)] - [2(-x + 1) - 3(-5)]\}$   
**38.**  $-4\{[3(x - 2) + 7] - [4(3x + 2) + 3]\}$ 

**39.** 
$$7\{2 - [3(11 - 2x) + 1] - 8(2x - 4)\}$$

Section 1-3 Answers

1.	q + 2n = d - 4	26.	5(2y + 1)
2.	6	27.	4(5t - 6s)
3.	3274 ft	28.	2(2a-3b+6c)
4.	-7	29.	33a
5.	$\frac{14}{9}$ or $1.\overline{5}$	30.	$6m^2 + 101$
6.	<i>x</i> + 3	31.	17x - 24y
7.	36 · 27	32.	13x + 12
8.	15 <i>x</i>	33.	23a + 19z
9.	-23y + 17x	34.	$-\frac{1}{3}a + \frac{8}{5}$
10.	5 + (2t + 7p)	35.	-15x - 42
11.	$(5 \cdot 3)x$ or $15x$	36.	4t + 6y - 4
12.	$\frac{12}{15x}$	37.	-8x - 4
13.	$\frac{7x}{15x}$	38.	36x + 40
14.	$-\frac{10x}{15x}$	39.	-70x
15.	-7		
16.	4		
17.	$\frac{7}{3}$		
18.	05		
19.	$\frac{1}{7}$		
20.	$-\frac{1}{4}$		
21.	$-\frac{3}{7}$		
22.	20		
23.	3x + 21		
24.	-2x - 10		
25.	8x - 28y + 12		

### **Chapter 1 Review Exercises**

**1.** Make a Visual Chart of the rules, processes, and topics of Chapter 1. It should be in a grid format on one side of a page and have plenty of illustrative examples.

**Evaluate.** 

60

**R-3** 

**2.** 
$$15 \div 3 + (7 - 3 \times 6)$$
 **3.**  $(3^4 - 27 \div 3) \div 2 + 4 \cdot (-3 \cdot 2)$ 

Evaluate the expression with the given variable(s).

4.  $5r + 7r^2$ ; when r = -35.  $\frac{6a}{b}$ ; when a = 3, b = 4

6. Roy earns m amount of money per month. Jessica earns 2m - 360. How much does Jessica earn if Roy earns \$700 per month?

#### Translate the following into math.

- **R-4 7.** Frank is 23 years less than twice Julie's age.
  - 8. There are three times as many kittens as puppies.
  - 9. A price increased by 7% of the price is equal to \$363.80.

#### Change these fractions into decimals.

**10.** 
$$-\frac{7}{3}$$
 **11.**  $\frac{-1}{-20}$ 

Write an inequality that has the same meaning.

**12.**  $-1 \le 5.9$  **13.** m < 99 **14.** -16 > -120

Find the absolute value.

**15.** |14| **16.** |5-7.3| **17.** |3(1-6)|

Perform the indicated operations.

1-2

1-1

<b>18.</b> $5 - (-3) + (-17)$	<b>19.</b> $3 + (-15) - 12 - (-5)$	<b>20.</b> $-\frac{1}{8}+\frac{3}{4}$
<b>21.</b> $-\frac{2}{7}-\frac{3}{14}$	<b>22.</b> -4.21 - 3.2	<b>23.</b> 8.1 – (–9.1)
<b>24.</b> $-3.8(-4) \cdot 7$	$25.  \frac{3^2 - (4+9) \cdot 3}{2(3-8)}$	<b>26.</b> $-27 \div (003)$

**27.** One of the stock market indices started the week at 2,901 points. During Monday, it lost 130 points. Tuesday is gained 57 points. Wednesday it gained 110. How many total points did it have after closing on Wednesday?

**28.** An anchor dropped from a large cruise ship starts at 22 feet above sea level and the ocean floor is 57 feet below sea level, how much chain must be let out?

#### Write an equivalent fraction for each of the following with a denominator of 36x.

<b>29.</b> $\frac{1}{3}$	30.	<u>5</u> 12	31.	$\frac{2}{3x}$

Multiply.

1-3

**32.** 5(x-2y) **33.** m(3+5t)

Factor.

34.	3ty - 2t	35.	20 + 5b + 15c
-----	----------	-----	---------------

Simplify by collecting like terms.

**38.**  $2\{[3(x+2)+4x]-[5+2(x-4)]\}$  **39.**  $7\{2m+3[5+3(m-7)]\}$ 

Chapt	er 1 Review Answers		
1.	Submit the complete, one-page chart.	21.	$-\frac{1}{2}$
2.	-6	22.	-7.41
3.	12	23.	17.2
4.	48	24.	106.4
5.	$\frac{9}{2}$ or 4.5	25.	3
6.	\$1040	26.	9,000
7.	F = 2J - 23	27.	2,938
8.	k = 3p	28.	79 ft
9.	P + .07P = 363.80	29.	<u>5x</u> 36x
10.	-2.3	30.	$\frac{15x}{36x}$
11.	.05	31.	$\frac{24}{36x}$
12.	$5.9 \ge -1$	32.	5x - 10y
13.	99 > m	33.	3m + 5mt
14.	-120 < -16	34.	t(3y - 2)
15.	14	35.	5(4 + b + 3c)
16.	2.3	36.	10t - 63
17.	15	37.	16x + 81
18.	-9	38.	10x + 18
19.	-19	39.	77 <i>m</i> – 336
20.	5 8		

3c)

# Section 2-1 The 3-Step Process to Solving

### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

	GOAL: Get x alone (x will represent any variable)
	1. SIMPLIFY
2.3	A) Distribute Across ()
2.5	B) Get rid of fractions (multiply all by LCD)
2.3	C) Combine "Like terms" and get all x's on the same side
2.1	2. ADDITION PRINCIPLE
2.1	3. MULTIPLICATION PRINCIPLE
2.2	Applications: Shapes, Formulas, Solving for a Variable
2.4	Applications: Substitution and Percents
2.6	Inequalities
2.7	Inequalities and Applications

## **Basics**

Definitions & Basics	Examples				
	Simplify:				
Algebra: Two types of	No "=" signs (or >, <, etc.)				
Problems	Combine like terms Example: 2x+3x				
Simplify &	Answer: 5x				
Solve					
	Solve:				
	Uses "=" signs (or >,<, etc.)				
	3x = 15 Example: $3x=15$				
	Find out what x equals				
	3x 15				
	$\overline{3} = \overline{3}$ Divide each side by 3				
	x = 5				
	Answer:  x = 5				
Equation:	A mathematical sentence. It must have an equal sign and an expression on				
	each side.				
	1+3 = 4; x = 5; or x + 7 = 10				
	Any number when replaced for the variable that makes an equation true.				
Solution:	Example: $x = 3$ is the "SOLUTION" for the equation $x+7 = 10$				
	Example. $x = 5$ is the SOLOTION for the equation $x + 7 = 10$				
Solve:	Find all the "SOLUTIONS" for an equation.				

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<ul> <li><u>Checking a solution</u></li> <li>1. Plug into the equation.</li> <li>2. Simplify.</li> <li>3. If the result is a true statement, the number is a solution.</li> </ul>	5 - 15 = -10 5 + (-15) = -10 -10 = -10 <b>Answer:</b> $x = 5$ is a set <b>Example 2:</b> Is $x = -4$ a solution to 5(-4) + 23 = 43 -20 + 23 = 43	It is a true statement <b>blution</b> the equation: $5x + 23 = 43$ ? Plug -4 into the equation. Simplify combining like terms. It is a false statement.

# **The Balance Rule**

The Dalance Kule	
Balance Rule of Solving	Examples
Whatever I do to one side of the equal sign, I must do the exact same to	Example 3:
the other side to maintain equality.	2(23) = 2(23) Multiplying <u>each side</u> by 2. 46 = 46
	46 - 4 = 46 - 4 Subtract 4 from <u>each side</u> . 42 = 42 $42 \div 7 = 42 \div 7$ Divide <u>each side</u> by 7.
Equivalent Equations:	6 = 6 The equation stays balanced.
Equivalent is a big word for equal or SAME. Thus, equivalent equations have the same solutions.	<b>Example 4:</b> Use the BALANCE RULE to keep the equations below equivalent or the SAME.
	36 = 36 $-4$ is subtracted from the left side $-4$
	36 = 36We must do the same thing (in $-4$ $-4$ $32 = 32$ The equation is balanced

<b>Example 5:</b> Use the BALANCE RULE to keep the equations below equivalent or the SAME.
x - 7 = 14 + 7 is added to the right side +7
x - 7 = 14 We must do the same thing (in
+7 $+7$ blue) to the other side
x = 21 The equation is balanced
<b>Example 6:</b> Use the BALANCE RULE to keep the equations below equivalent or the SAME.
$\frac{7x}{7} = \frac{21}{7}$ 7 is divided to the left side
$\frac{7x}{7} = \frac{21}{7}$ We must do the same thing (in blue) to the other side
x = 3 The equation is balanced

# **3-Step Process to solving: The Addition Principle**

The Addition Principle	Examples	·····				
The GOLDEN	3-Step Process to Solving					
Directions:	<ul> <li>GOAL: Get x alone (x will represent any variable)</li> <li>1. SIMPLIFY <ul> <li>A) Distribute Across ().</li> <li>B) Get rid of fractions (multiply all by LCD).</li> <li>C) Combine "Like terms" and get all x's on the same side.</li> </ul> </li> <li>2. ADDITION PRINCIPLE.</li> <li>3. MULTIPLICATION PRINCIPLE.</li> </ul>					
	Example 7: Solve	x + 5 = 15				
To Get x alone						
2) Identify what is being added or	x + 5 = 15	5 is being added to $x$				
subtracted to your variable. 3) Do the opposite	x + 5 = 15 -5 - 5	Do the opposite (subtract 5) to both sides.				
(operation) to <u>both</u> <u>sides</u> of the equation.	x + 0 = 10	<u>Check</u> , is 10 the solution to the equation: $x + 5 = 15$ ?				
-1	10 + 5 = 15	Plug in the answer into the original equation				
	15 = 15	True, 10 is a Solution				
	Answer: $x = 10$					

Note: International students may be familiar with moving the number to the opposite side of the equation with the inverse operation. This is called "transposition", was used in the U.S. for decades, and is equivalent to what is being taught here.

-4.3 = y - 7.7	7.7 is being subtracted from $y$
-4.3 = y - 7.7 +7.7 + 7.7	Do the opposite (add 7.7) to both sides.
3.4 = y + 0 $3.4 = y$	<u>Check</u> , is 3.4 the solution to the equation: $-4.3 = y - 7.7$ ?
-4.3 = 3.4 - 7.7	Plug in the answer into the original equation
-4.3 = -4.3	True, 3.4 is a Solution
Answer: $y = 3.4$	
<b>Example 9:</b> Solve $-\frac{3}{4}$	$+x=\frac{5}{8}$
$-\frac{3}{4} + x = \frac{5}{8}$	$-\frac{3}{4}$ is being added to x
$-\frac{3}{4} + x = \frac{5}{8} + \frac{3}{4} + \frac{3}{4} + \frac{3}{4}$	Do the opposite (subtract) to both sides. $-\left(-\frac{3}{4}\right) = +\frac{3}{4}$
$0 + x = \frac{11}{8}$	Simplify
$x = \frac{11}{8}$	<u>Check</u> , is $\frac{11}{8}$ the solution to the equation $-\frac{3}{4} + x = \frac{5}{8}$ ?
$-\frac{3}{4} + \frac{11}{8} = \frac{5}{8}$	Plug in the answer into the original equation
$\frac{5}{8} = \frac{5}{8}$	True, $\frac{11}{8}$ is a Solution
Answer: $x = \frac{11}{8}$	

Multiplication Principle	Examples			
	<b>Example 10:</b> Solve $3x = 15$			
<b>To Get</b> <i>x</i> <b>alone</b> 2) Identify what is	3x = 15	3 is being multiplied to <i>x</i>		
being multiplied or divided to your	$\frac{3x}{3} = \frac{15}{3}$	Do the opposite (divide) to both sides.		
variable. 3) Do the opposite	3 3	Simplify		
(operation) to <u>both</u>	x = 5			
sides of the equation.	Answer: $x = 5$			
	<b>Example 11:</b> Solve $\frac{x}{-4}$	= -12		
	$\frac{x}{-4} = -12$	-4 is being divided into x		
	$-4\left(\frac{x}{-4}\right) = -4(-1)$	2) Do the opposite (multiply) to both sides.		
	$-4\left(\frac{x}{-4}\right) = -4(-1)$	2) Simplify		
	Answer: $x = 48$			
	<b>Example 12:</b> Solve $\frac{2}{5}$	$=\frac{4}{15}b$		
Note: The cancelling seen here can also be done by multiplying	$\frac{2}{5} = \frac{4}{15}b$	$\frac{4}{15}$ is being multiplied to <i>b</i>		
numerators and denominators, then simplifying.	$\frac{15}{4} \cdot \frac{2}{5} = \frac{15}{4} \cdot \frac{4}{15}b$	Do the opposite (divide) to both sides. $\frac{4}{15} \div \frac{4}{15} = \frac{4}{15} \cdot \frac{15}{4}$		
	$\frac{315}{24} \cdot \frac{2}{5} = \frac{15}{4} \cdot \frac{4}{15} b$	Simplify		
	Answer: $x = \frac{3}{2}$			
L	<u> </u>			

# **3-Step Process to solving: The Multiplication Principle**

Addition & Multiplication Principles	Examples				
	<b>Example 13:</b> Solve $3x + 10 = 22$				
<b>GOAL: Get</b> <i>x</i> <b>alone</b> ( <i>x</i> will represent any variable)	3x + 10 = 22 Use the Addition Principle 10 is being added to x				
1. SIMPLIFY	3x + 10 = 22 Do the opposite (subtract 10) to both sides. -10 - 10				
<ul> <li>A) Distribute ( ).</li> <li>B) Get rid of Fractions (multiply all by LCD).</li> </ul>	3x = 12	Simplify			
C) Combine Like Terms (L.T.) and Get all <i>x</i> 's to 1 side.	3x = 12	Use the Multiplication Principle 3 is being multiplied to <i>x</i>			
2. ADDITION PRINCIPLE.	$\frac{3x}{3} = \frac{12}{3}$ Do the opposite (divide 3) to both sides.				
3. MULTIPLICATION PRINCIPLE.	x = 4 Simplify				
	<b>Answer:</b> $x = 4$ <b>Example 14:</b> Solve 12.	4 - 4.5b = -16.4			
	12.4 - 4.5b = -10	<ul><li>6.4 Use the Addition Principle</li><li>12.4 is being added to b</li></ul>			
		<ul><li>6.4 Do the opposite (subtract 12.4)</li><li>2.4 to both sides.</li></ul>			
	-4.5b = -28.8	Simplify			
	$\frac{-4.5b}{-4.5} = \frac{-28.8}{-4.5}$	Use the Multiplication Principle			
	b = 6.4 <b>Answer:</b> $b = 6.4$				

# SOLVING: Using Both Addition and Multiplication Principles Together

#### **Section 2-1 Exercises**

Find the Volume of a rectangular solid when the width, height and length are given. Formula is V = lwh

1. l = 4 in 2.  $l = 7 \, {\rm ft}$ 3. l = 7.2 m**R-4** w = 2.5 in w = 4 ftw = 9 mh = 3 mh = 3 in h = 2.8 ftV = $\mathbf{V} =$ V =

Find the Area of a trapezoid when the bases and height are given.

Formula is  $A = \frac{1}{2}h(B+b)$ 

4.	B = 15	5.	B = 21	6.	B = 19
	b = 10		b = 11		b = 6
	h = 7		h = 3		h = 10
	A=		A=		A=

Identify the property that is illustrated by each statement.

**1-3 7.** (8+5)+3=3+(8+5) **8.** (3xy)7x = (3yx)7x **9.** (8ab)7c = 8(ab7)c

#### Simplify.

**10.** 2s(t-7) - 6t(s+3) **11.**  $3(x^2 - 5n) + 3n - 7x^2$  **12.** 6kj - 7k + 8kj + 11



Check to see if the specified number is a solution for the given equation.

**13.** 13; y + 24 = 37 **14.** 19; p + 14 = 32 **15.** 24; t - 34 = 58 **16.** 45; x - 21 = 24Is 13 a solution for y + 24 = 37? 14 = 32?

#### Solve.

17.	x + 4 = 13	18.	13 + t = 27	19.	y + 17 = -12
20.	$y + \frac{2}{7} = 6$	21.	$x + \frac{9}{2} = 4$	22.	$8 = x - \frac{5}{8}$
23.	p - 16.2 = 11.2	24.	-6.1 + x = -6.7	25.	-4.2 + z = -3.1
26.	-y = 15	27.	45 = -x	28.	-p = -34
29.	$\frac{8}{3}y = 16$	30.	$-\frac{x}{4} = \frac{1}{6}$	31.	$\frac{7}{4} = -\frac{x}{5}$
32.	$\frac{4}{5}p = -5.6$	33.	$-\frac{4}{3}z = -15.3$	34.	$\frac{-x}{14} = 6$

35.	12x + 7 = 31	36.	4y + 18 = 30	37.	5z + 21 = 56
38.	5x - 5 = 20	39.	3y - 7 = 27	40.	-8x - 10 = 62
41.	-4x - 12 = 18	42.	2.7m + 12.13 = 20.5	43.	-3.5x + 2.4 = 24.1

Preparation: Read some of 2.2 and then

**44.** Solve for p: 3p + 7 = 15

**45.** Solve for p: mp + t = q

beeno			
1.	30 in <sup>3</sup>	29.	y = 6
2.	78.4 ft <sup>3</sup>	30.	$x = -\frac{2}{3}$
3.	194.4 m <sup>3</sup>	31.	$x = -\frac{35}{4} or - 8\frac{3}{4}$
4.	87.5	32.	p = -7
5.	48	33.	z = 11.475
6.	125	34.	x = -84
7.	Commutative property of addition	35.	x = 2
8.	Commutative property of multiplication	36.	y = 3
9.	Associative property of multiplication	37.	z = 7
10.	-4st - 14s - 18t	38.	x = 5
11.	$-4x^2 - 12n$	39.	$y = \frac{34}{3}$ or $11\frac{1}{3}$
12.	14kj - 7k + 11	40.	x = -9
13.	Yes	41.	$x = -7.5 \ or \ -\frac{15}{2}$
14.	No	42.	m = 3.1
15.	No	43.	x = -6.2
16.	Yes	44.	In class
17.	x = 9	45.	In class.
18.	t = 14		
19.	y = -29		
20.	$y = 5\frac{5}{7} or \frac{40}{7}$		
	$x = -\frac{1}{2} or5$		
22.	$x = 8\frac{5}{8} or \frac{69}{8} or 8.625$		
	p = 27.4		
24.	x = -0.6		
25.	<i>z</i> = 1.1		
26.	y = -15		
27	45		

**27.** x = -45

**28.** *p* = 34

# <sup>72</sup> Section 2-2 Applications and Formulas

EF	ER OVERVIEW ( <u>Video Instruction and Solutions Link</u> )						
		GOAL: Get x alone (x will represent any variable)					
		1. SIMPLIFY					
	2.3	A) Distribute Across ()					
	2.5	B) Get rid of fractions (multiply all by LCD)					
	2.3	C) Combine "Like terms" and get all x's on the same side					
	2.1	2. ADDITION PRINCIPLE					
	2.1	3. MULTIPLICATION PRINCIPLE					
	2.2	Applications: Shapes, Formulas, Solving for a Variable					
	2.4	Applications: Substitution and Percents					
	2.6	Inequalities					
	2.7	Inequalities and Applications					

# CHAPTER OVERVIEW (Video Instruction and Solutions Link)

<b>D.U.P.E. Process for word</b>	problems with	translation & formulas
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Main Topics	Examples			
D. U. P. E.	Data – Find the information (numbers, formulas, relationships, etc.).			
	Unknown - What value are you finding? Assign it a <b>variable</b> .			
	Plan – Think: "How can I use the data to make an equation?"			
	Equation – Make an equation from your plan. Then solve it!			
Goal: Solve for m	<b>Example 1:</b> Seven less than 3 times what number is 41?			
D- Data.	7, 3, 41 are the numbers involved. Let $m$ be the number			
U-Unknown.	we don't know.			
P- Plan (translating).	Seven less than 3 times what number is 41?			
E-Equation.	3 <i>m</i> 7 = 41			
	3m - 7 = 41			
	3m = 48			
	m=16			
	Answer:16			
	<b>Example 2:</b> Stacey traveled 81 miles while going 27 mph. Using the			
D- Data.	formula $rt = d$ , determine the time that she traveled.			
	d=81 miles			
U-Unknown.	<i>r=27 mph</i>			
P- Plan (use formula).	t=?			
E-Equation.	rt=d			
	(27)t = (81)			
	÷27 ÷27			
	<i>t</i> = 3			
	Answer: 3 hours			

# Common Geometry Formulas

<i>l</i> <i>w</i> Rectangle	P = 2l + 2w $A = lw$	<ul> <li><i>P</i> is the Perimeter</li> <li><i>l</i> is the length</li> <li><i>w</i> is the width</li> <li><i>A</i> is the Area</li> </ul>
<i>a h h</i> Parallelogram	P = 2a + 2b $A = bh$	<ul> <li><i>P</i> is the Perimeter</li> <li><i>a</i> is a side length</li> <li><i>b</i> is the other side length</li> <li><i>h</i> is height</li> <li><i>A</i> is the Area</li> </ul>
a h d B Trapezoid	$P = b + a + B + d$ $A = \frac{1}{2}h(B + b)$	<ul> <li><i>P</i> is Perimeter</li> <li><i>b</i> is the little base</li> <li><i>B</i> is the big Base</li> <li><i>a</i> is a leg</li> <li><i>h</i> is height</li> <li><i>d</i> is a leg</li> <li><i>A</i> is the Area</li> </ul>
h h Triangle	$P = s_1 + s_2 + s_3$ $A = \frac{1}{2}bh$	$P$ is the Perimeter $h$ is height $b$ is base $A$ is the Area $s_1$ is one side $s_2$ is a second side $s_3$ is the third side
<i>a</i> Triangle	a + b + c = 180	<ul> <li><i>a</i> is one angle</li> <li><i>b</i> is another angle</li> <li><i>c</i> is another angle</li> </ul>
h l Rectangular Solid	SA = 2lw + 2wh + 2lh $V = lwh$	<ul> <li><i>l</i> is the length</li> <li><i>h</i> is the height</li> <li><i>w</i> is the width</li> <li><i>SA</i> is the Surface Area</li> <li><i>V</i> is Volume</li> </ul>

r	$C = 2\pi r$ $A = \pi r^2$	<ul> <li><i>C</i> is the Circumference or perimeter</li> <li><i>π</i> is a number, about 3.14159 (it has a button on your calculator)</li> <li><i>r</i> is the radius of the circle</li> <li><i>A</i> is the area inside the circle.</li> </ul>
r h Cylinder	$LSA = 2\pi rh$ $SA = 2\pi rh + 2\pi r^{2}$ $V = \pi r^{2}h$	<ul> <li>LSA is Lateral Surface Area = Area just on the sides</li> <li>h is the height</li> <li>SA is total Surface Area</li> <li>π is a number, about 3.14159 (it has a button on your calculator)</li> <li>r is the radius of the circle</li> <li>V is Volume</li> </ul>
Cone	$LSA = \pi rl$ $SA = \pi r^{2} + \pi rl$ $V = \frac{1}{3}\pi r^{2}h$	h  is the height r  is the radius of the circle l  is the slant height $\pi \text{ is a number, about 3.14159} (it has a button on your calculator)}$ SA  is total Surface Area $LSA \text{ is Lateral Surface Area} = \text{Area just on the sides}}$ V  is Volume
sphere re	$SA = 4\pi r^2$ $V = \frac{4}{3}\pi r^3$	<i>r</i> is the radius <i>SA</i> is the Surface Area <i>V</i> is the Volume

Main Topics	Examples		
	<b>Example 3:</b> If the angles of a triangle are 66°, x, and 2x, solve for x.		
D- Data.	66° is the angle we know		
	x = what we are trying to find		
U-Unknown.			
P- Plan(use the formula for	angles add to 180		
a triangle).	66 + x + 2x = 180		
E-Equation.	66 + 3x = 180		
Solve as before.			
	66 + 3x = 180		
	2 114		
	3x = 114		
	x = 38		
	$\lambda = 50$		
	If $x = 38$ , then $2x = 78$ .		
	<b>Answer:</b> The three angles are 66°, 38°, and 78°.		
	Example 4: Using the formulas for a cylinder find the missing variable:		
	$r = 9cm$ $h = ?$ $V = 356 cm^3$		
D- Data.	r = 9cm		
U-Unknown.	$V = 356  cm^3$		
P- Plan(use the formula for	h = height that we are trying to find		
volume).	$V = \pi r^2 h$		
E-Equation.	$356 = \pi(81)h$		
Solve as before.	356 = 254.47h		
	356 254.47 <i>h</i>		
	$\frac{1}{254.47} = \frac{1}{254.47}$		
	1 4 - b		
	1.4 = h Answer: height is 1.4 cm		

### Solving for Variable

ple 5: Solve $rt=d$ for rt = d for t $\frac{rt}{r} = \frac{d}{r}$ $t = \frac{d}{r}$ Answer: $t = \frac{d}{r}$ ple 6: Solve $y - c =y - c = bx\frac{y - c}{b} = \frac{bx}{b}$	
y-c=bx	= bx for x
$\frac{y-c}{b} = x$ Answer: $x = \frac{y-c}{b}$ ple 7: Solve $-3m - 3m - 4pt = 7$ for m $-3m = 7 + 4pt$	Note that the answer could also be written as $x = \frac{-c+y}{b}$ .
$m = \frac{7+4pt}{-3}$	Note that the answer could also be written as $m = -\frac{7+4pt}{3}$ or $m = \frac{-7-4pt}{3}$ or $m = -\frac{7}{3} - \frac{4pt}{3}$
	$\frac{-3m}{-3} = \frac{7+4pt}{-3}$

### **Section 2-2 Exercises**

2-2

Check to see if the specified number is a solution for the given equation.

2-1	1.	4; $7y + 13 = 15$	2.	9; 99 - 3 <i>p</i> = 72	3.	-21; y + 4 = y + 4
Solve.						
	4.	t - 15 = 43	5.	y - 22 = 23	6.	p - 12 = -21
	7.	$\frac{8}{9} + y = \frac{13}{6}$	8.	8.1 = 4.2 + x	9.	12.6 = z - 13.3
	10.	$\frac{2}{5}x = \frac{1}{10}$	11.	$-\frac{4}{9}y = \frac{1}{3}$	12.	$-\frac{5}{7} = -\frac{15}{14}z$
	13.	3.6y = 18	14.	94.8 = 23.7x	15.	-2.1z = 12.6
	16.	7y + 7 = 35	17.	2z + 13 = 3	18.	4y + 25 = 13
	19.	21 - x = 13	20.	9 - 5y = 27	21.	-14 - 6y = 17

**22.** 27 is 6 more than 3 times a number. What is the number?

23. 18 less than 5 times a number is 52. What is the number?

24. A triangle has angles that measure x, 3x, and 72°. Solve for x and find the angle measures.

**25.** If a cone has a Lateral Surface Area of 250  $ft^2$ , a radius of 8ft, what is the slant height of the cone?

**26.** If a cylinder has a volume of  $538 \text{ cm}^3$  and a radius of 6 cm, how tall is it?

**27.** Find the missing variable for a rectangle:

$$P = 39 \text{ ft}$$
  
w = 7.2 ft  
 $l =$ 

**28.** Find the missing variable for a cylinder:

$$SA = 800 \text{ in}^2$$
$$h =$$
$$r = 9 \text{ in}$$

**29.** 
$$y = mx + b$$
 for  $b$ **30.**  $5m - 7 = r$  for  $m$ **31.**  $A = 2\pi rh$  for  $h$ **32.**  $A = \frac{1}{2}bh$  for  $b$ **33.**  $3m - 8qt = 14$  for  $m$ **34.**  $19 = 3pqr$  for  $r$ **35.**  $C = \frac{5}{9}(F - 32)$  for  $F$ **36.**  $V = \frac{1}{3}\pi r^2 h$  for  $h$ 

### Preparation.

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- **37.** After reading some from Section 2.3, try to solve this equation for x.  $x + \not\equiv 9 + \not\equiv$
- **38.** Solve the following for *x*: 5x + 9y + 10p = 9y + 15 + 10p

### Section 2-2 Answers

1.	No	26.	4.76 cm
2.	Yes	27.	12.3 ft
3.	Yes	28.	5.15 in
4.	t = 58	29.	b = y - mx
5.	<i>y</i> = 45	30.	$m = \frac{r+7}{5}$
6.	p = -9	31.	$h = \frac{A}{2\pi r}$
7.	$y = \frac{23}{18}$	32.	$b = \frac{2A}{h}$
8.	x = 3.9	33.	$m = \frac{14 + 8qt}{3}$
9.	<i>z</i> = 25.9	34.	$r = \frac{19}{3pq}$
	$x = \frac{1}{4}$	35.	$F = \frac{9}{5}C + 32$
11.	$y = -\frac{3}{4}$	36.	$h = \frac{3V}{\pi r^2}$
12.	$z = \frac{2}{3}$	37.	In class.
13.	y = 5	38.	In class.
14.	x = 4		
15.	z = -6		
16.	y = 4		
17.	z = -5		
18.	y = -3		
19.	x = 8		
20.	$y = -\frac{18}{5}$		
21.	$y = -\frac{31}{6} or - 5\frac{1}{6} or - 5.1\overline{6}$		
22.	7		
23.	14		
24.	x = 27; angles 27°, 81°, 72°		
25.	9.95 ft		

Answers for numbers 29-36 are acceptable if expressed in a different but equivalent form.

		(Index more defined and solutions limit)					
		GOAL: Get x alone (x will represent any variable)					
		1. SIMPLIFY					
	2.3	A) Distribute Across ()					
	2.5	B) Get rid of fractions (multiply all by LCD)					
	2.3	C) Combine "Like terms" and get all x's on the same side					
	2.1	2. ADDITION PRINCIPLE					
	2.1	3. MULTIPLICATION PRINCIPLE					
ſ	2.2	Applications: Shapes, Formulas, Solving for a Variable					
	2.4	Applications: Substitution and Percents					
	2.6	Inequalities					
	2.7	Inequalities and Applications					

### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

# Combine "like terms" and get all x's on one side

Main Topics	Examples					
	<b>Example 1:</b> Solve $9(x + 2) - 4x = 28 + x + 2$					
<b>GOAL: Get</b> <i>x</i> <b>alone</b> ( <i>x</i> will represent any variable)	9(x + 2) - 4x = 28 + x + 2 9x + 18 - 4x = 28 + x + 2	First distribute into the parentheses				
1. Simplify A) Distribute across ( ).	9x + 18 + 4x = 28 + x + 2 5x + 18 = 30 + x	Combine all of the like terms on each side of the equation				
<ul><li>B) Get rid of fractions</li><li>(multiply all by LCD).</li><li>C) Combine "like terms"</li><li>and get all <i>x</i>'s on the same side.</li></ul>	5x + 18 = 30 + x - x $-x - x$ $4x + 18 = 30$	Get all of the x's on one side of the equation				
<ol> <li>Addition Principle.</li> <li>Multiplication Principle.</li> </ol>	$4x + 18 = 30 \\ -18 - 18$	Subtract 18 from both sides				
	4x = 12					
	$4x = 12$ $\div 4 \div 4$ $x = 3$ Answer: $x = 3$	Divide both sides of the equation by 4 to get the x alone				

<b>Example 2:</b> Solve 24 – 2(	(3x - 4) = -4
24 - 2(3x - 4) = -4 24 - 6x + 8 = -4	First distribute into the parentheses
24 - 6x + 8 = -4 32 - 6x = -4	Combine all of the like terms on each side All terms with x-s are already on the same side.
32 - 6x = -4 (-32) (-32) $-6x = -36$	Subtract 32 from both sides.
-6x = -36 $\div (-6) \div (-6)$ x = 6	Divide both sides of the equation to get the x alone
Answer: $x = 6$	

# **Distribute across Parentheses**

Main Topics	Examples				
	<b>Example 3:</b> Simplify: $4[6(1 + x) - 3x] = 6 - 2(5 - x)$				
<ol> <li>Simplify.</li> <li>A) Distribute across ( ).</li> <li>B) Get rid of fractions (multiply all by LCD).</li> </ol>	4[6(1+x) - 3x] = 6 - 2(5-x) $4[6+6x - 3x] = 6 - 10 + 2x$	Distribute into the parenthesis Distribute into the brackets			
<ul> <li>C) Combine "like terms" and get all <i>x</i>'s on the same side.</li> <li>2. Addition Principle.</li> <li>3. Multiplication Principle.</li> </ul>	24 + 24x - 12x = 6 - 10 + 2x $24 + 12x = -4 + 2x$	Combine like terms			
	$24 + 12x = -4 + 2x$ $-2x \qquad -2x$	Get all of the x's on one side			
	10x + 24 = -4				
	$10x + 24 = -4 \\ -24 - 24$	Subtract 24 from both sides			
	10x = -28 $\div 10 \div 10$ x = -2.8	Divide by the number attached to the x			
	Answer: $x = -2.8$				

## **Special Cases**

Main Topics	Examples	
	<b>Example 4:</b> Solve $2x + 1 =$	2x + 1
If equation becomes a statement that is true all the time, the answer is all real numbers.	$ \begin{array}{c}                                     $	Get all x's on one side The x's all vanished!
There are an infinite number of solutions.	Solution is all real numbers if you get something like: 0 = 0 5 = 5 -3 = -3 Answer: All Real Numbers	
	Example 5: Solve $2x + 1 = 2x$ 2x + 1 = 2x - 5 -2x - 2x 1 = -5 There is no solution if you	$\frac{x - 5}{\text{Get all x's on one side}}$ Again, the x's all vanished.
If the equation is an untrue statement then the answer is no solution.	There is <b>no solution</b> if you get something like: 0 = 1 5 = 7 -3 = 2 <b>Answer: No Solution</b>	

### **Section 2-3 Exercises**

Solve.

Solve for specified variable.

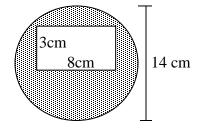
1.  $\frac{x}{-6} = -3$ 2. 13.7 - 3.4t = -18.93. -17 - 7m = -184.  $\frac{3}{7}t + 1 = -11$ 5. 9 = 3x + 176.  $\frac{5x+7}{4} = 13$ 7. 8t + 3t + 14t - 17 = -178. 94.8 = 23.7x - 13.59. p = fx + bn for f10.  $F = \frac{xf - xz}{2}$  for f11. M = 5t - 3p for t12.  $LSA = \pi rl$  for r13.  $E = Q - \frac{T_1}{T_2}$  for Q14.  $\frac{3s - 4g}{7} = c$  for g

15. 48 is 9 more than 3 times a number. What is the number?

16. 18 less than 7 times a number is 80. What is the number?

- 17. If two angles of a triangle are  $70^{\circ}$  and  $48^{\circ}$ , what is the measure of the third angle?
- **18.** What is the width of a rectangle that has an area of  $390 \text{in}^2$  and a length of 20 in?

19. Find the area of the shaded region:



**20.** What is the slant height of a cone that has radius of 7m and a surface area of  $700m^2$ ?

**21.** What is the width of a rectangular solid that has a volume of 238mm<sup>3</sup>, a length of 17mm and a height of 2mm?

**22.** If a cone has a volume of  $338 \text{ cm}^3$  and a radius of 6 cm, how tall is it?

**23.** Find the missing variable for a parallelogram:

$$A = 64 \text{ in}^2$$
  
 $h =$   
 $b = 12.6 \text{ in}$ 

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Solve.

24.	5p + 12 = 33 - p	25.	7n + 18 = 5(n - 2)	26.	5x - 10 = 5x + 7
27.	x - 7 = 15x	28.	2x - 4(x - 3) = -2x + 12	29.	.07x = 1312x
30.	.7(3x-2) = 3.5x + 1	31.	3x - 9 + 2x = 4x - 3	32.	.4y = 78 + .4y
33.	7(x-5) - 3x = 4x - 35	34.	9x - 4(x - 3) = 15x	35.	2x - 3x + 7x = 9x + 8x

### Preparation.

**36.** Find the final price of an object that is \$200 but has 15% off.

**37.** Find the final amount of a savings account that as \$170 and then has 15% added to it.

**38.** After reading some of Section 2-4, try to find out what the original price of an object was if the final price after 15% off was \$85.

## Section 2-3 Answers

- 1. *x* = 18 **2.** *t* = 9.59 3.  $m = \frac{1}{7}$ 4. t = -285.  $x = -\frac{8}{3}$ **6.** *x* = 9 7. t = 0**8.** *x* = 4.57 9.  $f = \frac{p-bn}{x}$ 10.  $f = \frac{2F+xz}{x}$ 11.  $t = \frac{M+3p}{5}$ 12.  $r = \frac{LSA}{\pi l}$ **13.**  $Q = E + \frac{T_1}{T_2}$ 14.  $g = \frac{7c - 3s}{-4}$  or  $\frac{3s - 7c}{4}$ **15.** *x* = 13 **16.** *x* = 14 **17.** 62° **18.** 19.5 *in* **19.** 129.9 *cm*<sup>2</sup> **20.** 24.83 *m*
- **21.** 7 *mm*
- 22.  $h = 8.97 \ cm$

- 23. h = 5.08 in24.  $p = \frac{7}{2} or 3.5$ 25. n = -1426. No solution 27.  $x = -\frac{1}{2}$ 28. All real numbers 29. 68.42
- **30.**  $x = -\frac{12}{7} \text{ or } -1.71$
- **31.** x = -3.53
- 32. No solution
- **33.** All real numbers

34. 
$$x = \frac{6}{5} \text{ or } 1.2$$

**35.** 
$$x = 0$$

- **36.** In class.
- **37.** In class.
- **38.** In class.

# Section 2-4 Applications: Substitution and Percents

### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

	GOAL: Get x alone (x will represent any variable)
	1. SIMPLIFY
2.3	A) Distribute Across ()
2.5	B) Get rid of fractions (multiply all by LCD)
2.3	C) Combine "Like terms" and get all x's on the same side
2.1	2. ADDITION PRINCIPLE
2.1	3. MULTIPLICATION PRINCIPLE
2.2	Applications: Shapes, Formulas, Solving for a Variable
2.4	Applications: Substitution and Percents
2.6	Inequalities
2.7	Inequalities and Applications

# D.U.P.E. Process for word problems with substitution

Main Topics	Examples		
D. U. P. E.	<ul> <li>Data – Find the information (numbers, formulas, relationships, etc.).</li> <li>Unknown - What value are you finding? Assign it a variable.</li> <li>Plan – Think: "How can I use the data to make an equation?"</li> <li>Equation – Make an equation from your plan. Then solve it!</li> </ul>		
Steps	<b>Example 1:</b> Two numbers add to 15, and the second is 7 bigger than the		
	first. What are the two numbers?		
<ol> <li>D -What numbers are important?</li> <li>U- What variables will we use?</li> </ol>	f + s = 151. The two numbers both add to 15, and one is 7 bigger than the other $s = f + 7$ 2. $f$ will represent the first number and $s$ will represent the second number		
3. P- Substitute.	f + s = 15 3. Substitute $f + 7$ in for $s$		
4. E - Write the equation to solve.	f+f+7=15 4. Write the equation to solve		
	f + f + 7 = 15 2f + 7 = 15 Solve for $f2f = 8f = 4$		
	Now that you know the first number $f$ , you s = f + 7 can find the second number $s$ using the s = 4 + 7 equations you wrote at the very beginning. s = 11		
	Answer: 4 and 11		

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		<b>Example 2:</b> A man cuts a 65-inch board so that one piece is four times bigger than the other. What are the lengths of the two pieces?
Ste	eps	1. They equal 65 inches total, and one is 4 times the
1.	D -What numbers are important?	x + y = 65other $y = 4x$ 2.x will represent the one piece, and y will represent the other piece
2.	U- What variables will we use?	x + y = 65 3. Substitute 4x in for y y = 4x
3.	P- Substitute.	x + 4x = 65 4. Write the equation to solve
4. E - Write the equation to solve. x + 4x = 65 $5x = 65$ Solve the equation $x = 13$		
		x + y = 65 Now that you know how long one piece x is,
		13 + y = 65 you can solve for the other piece y by using the
		y = 52 equations you wrote at the very beginning.
		Answer: 13 inches & 52 inches
		perimeter is 58 mm, what are the dimensions of the rectangle? 1. $l$ will represent the length, and $w$ will 2w + 2l = 58 represent the width l = 3w + 5 2. 58 millimeters total, and the length is 3 times the width plus 5
		2w + 2l = 58 l = 3w + 5 3. Substitute $3w + 5$ in for $l$
		2w+2(3w+5)=58 4. Write the equation to solve
		2w+6w+10 = 58 8w + 10 = 58 Solve the equation 8w = 48 w = 6
		2w + 2l = 582(6) + 2l = 5812 + 2l = 58Solve for the other variable2l = 46l = 23
		Answer: width is 6 mm, length is 23 mm

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	<b>Example 4:</b> I have created a triangular garden such that the largest side is			
Steps	8m less than twice the smallest side, and the medium side is 12m longer			
	than the smallest side. If the total perimeter of the garden is 104m, what are			
1. D - What numbers are	the lengths of the three sides?			
important?	s + m + l = 104 1. 104m total			
important:	l = 2s - 8 2. <i>l</i> for largest, <i>m</i> for medium, and			
	m = s + 12 s for smallest			
2.U- What variables will	s + m + l = 104			
we use?	m = (3 + 12) 3. Substitute the values for <i>l</i> and <i>m</i>			
we use?	l = 2s - 8/			
3.P- Substitute.				
5.P- Substitute.	s + (s + 12) + (2s - 8) = 104 4. Write the equation to solve			
	s+(s+12)+(2s-8) = 104			
	4s + 4 = 104 Solve the equation			
4.E - Write the equation to	4s = 100			
solve.	s = 25			
	m = s + 12			
	m = 25 + 12			
	m = 37			
	Plug in to find the other			
	l = 2s - 8 variables			
	l = 2(25) - 8			
	l = 50 - 8 l = 42			
	Answer: smallest is 25m, medium is 37m,			
	largest is 42m			
	<b>Example 5:</b> Three consecutive integers add to 39. What are they?			
	1. The three numbers add to 39. The word			
Steps	x + y + z = 39 <i>consecutive</i> tells us that each number is 1			
Steps	more than the one before it, which is			
1.D -What numbers are	y = x + 1 where the other two equations come from			
important?	2. $x$ is the first number, $y$ is the second, $z$ is			
important:	z = x + 2 the third			
2.U- What variables will	x + y + z = 39			
we use?	y = x + 1 3. Substitute the values for y and z			
	$z = (x+2)^{1/2}$			
3.P- Substitute.	x+(x+1)+(x+2)=39 4. Write the equation to solve			
J.1 - DUDSULUIC.	x + x + 1 + x + 2 = 39			
4.E - Write the equation to	3x + 3 = 39 Solve the equation			
-	3x = 36			
solve.	x = 12			
	Answer: 12, 13, & 14			

Steps	<b>Example 6:</b> Three con What are they?	secutive even integers add to 72.
1.D -What numbers are important?	x + y + z = 72	1. The three numbers add to 72. The words <i>consecutive even</i> tells us that each number is 2 more than the one before it, which is where
2.U- What variables will we use?	y = x + 2 $z = x + 4$	<ul><li>the other two equations come from</li><li><i>x</i> is the first number, <i>y</i> is the second, <i>z</i> is the third</li></ul>
3.P- Substitute.	x + y + z = 72 y = x + 2 z = x + 4	3. Substitute the values for $y$ and $z$
4.E - Write the equation to	x+(x+2)+(x+4)=72	4. Write the equation to solve
solve.	x + x + 2 + x + 4 = 72 3x + 6 = 72 3x = 66 x = 22	Solve the equation
	Answer: 22	, 24, 26

# Simple Percent Problems

Main Topics	Examples		
Remember this:	<b>Percent:</b> per = divide, cent = 10	<b>Percent:</b> per = divide, cent = 100	
"of" means "times". "what" means "x". "is" means "=".	$\begin{array}{ll} 0.73 = 73\% & 0.2 = 20\% \\ 2.3 = 230\% & 2.14 = 214\% \end{array}$	1 = 100%	
	<b>Example 7:</b> What is 26% of \$40	)?	
	$x = .26 \cdot 40$ and "	p an equation. Remember tt" means "x", "is" means "=" 'of" means times the equation	
	<b>Example 8:</b> 118.08 is what percent of 246?		
	118.08 is what percent of 246	Set up an equation.	
		Remember "what" means "x",	
	$118.08 = x \cdot \overline{2}46$	"is" means "=" and "of" means times	
	$118.08 = x \cdot 246$	Solve the equation	
	$\begin{array}{r} \div 246 \qquad \div 246 \\ .48 = x \end{array}$		
	x = .48	Turn the answer into a percent by moving the decimal two places to the right	
	Answe	er: 48%	

<b>Example 9:</b> 136 is 16% of w	<b>Example 9:</b> 136 is 16% of what?	
136 is 16% of what	Set up an equation.	
	Remember "what" means	
$136 = .16 \cdot x$	"x", "is" means "=" and "of"	
	means times	
$136 = .\lambda 6 \cdot x$	Solve the equation	
$136 = .16 \cdot x$ ÷ .16 ÷ .16		
850 = x		
Ans	wer: 850	

## **Forward Percent Problems**

Main Topics	Examples			
	<b>Example 10:</b> If you want to buy a \$759 computer with 8% sales tax,			
	how much tax will you end up paying?			
	r = 8%	6 D -	- Data	
	P = \$75	59		
	T = ?		- Unknown	
	T = rF		Plan	
			Equation	
	T = 60.7	72 Sol	ve as before	
	Answer: Y	You would pay \$	60.72 in sales tax	
	Example 11: How	much will Alice	save on a pair of sho	bes that are worth
	\$92 but are on sale	for 20% off?		
	r = 20% D – Data			
	P = \$92	2		
	D =?		Unknown	
	D = rP P - Plan D = (.20)(92) E - Equation			
	D = 18.4		ve as before	
	Answer: Alice will save \$18.40			
	<b>Example 12:</b> The original price of a TV was \$75, and it has a 6% sales			has a 6% sales
	tax. What is the final price of the TV?			
	P = 75 D – Data Or in other words:			a wondo.
	r = .06			
	F = ?	U – Unknown	75 + 0.06(75)	Add the
	F = P + rP			amount of tax
	75 + .06(75)		75+4.5	to the original
	75 + 4.5	Solve as	79.5	price
	79.5	before		Solve
	Answer: The fina	l price is \$79.50		

### **Backward Percent Problems**

Main Topics	Examples		
	<b>Example 13:</b> Henry purchased a picture frame. After a 15% discount its		
Percent Change Formula	cost was \$30.60. What was the original price?		
$P \pm rP = F$	P15P = 30.60	r = .15 P is what we don't know F=30.60	
or		1-50.00	
	P15P = 30.60	Solve the equation for P	
$P(1\pm r)=F$	.85P = 30.60	Combine like terms	
<i>P</i> = Principal (original) amount			
r = rate (percent as a decimal) F = (Final amount) $\pm$ means that you use + for	.85P = 30.60 $\div .85 \div .85$	Divide both sides by .85	
percent <u>increases</u> and – for percent <u>decreases</u> .	<i>x</i> = 36		
	Answer: Original cost was \$36.		
	<b>Example 14:</b> How many people lived in a town last year if 19,980 people live there this year and it grew 8% from last year?		
	x + .08x = 19,980	Add the amount of growth to last year's population (x) and set it equal to this	
	x + .08x = 19,980	year's population Solve the equation for x	
	108x = 19,980 $\div 1.08 \div 1.08$		
	<i>x</i> = 18,500		
	Answer: Last yea	ar the town's population was 18,500	

# **Reverse Averages**

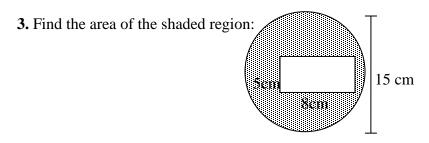
Main Topics	Examples		
Average: Add up then divide by number of entries.	<b>Example 15:</b> Mindy has earned 79, 85, 92, and 88 on her first four tests. What will she need to get on her 5 <sup>th</sup> test in order to have an average of 87?		
	79, 85, 92, 88	Write down what information we have been given—scores of her first four tests.	
	<i>T</i> =?	Pick a variable for the score on the 5 <sup>th</sup> test.	
	$\frac{79 + 85 + 92 + 88 + T}{5} = 87$	Plug all the information that we already know.	
	$\frac{344+T}{5} = 87$	Simplify	
	$5 \cdot \frac{344 + T}{5} = 87 \cdot 5$	Multiply both sides by 5 to clear out the division.	
	344 + T = 435		
	T = 91		
	Answer: Mindy needs a	score of 91 to get an average of 87.	

### **Section 2-4 Exercises**

2-2

1. 45 is 12 more than 3 times a number. What is the number?

2. 25 less than 7 times a number is 108. What is the number?



- 4. If a parallelogram has an area of 258.9  $\text{cm}^2$  and a base of 23.2 cm, how tall is it?
- **5.** Find the missing variable for a trapezoid:

```
A = 68 \text{ ft}^2b =h = 4 \text{ft}B = 21 \text{ft}
```

```
2-3 Solve.
```

6. 7p + 13 = 33 - 4p 7. 5n + 48 = 7n - 2(n - 2) 8. 5x - 10 = 7(x - 2)

- 9. 3x 7 = 12x 10. 5x 7(x + 3) = -2x 21 11. .06x = 15 .18x
- **12.** .8(7m-2) = 9.5m+1 **13.** .2q-7+2q = 3q-5 **14.** 12t = 45 + .4t
- **15.** 6(x-5) x = 5x 20 **16.** 9x 2(x-3) = 15x + 7 **17.** 5x 13x + x = 7x + 8x

2-4

**18.** Two numbers add to 251 and the second is 41 bigger than the first. What are the two numbers?

19. Jack earned 68, 75, and 82 on his first three tests. What does he need on his 4<sup>th</sup> test to average 79?

**20.** I have created a triangular garden such that the largest side is 8m less than twice the smallest and the medium side is 12m larger than the smallest side. If the total perimeter of the garden is 108m, what are the lengths of the three sides?

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**21.** If a rectangle's length is 5 more than 3 times the width and the perimeter is 58 mm what are the dimensions of the rectangle?

22. Two consecutive integers add to 123, what are they?

23. Three consecutive odd integers add to 93. What are they?

**24.** Cindy has 7 quiz scores of 87, 76, 88, 92, 93, 88, and 85. What does she need to get on her 8<sup>th</sup> quiz to get an average of 88?

- **25.** 18 is what percent of 58? **26.** What is 87% of 54?
- **27.** 34 is 56% of what? **28.** 119 is 8% of what?
- **29.** 23 is what percent of 74?
- **30.** Original Price: \$92.56**31.** Original Price:Tax: 7.3%Discount: 40%Final Price:Final Price: \$43.90
- **32.** Original Price:**33.** Original Price: \$58.50Tax: 5%Discount: 30%Final Price: \$237.50Final Price:

**34.** If the population of a town grew 21% up to 15,049 people, what was the population last year?

35. If the price of an object dropped 25% down to \$101.25, what was the original price?

### Preparation.

**36.** After reading some from Section 2.5, Try to solve this equation.  $\frac{x}{7} + \frac{13}{7} = \frac{15}{7} - \frac{2x}{7}$ 

**37.** Solve.

$$\frac{x}{3} + \frac{13}{3} = \frac{15}{3} - \frac{2x}{3}$$

### **Section 2-4 Answers**

1.	x = 11	30.	\$99.32
2.	x = 19	31.	\$73.17
3.	$136.71 \text{ cm}^2$	32.	\$226.19
4.	11.16 cm	33.	\$40.95
5.	13 ft = b	34.	12,437
6.	$p = \frac{20}{11}$	35.	\$135
7.	No solution	36.	In class
8.	x = 2	37.	In class
9.	$x = -\frac{7}{9}$		
10.	All numbers		
11.	x = 62.5		

- 11. x = 62.512.  $m = -\frac{2}{3}$ 13. q = -2.514. t = 3.879
- t = 5.077
- **15.** No solution
- 16.  $x = -\frac{1}{8}$
- 17. x = 0
- **18.** 105, 146
- **19.** 91
- **20.** 26m, 38m, 44m
- **21.** w = 6mm, l = 23mm
- **22.** 61 & 62
- **23.** 29, 31, & 33
- **24.** 95
- **25.** 31%
- **26.** 46.98
- **27.** 60.7
- **28.** 1487.5
- **29.** 31%

# 96 Section 2-5 The 3-Step Process to Solving

### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

	GOAL: Get x alone (x will represent any variable)
	1. SIMPLIFY
2.3	A) Distribute Across ()
2.5	B) Get rid of fractions (multiply all by LCD)
2.3	C) Combine "Like terms" and get all x's on the same side
2.1	2. ADDITION PRINCIPLE
2.1	3. MULTIPLICATION PRINCIPLE
2.2	Applications: Shapes, Formulas, Solving for a Variable
2.4	Applications: Substitution and Percents
2.6	Inequalities
2.7	Inequalities and Applications

### STEP 1—Simplify the Equation: Fractions, Parentheses, Like Terms

Main Topic	Examples
Getting Rid of Fractions	<b>Example 1:</b> Solve $\frac{5}{6}x + \frac{1}{4} = \frac{11}{3}$
1) Determine the LCD.	$\frac{5}{6}x + \frac{1}{4} = \frac{11}{3}$ First find the LCD.
2) Multiply everything by the LCD to remove fractions.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
	$12 \cdot \frac{5}{6}x + \frac{1}{4} \cdot 12 = \frac{11}{3} \cdot 12$ Multiply everything by 12.
	Simplify.
	10x + 3 = 44 Subtract 3 from both sides -3 - 3
	10x = 41 /10 /10 Divide by 10.
	$x = \frac{41}{10}$
	Answer: $x = \frac{41}{10}$

GOAL: Get x alone (x will represent any variable)	<b>Example 2:</b> Solve $\frac{2}{7} - \frac{3}{4}x = \frac{1}{2}$
<ol> <li>SIMPLIFY         <ul> <li>A) Distribute Across ()</li> <li>B) Get rid of fractions (multiply all by LCD)</li> </ul> </li> </ol>	742Find the LCD by making a factor $ $ $\land$ $ $ tree of the denominators.72222 × 2 × 7 = 2828
<ul><li>C) Combine "Like terms" and get all x's on the same side</li></ul>	$\frac{2}{7} \times 28 - \frac{3}{4}x \times 28 = \frac{1}{2} \times 28$ $\frac{1}{2} \times 28$ $\frac{1}{2} \times 28 = \frac{1}{2} \times 28$ $\frac{1}{2} \times 28$ $1$
<ol> <li>ADDITION PRINCIPLE</li> <li>MULTIPLICATION</li> </ol>	8 - 21x = 14 -8 - 8 Subtract 8 from both sides.
PRINCIPLE	-21x = 6 $/-21 / -21$ Divide both sides by -21
	$x = -\frac{6}{21}$
	$x = -\frac{2}{7}$ Simplify
	Answer: $x = -\frac{2}{7}$
	<b>Example 3:</b> Solve $\frac{2}{3}x - 2 = \frac{1}{2}$
	$\frac{2}{3}x \times 6 - 2 \times 6 = \frac{1}{2} \times 6$ Multiply every by LCD of 6.
	4x - 12 = 3 $+12 + 12$ Shazaam! No fractions. Add 12 to both sides.
	4x = 15 Divide both sides 4. 4x = 15
	$x = \frac{15}{4}$ Answer: $x = \frac{15}{4}$
	4

90	3 2	3
GOAL: Get x alone (x will	<b>Example 4:</b> Solve $\frac{3}{10}x - \frac{2}{5}(x + \frac{3}{5})$	$(-3) = \frac{3}{2}x + 3$
represent any variable) 1. SIMPLIFY A) Get rid of fractions	$\frac{3}{10}x - \frac{2}{5}(x-3) = \frac{3}{2}x + 3$	Distribute across parentheses.
<ul><li>(multiply all by LCD)</li><li>B) Distribute Across ()</li><li>C) Combine "Like terms"</li></ul>	$\begin{array}{c} (10) & (10) & (10) & (10) & (10) \\ \frac{3}{10}x - \frac{2}{5}x + \frac{6}{5} = \frac{3}{2}x + 3 \end{array}$	Multiply every by LCD of 10.
and get all x's on the same side	3x - 4x + 12 = 15x + 30	Simplify. No fractions 😊.
	-x + 12 = 15x + 30	Combine like terms on both sides.
	+x + x	Add x to get the x-s on one side.
2. ADDITION PRINCIPLE	$12 = 16x + 30 \\ -30 - 30$	Subtract 30 from both sides.
3. MULTIPLICATION PRINCIPLE	-18 = 16x      /16 /16	Divide both sides by 16.
	$x = -\frac{9}{8}$	
	Answer: $x = -\frac{9}{2}$	
	<b>Example 5:</b> Solve $\frac{2x-5}{3} = \frac{4}{3}$	$\frac{x-1}{2}$
	$\frac{2x}{3} - \frac{5}{3} = \frac{4x}{2} - \frac{1}{2}$	Grouping over a fraction acts as a parentheses. Break up into individual fractions.
		Same as distributing.
	$\frac{\binom{6}{2x}}{3} - \frac{\binom{6}{5}}{3} = \frac{\binom{6}{2}}{2} - \frac{\binom{6}{1}}{2}$	Multiply every by LCD of 6.
	4x - 10 = 12x - 3	Simplify. No fractions 😊.
	4x - 10 = 12x - 3 $-4x - 4x$	Combine like terms on both sides. Subtract 4x to get the x-s on one side.
	$ \begin{array}{r} -10 = 8x - 3 \\ +3 + 3 \end{array} $	Add 3 to both sides.
	$-7 = 8x$ $-\frac{7}{8} = x$	Divide both sides by 8.
	Answer: $x = -\frac{7}{8}$	
	<u> </u>	

### **Section 2-5 Exercises**

2 - 2

**1.** 35 less than 7 times a number is 98. What is the number?

**2.** The perimeter of a rectangle is 702 cm. The length is 71 cm longer than the width. What are the dimensions?

2-3Solve.3. 7p + 12 = 33 - 4p4. 3n + 48 = 7 - 2(n - 2)5. 5x - 10 = 5(x - 2)6. 3x - 7 = 15x7. 5x - 7(x + 3) = -2x + 128. .09x = 13 - .18x9. .8(3x - 2) = 9.5x + 110. .2x - 7 + 2x = 3x - 511. 12m = 70 + .4m12. 5(x - 5) - x = 4x - 2013. 9x - 4(x - 3) = 15x + 714. 8x - 12x + x = 9x + 8x

**2-4 15.** I have three colors of paint: blue, green, and yellow. The number of gallons of blue paint is 5 more than twice the number of green. The number of gallons of yellow paint is 3 less than 7 times the number of green. All together I have 82 gallons of paint. How many of each color are there?

16.	85 is what percent of 39?	17.	85 is 54% of what?
18.	What is 19% of 2,340?	19.	What is 23% of 79?
20.	119 is 18% of what?	21.	43 is what percent of 174?
22.	Original Price:\$72.56 Tax: 7.3% Final Price:	23.	Original Price: Discount: 30% Final Price: \$49.70
24.	Original Price: Tax: 5% Final Price: \$339.50	25.	Original Price: \$55.50 Discount: 40% Final Price:

26. If the population of a town grew 31% up to 17,049. What was the population last year?

27. If the price of an object dropped 35% down to \$101.25, what was the original price?

### 100 **Solve.**

2-5 28.  $\frac{4}{5}x = 2x - \frac{5}{3}$ 29.  $\frac{2}{3}x - 6 = 3 + \frac{1}{2}x$ 30\*. 7/3t - 5 = 1931.  $-\frac{3}{8}(x - 7) = 5 + 3x$ 32.  $\frac{3}{5}x - \frac{2}{5}(x - 3) = \frac{1}{5}x + 3$ 33.  $\frac{3x + 2}{7} = \frac{4x - 1}{5}$ 34. .9(-4x - 5) = 2.5x + 635. .0005x + .0045 = .004x36.  $\frac{x + 7}{4} = 8 - \frac{5}{6}x$ 

### Preparation.

**37.** Solve.  
a. 
$$3x - 7 = 17$$
 b.  $3x - 7 < 17$  c.  $3x - 7 > 17$ 

\*Remember that the "/" means the same as the  $\div$  symbol.

### Section 2-5 Answers

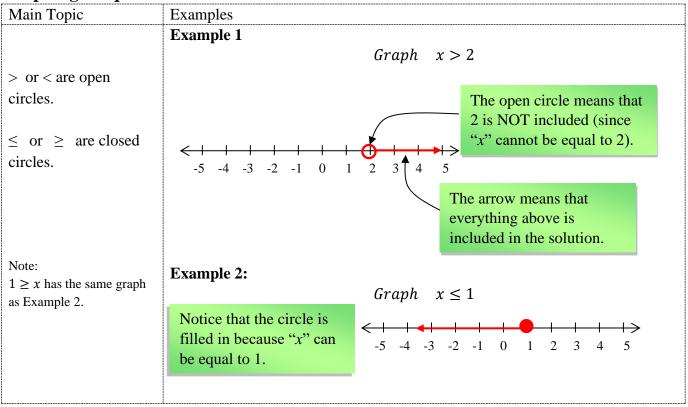
1.	19	28.	$x = \frac{25}{18}$
2.	w = 140cm, $l = 211$ cm	29.	<i>x</i> = 54
3.	$p = \frac{21}{11}$	30.	$t = \frac{72}{7}$
4.	$n = -\frac{37}{5}$ or -7.4	31.	$x = -\frac{19}{27}$
5.	All numbers	32.	No solution
6.	$x = -\frac{7}{12}$	33.	$x = \frac{17}{13}$
7.	no solution	34.	$x = -\frac{105}{61}$
8.	<i>x</i> = 48.15	35.	$x=rac{9}{7}$
9.	<i>x</i> =366	36.	$x = \frac{75}{13}$
10.	x = -2.5	37.	In class.
11.	m = 6.03		
12.	no solution		
13.	$x = \frac{1}{2}$		
14.	x = 0		
15.	21 gal – blue, 8gal – green, 53gal – yellow		
16.	218%		
17.	157.4		
18.	444.6		
19.	18.17		
20.	661.1		
21.	24.7%		
22.	\$77.86		
23.	\$71.00		
24.	\$323.33		
25.	\$33.30		
26.	13,015		
27.	\$155.77		

# 102 Section 2-6 Inequalities

ΈI	ER OVERVIEW ( <u>Video Instruction and Solutions Link</u> )		
		GOAL: Get x alone (x will represent any variable)	
		1. SIMPLIFY	
	2.3	A) Distribute Across ()	
	2.5	B) Get rid of fractions (multiply all by LCD)	
	2.3	C) Combine "Like terms" and get all x's on the same side	
	2.1	2. ADDITION PRINCIPLE	
	2.1	3. MULTIPLICATION PRINCIPLE	
	2.2	Applications: Shapes, Formulas, Solving for a Variable	
	2.4	Applications: Substitution and Percents	
	2.6	Inequalities	
[	2.7	Inequalities and Applications	

#### 1 41 CHAPT

### **Graphing Inequalities**



Examples	
<b>Example 3:</b> Solve and graph 5.	$x - 18 \ge -28$
$5x - 18 \ge -28$	No parentheses, no fractions, only one term with x.
+18 +18	Add 18 to both sides.
$5x \ge -10$ $5x \ge -10$ /5  /5	Divide to get x all alone.
$x \ge -2$	Graph the solution.
< + + + + ← -5 -4 -3 -2	-1 0 1 2 3 4 5
<b>Example 4:</b> Solve and graph 4.	$x + 2 - 5x \ge 10$
$4x + 2 - 5x \ge 10$ $2 - x \ge 10$ $2 - x \ge 10$ $-2 - 2$ $-x \ge 8$ $-x \ge 8$ $\div (-1) \div (-1)$ $x \le -8$ $(-1) - 2 - 8$	
	Example 3: Solve and graph 5. $5x - 18 \ge -28$ $5x - 18 \ge -28$ +18 + 18 $5x \ge -10$ $5x \ge -10$ $5x \ge -10$ 75 /5 $x \ge -2$ < + + + + = -5 Example 4: Solve and graph 4. $4x + 2 - 5x \ge 10$ $2 - x \ge 10$ $2 - x \ge 10$ $2 - x \ge 10$ -2 $-2-x \ge 8-x \ge 8-x \ge 8+ (-1) \div (-1)x \le -8$

Example 5: Solve and graph 
$$2(3 + 4y) - 9 \ge 45$$
  
 $2(3 + 4y) - 9 \ge 45$   
 $6 + 8y - 9 \ge 45$   
 $6 + 8y - 9 \ge 45$   
 $8y - 3 \ge 45$   
 $9 - 10$   
Graph the answer.  
Example 6: Solve and graph  $\frac{3}{5}(x + 4) < \frac{7}{2}x + 1$   
 $\frac{3}{5}x + \frac{12}{5} < \frac{7}{2}x + 1$   
 $\frac{3}{5}x + \frac{12}{5} < \frac{7}{2}x + 1$   
 $\frac{6x + 24 < 35x + 10}{-6x - 6x}$   
 $6x + 24 < 35x + 10$   
 $-6x - 6x$   
 $24 < 29x + 10$   
 $-10$   
 $14 < 29x$   
 $/29$   
 $/29$   
Divide to get y all alone.  
 $\frac{14 < 29x}{/29}$   
 $/29$   
 $/29$   
Divide to get y all alone.  
 $\frac{14 < 29x}{-10}$   
 $14 < 29x$   
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### **Section 2-6 Exercises**

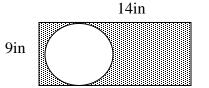
### Solve for the specified variable.

1. 
$$\frac{2s-at^2}{2t} = V$$
 for s  
3.  $d = \frac{LP}{F}$  for F  
4.  $\frac{9s-5g}{11} = c$  for s

5. 84 is 6 more than 3 times a number. What is the number?

**6.** A stick that is 438cm long is cut into two pieces. The first is 74 bigger than the second. What are the lengths of the two pieces?

7. Find the area of the shaded region:



**8.** If a rectangle's length is 7 more than 4 times the width and the perimeter is 194 mm, what are the dimensions of the rectangle?

**9.** Find the missing variable for a rectangle:

$$P = 48.3 \text{ ft}$$
  
w = 7.2 ft  
 $l =$ 

**10.** Find the missing variable for a circle:

**Final Price:** 

in

Solve.



- **11.** 7p + 12 = 13 7p **12.** 4n + 68 = 7 2(n 2) **13.** 7x 10 = 5(x 2)
- **14.** 9x 4 = 15x **15.** 8x 7(x + 3) = x 21 **16.** .18x = 13 .20x

Final Price: \$43.90



219 is 28% of what?
 27 is what percent of 74?
 Original Price: \$192.56
 Tax: 7.3%
 Original Price: Discount: 35%

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**21.** If the price of a meal after a 20% tip was \$28.80? What was the price of the meal before the tip was added?

22. If the price of an object dropped 15% down to \$59.50, what was the original price?

### Solve.

# 2-5 23. $\frac{7}{3}t - 2 = 19 + 5t$ 24. $-\frac{3}{4}(x - 4) = 5 + 2x$ 25. $\frac{1}{6}x - 4 = 3 + \frac{3}{10}x$ 26. $\frac{5}{2}(-4x - 2) = \frac{3}{4}x + 6$ 27. $\frac{x - 5}{3} = \frac{5x + 8}{6}$ 28. $\frac{x + 7}{14} = 6 - \frac{3}{7}x$

Solve and graph.

2-6	29.	3t + 5 > 12	30.	$4m+2 \leq -18$	31.	$3(x+4) - 6x \ge 5(x-2)$
	32.	-7p + 3 < 24	33.	$\frac{3}{5}(n+4) - 2 \ge \frac{3}{2}n$	34.	3m < -21
	35.	$\frac{3}{4}(x-5) \ge \frac{7}{2}x+1$	36.	$3a+5a \leq 7a-8a$	37.	$5y - 7 \ge \frac{2}{3}y + 4$

### Preparation.

### Solve the following.

**38.** At a family reunion, Logan reserves a table at a dinner and a show event. There is a \$50 reservation fee for the show, plus a fee of \$15 per person for the dinner. If he has a budget of \$450, how many people can come to the dinner?

**39.** On his first two tests, Josh received scores of 85 and 89. If he wants at least a 90 for the average of his first three tests, what possible scores could he get on his third test?

Section 2-6 Answers

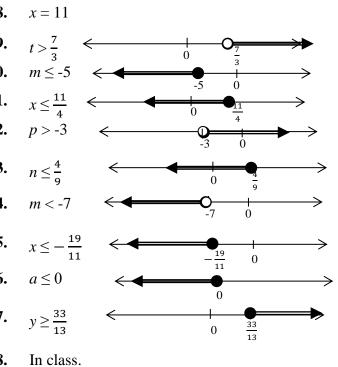
secu	11 2-0 Allswel 5		
1.	$S = \frac{2Vt + at^2}{2}$	28.	<i>x</i> =
2.	$p = \frac{l}{rt}^2$	29.	<i>t</i> >
3.	$F = \frac{LP}{d}$	30.	m
	$s = \frac{\frac{a}{11c+5g}}{9}$	31.	<i>x</i> ≤
5.	26	32.	<i>p</i> >
6.	182cm, 256cm	33.	n <u>&lt;</u>
7.	62.38 in <sup>2</sup>	34.	m
8.	18mm X 79mm	35.	<i>x</i> ≤
9.	l = 16.95 ft	36.	a <u>&lt;</u>
10.	127.3 in	37.	<i>y</i> ≥
11.	$p=rac{1}{14}$	38.	In
12.	n = -9.5	39.	In
13.	x = 0		
14.	$x = -\frac{2}{3}$		
15.	All numbers		
16.	<i>x</i> = 34.21		
17.	782.1		
18.	36.5%		
19.	\$206.62		
20.	\$67.54		
21.	\$24		
22.	\$70		

**23.** 
$$t = -\frac{63}{8}$$
 or -7.875  
**24.**  $x = -\frac{8}{11}$  or -0.73

**25.** 
$$x = -52.5$$

 $x = -\frac{44}{43}$  or -1.0226.

**27.** 
$$x = -6$$



class.

# <sup>108</sup> Section 2-7 Word Problems: Inequalities

### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

	GOAL: Get x alone (x will represent any variable)	
	1. SIMPLIFY	
2.5	A) Get rid of fractions (multiply all by LCD)	
2.3	B) Distribute Across ()	
2.3	C) Combine "Like terms" and get all x's on the same side	
2.1	2. ADDITION PRINCIPLE	
2.1	3. MULTIPLICATION PRINCIPLE	
2.2	Applications: Shapes, Formulas, Solving for a Variable	
2.4	Applications: Substitution and Percents	
2.6	Inequalities	
2.7	Inequalities and Applications	

### **INEQUALITY WORD PROBLEMS: TRANSLATION**

COMMON PHRASES EXAMPLE		TRANSLATION
at least / minimum	The minimum speed is 35 mph.	$S \ge 35$
at most	You can have at most 15 in the group.	$P \le 15$
cannot exceed / maximum	The weight cannot exceed 2000lbs.	$W \le 2000$
must exceed	The cost must exceed \$10	<i>C</i> > 10
less than	He has less than a 95%	<i>x</i> < 95%
more than	We have more than \$1000 in our account.	<i>M</i> > \$1000
between	His age is somewhere between 25 and 30 years old.	25 < <i>A</i> < 30
no more than	There can be no more than 10 people on the boat.	$P \le 10$
no less than	You should walk no less than 5 miles a day.	$d \ge 5$

Main Topics	Examples		
Power of "at least" 1horsepower. Power $\ge$ 10 horsepower	<b>Example 1:</b> In order for my model rocket to work it needs to put out a power of at least 10 horsepower		
	Determine the key phrase that will help us to figure out which inequality sign to use		
	Translate it into an inequality sign		
	Answer: Power $\geq$ 10 horsepower		

	<b>Example 2:</b> The required thickness of penny is between 1.8 and 2mm.
Thickness of penny is "between" 1.8 and 2mm. 1.8mm < T < 2mm	Determine the key phrase that will help us to figure out which inequality sign to use
Note that it could also be $1.8mm \le T \le 2mm$	Translate it into an inequality sign
	Answer: 1. 8mm < T < 2mm

Examples	
<b>Example 3:</b> Glen Road has a speed limit of 45mph.	
Determine the key phrase that will help us to figure out which inequality sign to use	
Translate it into an inequality sign	
Answer: speed ≤ 45mph	
<b>Example 4:</b> A box that weighs 5 lbs can hold up to 25 books that e	
The weight of the box (5lbs) plus 2.5 lbs for every book (x) can be at most 48 lbs. $5 + 2.5x \le 48$ $5 + 2.5x \le 48$	
$\frac{-5}{2.5x \le 43}$	
$\div 2.5 \div 2.5$ Can we have 17.2 books? No, so we need to change it to 17 $x \le 17$	
We also note that a negative number of books would make no sense, so we have to have at least 0. <b>Answer: <math>0 \le Books \le 17</math></b>	
	Example 3: Glen Road has a speed limit of 45mph.Determine the key phrase that will help us to figure out which inequality sign to useTranslate it into an inequality signAnswer: speed $\leq 45$ mphExample 4: A box that weighs 5 lbs can hold up to 25 books that e weighs 2.5 lbs. Due to recent back surgery I can only carry at most lbs. If I want to move the box, how many books can the box have iThe weight of the box (5lbs) plus 2.5 lbs for every book (x) can be at most 48 lbs.2.5x $\leq 48$ $-5$ 2.5x $\leq 48$ $-5$ 2.5x $\leq 48$ $-5$ Can we have 17.2 books? No, so we need to change it to 17 $x \leq 17$ We also note that a negative number of books would make no

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	<b>Example 5:</b> In order for David to reach his saving goal he needs to earn at least \$109,200 in commission this year. He earns 15% commission from all of his sales. If he has already earned \$89,700 in commission this year, how much more in sales does he need this year in order to reach his goal?
Set up an inequality with the information we are given.	David's sales amount last year (\$89,700) needs to increase by 15% of x to be at least \$109,200 $89,700 + .15x \ge 109,200$
Solve the inequality we just came up with	$89,700 + .15x \ge 109,200$ -89,700 - 89,700 .15x \ge 19,500 ÷ .15 ÷ .15
Check to see if the answer makes sense	$x \ge 130,000$ Can we have 130,000 dollars? Yes, our answer works $x \ge 130,000$ Answer: sales $\ge$ \$130,000
Note that solving these problems using equations and then adding the inequality sign when the answer is obtained is acceptable.	

Main Topics	Examples	
Set Notation		
	Inequality	Set Notation
{ } means "set of".	x > 5	$\{x   x > 5\}$
x   means "x such that".	$x \le -7$	$\{x   x \le -7\}$
$\{x \mid x > 5\}$ The set of all x such that x > 5.	$-2 < x \le \frac{7}{2}$	$\left\{ x \mid -2 < x \le \frac{7}{2} \right\}$

#### **Section 2-7 Exercises**

2-5

#### Translate the following statements into an equation and solve.

**4.** While studying the weather patterns in Omaha, Jackson recorded that between the months of March and May the average temperature highs rose by 25%. If the average temperature in May is 78°F, what was the average temperature in March?

**5.** While running her latest marathon, Erika lost 2% of her body weight in sweat. After drinking water after the race, she regained 90% of the weight that she lost. If she originally weighed 120 pounds, how much did she weigh after drinking?

#### Solve the following inequalities, and write the answer in set notation.

2-6	<b>6.</b> 14 <i>h</i> + (−7.2) < −220	<b>7.</b> $8k - \frac{3}{4} \ge 10k$	8.	$0.5(8r + 22) \le 2r + 11$
	9. $\frac{75}{3} > \frac{15b-30}{3}$	<b>10.</b> $12.7p + 4.5 + 1.3p \ge -31.9$		

#### Write the following statements as an inequality and graph.

7 <b>11.</b> It is at most $5^\circ$ outside.		<b>12.</b> The show will begin in less than 5 minutes.		
	<b>13.</b> 60 inches is the minimum height to enter.	<b>14.</b> The road is between 5 and 8 miles away.		
	<b>15.</b> The speed limit is 45 miles per hour.	<b>16.</b> I have more than 3 years until graduation.		

#### Solve the following word problems by writing them in an inequality.

**17.** On his first two tests, Josh received scores of 88 and 92. If he wants at least an average of 93, what does his score on the third test have to be?

**18.** An elevator can hold up to 3,300 pounds. If each person on the elevator weighs an average of 165 pounds, how many people can ride at one time? (When you state your answer, remember that we can't have a negative number of people.)

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**19.** At a family reunion, Logan reserved a table at a dinner and a show event. There was a \$50 reservation fee for the show, plus a fee of \$15 per person for the dinner. If he had a budget of \$450, how many people can come to the dinner? (When you state your answer, remember that we can't have a negative number of people.)

**20.** In order to qualify for financial aid, Sheyla needs to take at least 30 credits combined between two semesters. If she took 16 credits last semester, how many more credits does she need to take this semester to qualify for aid?

**21.** Patty wants to know how long she can talk to her grandma on a long-distance phone call with the \$2.20 she has. If it costs \$0.50 to place a call and \$0.10 per minute, how long can she talk?

**22.** The width of a rectangle is fixed at 6 meters. For what lengths will the area be more than  $96m^2$ ?

#### Section 2-7 Answers

- **1.** 12.5%
- **2.** 0.00018
- **3.** 400
- **4.** 62.4° F
- 5. 119.76 pounds
- 6.  $\{h|h < -15.2\}$
- 7.  $\{k | k \le -0.375\}$
- 8.  $\{r | r \le 0\}$
- 9.  $\{b | b < 7\}$
- **10.**  $\{p | p \ge -2.6\}$
- **11.** Temperature  $\leq 5^{\circ}$
- 12.  $0 \leq Show \ begins < 5 \ min.$
- 13.  $height \ge 60$  inches
- 14.  $5 mi \le road \le 8 mi$ or 5 mi < road < 8 mi or or 5 mi < road < 8 mi

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5

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Ô

60

- 15.  $0 < speed \le 45 mph$
- 16. years > 3 4
- **17.**  $grade \ge 99$
- 18.  $0 \le people \le 20$
- 19.  $0 \le people \le 26$  or  $0 \le P < 27$
- **20.**  $credits \geq 14$
- **21.**  $0 < time \le 17$  minutes
- **22.**length > 16 meters

## 114 Chapter 2 Review Exercises

**1.** Create a visual chart of all of the methods, formulas, and examples from studying how to solve these linear equations and inequalities.

#### Solve.

2 - 2

**2-1 2.** 
$$-\frac{2}{9}$$
 m = 24 **3.**  $9\left(\frac{8-6x}{4}+6\right)+5=-31$  **4.**  $\frac{8x-5}{3}=33$ 

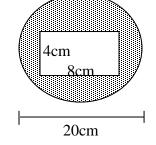
Solve for the specified variable.

**5.** 
$$Rd = pM(f + t)$$
 for t **6.**  $d = \frac{pM(f - t)}{R}$  for R

**7.** 13.2 less than 7 times a number is 18.8. What is the number?

8. Two numbers add to 336 and the first is 24 bigger than the second. What are the two numbers?

9. Find the area of the shaded region:



**10.** I have created a triangular garden such that the largest side is 6m less than twice the smallest and the medium side is 15m larger than the smallest side. If the total perimeter of the garden is 105m, what are the lengths of the three sides?

11. If a parallelogram has an area of 158.9  $cm^2$  and a base of 23.2 cm, how tall is it?

12. A triangle has angles of g - 3, 2g + 8, and 3g - 17. Solve for g and find the measures of the angles.

#### Solve.

**2-3 13.** 
$$7p + 12 = 12 + 7p$$
 **14.**  $9n + 48 = 7n - 2(n - 2)$  **15.**  $7x + 18 = 9(x - 3)$ 

**16.** Rick has taken 4 tests. His scores are 83, 92, 94, and 85. What does he need to get on his 5<sup>th</sup> test for his average to be 90?

17.	45 is what percent of 39?		
18.	25 is 44% of what?	19.	What is 59% of 2,340?
20.	Original Price: Tax: 5% Final Price: \$359.50	21.	Original Price: \$55.50 Discount: 20% Final Price:

22. If the population of a town grew 11% up to 17,046. What was the population last year?

23. If the price of an object dropped 15% down to \$62.90, what was the original price?

Solve.

**2-5 24.** 
$$\frac{7}{3}t - 8 = 4 + 7t$$
 **25.**  $-\frac{3}{7}(m - 12) = 3m + 6$  **26.**  $\frac{5}{6}x - 8 = 7 + \frac{7}{8}x$   
**27.**  $.13(-2x + 2) = .05x + 7$  **28.**  $\frac{x - 7}{4} = \frac{5x + 3}{10}$ 

Solve and graph.

 2-6
 29. 3t + 5 > 15 30.  $4m + 30 \le -18$  31.  $3(x + 2) - 6x \ge 5(x - 2)$  

 32. -7p + 3 < -10 33.  $\frac{3}{5}(n + 6) - 2 \ge \frac{3}{2}n$  34. 7m < -21 

 35.  $\frac{3}{4}(x - 5) \ge \frac{7}{2}x + 15$  36. 3a + 5a > 7a - 8a 37.  $5y - 15 \ge \frac{2}{3}y + 4$ 

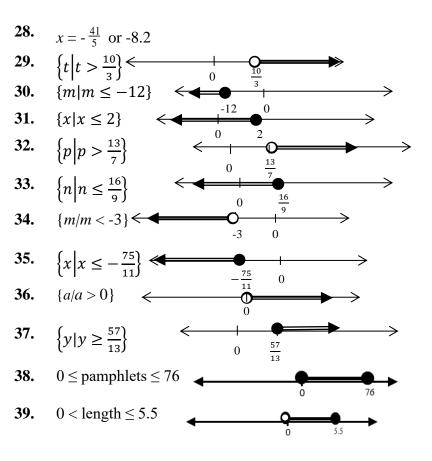
#### Solve. Write your answer as an inequality. Then graph the solution.

**38.** A copy job to run a pamphlet costs \$7 for a setup fee and then \$2.21 for each copy. How many copies can be run if the budget is \$175? (Include in the answer the idea that a negative number of copies cannot be made.)

**39.** An envelope has to have a maximum area of 18 in<sup>2</sup>. What can the length be if the width is  $3\frac{1}{4}$  in? (Include the idea that a length cannot be negative.)

#### **Chapter 2 Review Answers**

1.	It better be good.
2.	m = -108
3.	x = 8
4.	x = 13
5.	$t = \frac{Rd - pMf}{pM}$ or $t = \frac{Rd}{pM} - f$
6.	$R = \frac{pM(f-t)}{d}$ or $R = \frac{pMf-pMt}{d}$
	$\frac{32}{7}$ or 4.57
8.	156, 180
9.	282.16cm2
10.	24m, 39m, 42m
11.	6.85cm
12.	g = 32 angles are 29°, 72°, 79°
13.	All numbers
	All numbers $n = -11$
14.	
14.	n = -11 $x = \frac{45}{2}$ or 22.5
14. 15. 16.	n = -11 $x = \frac{45}{2}$ or 22.5
14. 15. 16. 17.	n = -11 $x = \frac{45}{2}$ or 22.5 96
14. 15. 16. 17.	n = -11 $x = \frac{45}{2}$ or 22.5 96 115.4%
14. 15. 16. 17. 18.	n = -11 $x = \frac{45}{2}$ or 22.5 96 115.4% 56.82
<ol> <li>14.</li> <li>15.</li> <li>16.</li> <li>17.</li> <li>18.</li> <li>19.</li> <li>20.</li> </ol>	n = -11 $x = \frac{45}{2} \text{ or } 22.5$ 96 115.4% 56.82 1380.6
<ol> <li>14.</li> <li>15.</li> <li>16.</li> <li>17.</li> <li>18.</li> <li>19.</li> <li>20.</li> <li>21.</li> </ol>	n = -11 $x = \frac{45}{2} \text{ or } 22.5$ 96 115.4% 56.82 1380.6 \$342.38
<ol> <li>14.</li> <li>15.</li> <li>16.</li> <li>17.</li> <li>18.</li> <li>19.</li> <li>20.</li> <li>21.</li> <li>22.</li> </ol>	n = -11 $x = \frac{45}{2} \text{ or } 22.5$ 96 115.4% 56.82 1380.6 \$342.38 \$44.40
<ol> <li>14.</li> <li>15.</li> <li>16.</li> <li>17.</li> <li>18.</li> <li>19.</li> <li>20.</li> <li>21.</li> <li>22.</li> </ol>	n = -11 $x = \frac{45}{2} \text{ or } 22.5$ 96 115.4% 56.82 1380.6 \$342.38 \$44.40 15,357
<ol> <li>14.</li> <li>15.</li> <li>16.</li> <li>17.</li> <li>18.</li> <li>19.</li> <li>20.</li> <li>21.</li> <li>22.</li> <li>23.</li> </ol>	n = -11 $x = \frac{45}{2} \text{ or } 22.5$ 96 115.4% 56.82 1380.6 \$342.38 \$44.40 15,357 \$74
<ol> <li>14.</li> <li>15.</li> <li>16.</li> <li>17.</li> <li>18.</li> <li>19.</li> <li>20.</li> <li>21.</li> <li>22.</li> <li>23.</li> <li>24.</li> <li>25.</li> </ol>	n = -11 $x = \frac{45}{2} \text{ or } 22.5$ 96 115.4% 56.82 1380.6 \$342.38 \$44.40 15,357 \$74 $t = -\frac{18}{7}$



# Section 3-1 Coordinates and Graphing Lines

3-1: Coordinates	Graphing Lines
3-2: Intercepts	Vertical and Horizontal Lines
3-3: Slope	
3-4: Graphing with slope	Equation shortcuts
3-5: Writing Equations of Lines	Prediction

## CHAPTER OVERVIEW (Video Instruction and Solutions Link)

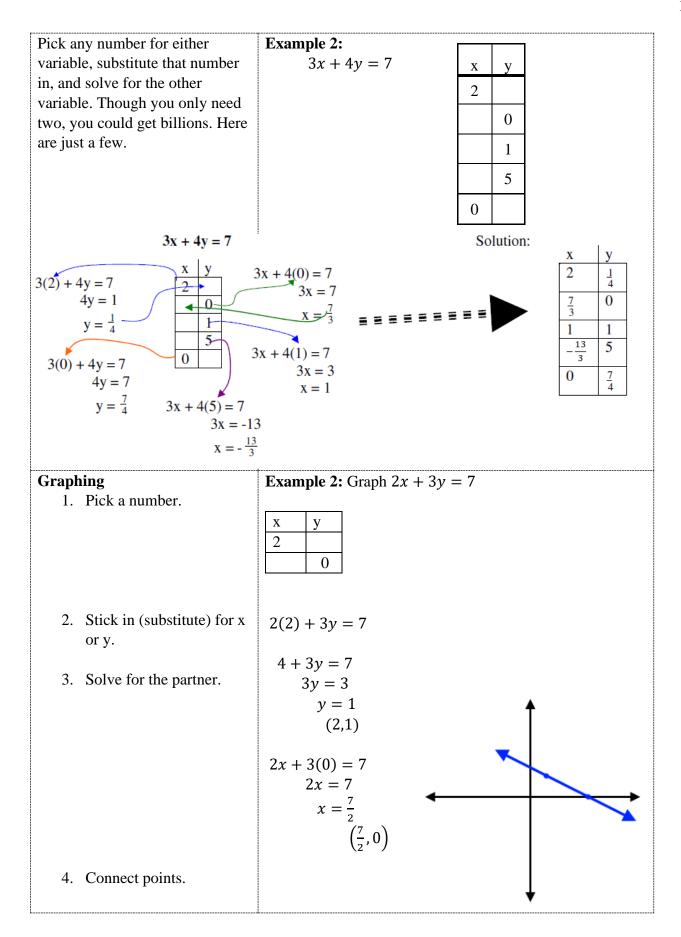
# Graphs

Main Topics	Examples	
Coordinate Axes	Alphabetical Ordinates	
	A, B, C, D, E	
Ordinates	Numerical Ordinates	
	1, 2, 3, 4, 5	
	A B C D E F G H I J	
	Battleship:	
Games	2 3	
	Coordinates C9, D9, E9, F9 4	
	indicate the placement of a ship. <sup>5</sup>	
	6 7 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8	
	8 8	
	Maps:	
	Kadesh-Barnea is found at C2 on	
	this LDS Study Helps	
	2. Israel's Exodus from Egypt and Entry into Canaan	
	KEY	
	Possible route of the Exodus	
	Great Sea Gaza CANAAN	
	Beersheba	
Maps	Nile Delta Widerress LEDOM	
	Rameses (Tanis) Wildemeer of C2 bares	
	GOSHEN Shur Mit Hor	
	EGYPT Witterness of the second s	
	On (Heliopolis) Pi-hahiroth? Widemess of Ezion-geber	
	Noph (Memphis) Sinai Peninsula	
	Guit of Suez Gilling	
	Guit of Suez Guit of Suez Minderness Strait	
	Rephidim? Guit of Agaba	
	Miles Kilometers (Noveb)	
	0 25 50 75 0 40 80 120 71kG 308	
	I	

In 1637, Rene Descartes published the idea of using pairs of numerical<br/>ordinates in equations with variables to describe geometric objects such<br/>as lines and circles.Cartesian CoordinatesThe first ordinate x and the second ordinate y give us (x, y). We now<br/>call this the Cartesian (named after Descartes) Coordinate System.(-3,1)(-3,1)(-3,1)(0,0)(-1,5)(-2,5)(-1,5)(-2,5)

## **Finding Points**

inung i onus		
Main Topics	Examples	
Two PointsOne point can have many lines going through it, but you find a $2^{nd}$ point, there is only one line.		
Pick 'n Stick	Example 1: Fill in the table for	
To organize the points we make,	$y = \frac{1}{4}x - 2 \qquad x \qquad y$	
we can outline the points on the	4	
graph by using a table.	0	
	0	
	3	
x y 4 -1	when $x = 4$ we have $y = \frac{1}{4}(4) - 2$ which means $y = -1$ . when $x = 0$ we have $y = \frac{1}{4}(0) - 2$ which means $y = -2$ . when $y = 0$ we have $0 = \frac{1}{4}(x) - 2$ which means $x = 8$ . when $y = 3$ we have $3 = \frac{1}{4}(x) - 2$ which means $x = 20$ . Now fill in the table with each value.	



Example 3: Graph $y = \frac{2}{3}x - 4$ $\boxed{x  y}$ 0 5 $y = \frac{2}{3}(0) - 4$ y = 0 - 4 y = -4 (0, -4) $y = \frac{2}{3}(5) - 4$

#### **Section 3-1 Exercises**

**1.** Three types of bears are in a national park. The number of grizzly bears is 4 more than twice the number of black bears, and the number of panda bears is50 more than the number of black bears. There are a total of 874 bears in the park. How many of each kind are there?

**2.** An international phone call costs  $35\phi$  to connect and  $12\phi$  for every minute of the call. How long can a person talk for \$3.60?

3. A 52m rope is cut so that one piece is 18m longer than the other. What are the lengths of the pieces?

4. Original Price:\$292.505. Original Price:Discount:20%Discount: 40%Final Price:Final Price: \$73.90

#### Solve and graph (on a number line).



3-1

2-4

**6.** 5(x-2) > 7x + 8

#### Fill out the table for each of the following:

<b>7.</b> $x + y = 9$	<b>8</b> . $2x - y = 5$	<b>9</b> . $5x + 4y = 9$	<b>10</b> . x–7y = 13
x y	x y	x y	x y
5	2	1	1
-4	0	0	3
3	-1	-3	2
0	0	0	0
7	4	5	-1

Graph the following lines, and label three points (your points may be different than mine).

**11.** 3x + y = 10**12.** y = 2x**13.** x - 4y = 7**14.** 2x + y = 3**15.**  $y = -\frac{3}{7}x + 4$ **16.** 6x - 5y = 12**17.**  $y = \frac{1}{2}x - 4$ **18.** 5x + 2y = 6

#### **Preparation.**

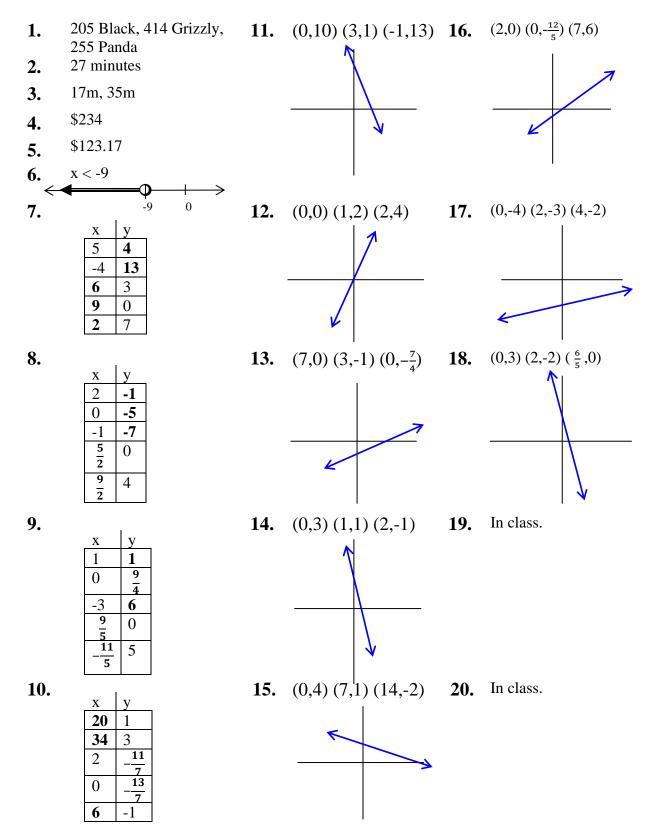
19. After reading a bit of section 3.2, try to find the x-intercept and y-intercept of  $y = \frac{2}{3}x + 5$ .

#### **20.** Solve for y in each of these equations:

a) 
$$2x + y = 7$$
 b)  $5x + 3y = 6$  c)  $2x - 7y = 11$ 

### Section 3-1 Answers

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Section 3-1

# Section 3-2 Intercepts, Vertical, Horizontal

3-1: Coordinates	Graphing Lines
3-2: Intercepts	Vertical and Horizontal Lines
3-3: Slope	Parallel and Perpendicular
3-4: Graphing with slope	Slope Intercept and equation shortcuts
3-5: Writing Equations of Lines	Prediction

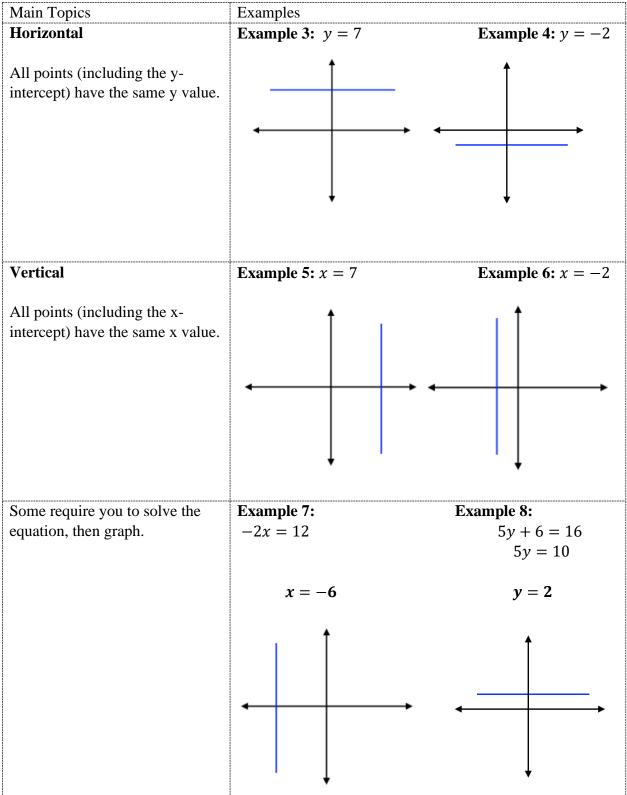
# CHAPTER OVERVIEW (Video Instruction and Solutions Link)

## Intercepts

Main Topics	Examples			
<b>Intercepts</b> x – intercept when y is 0. ( ,0)	<b>Example 1:</b> Find the x-intercept of $2x - 7y = 12$ Stick 0 in for y $2x - 7 \cdot 0 = 12$	<b>Example 2:</b> Find the y-intercept of $2x - 7y = 12$ Stick 0 in for x $2 \cdot 0 - 7y = 12$		
y – intercept when x is 0. (0, )	2x = 12 $x = 6$ The x-intercept is (6,0)	$-7y = 12$ $y = -\frac{12}{7}$ The y-intercept is $\left(0, -\frac{12}{7}\right)$		
Why do we call them intercepts? In math, the word "intercept" means "to cross". A point (0, ) is on the y-axis.	Example 3: Graph the following $y = \frac{2}{3}x - 5$ y-intercept: stick in 0 for x $y = \frac{2}{3}(0) - 5$ $= -5$ $(0, -5)$ $\frac{15}{2} = x  \left(\frac{15}{2}\right)$	5		

# Vertical and Horizontal Lines

124



#### **Section 3-2 Exercises**

**1.** Three types of trees are in a local park. The number of aspens is 5 more than three times the number of oaks, and the number of maples is 20 less than the number of oaks. There are a total of 850 trees in the park. How many of each kind are there?

2. Original Price:\$49.50 Discount:20% Final Price: **3.** Original Price: Discount: 40% Final Price: \$53.70

#### Solve and graph (on a number line).

2-6

**4.** 6(x-2) > 7x + 8

5. 2x + y = 9

#### Fill out the table for each of the following:

3-1

Х	У
5	
-4	
	3
	0
	7

6.	2x - 3y = 5	х	у
U.	2x - 3y - 3	2	
		0	
		-1	
			0
			4

Graph the following lines, and label three points (your points may be different than mine).

**7.**  $y = -\frac{3}{7}x + 4$  **8.** 6x - 5y = 12

Find the x and y intercepts for each line. Then graph.

3-2	9.	5x + 2y = 20	10.	y = 2x - 10	11.	4x - y = 8
	12.	x + y = 7	13.	$y = -\frac{3}{7}x - 6$	14.	2x - 6y = 18

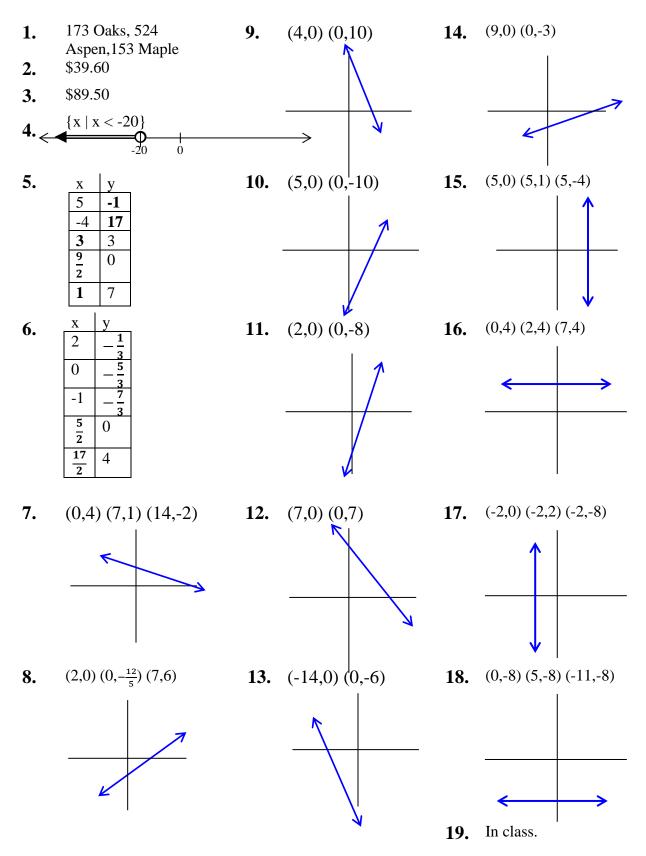
Graph the following lines, and label three points (your points may be different than mine).

**15.** 
$$x = 5$$
 **16.**  $y = 4$  **17.**  $3x = -6$  **18.**  $2y + 1 = -15$ 

#### **Preparation.**

**19.** After reading a bit of section 3-3, try to find the slope between (4,1) and (7,11).

#### 126 Section 3-2 Answers



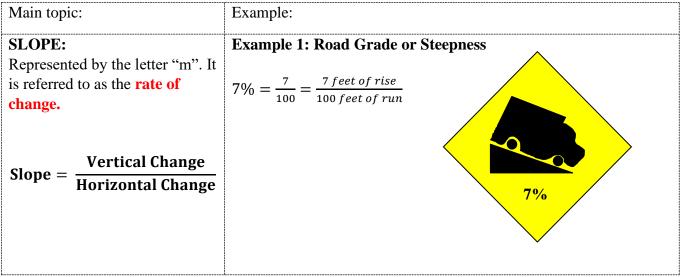
Section 3-2

# Section 3-3 Slope

3-1: Coordinates	Graphing Lines
3-2: Intercepts	Vertical and Horizontal Lines
3-3: Slope	Parallel and Perpendicular
3-4: Graphing with slope	Slope Intercept and equation shortcuts
3-5: Writing Equations of Lines	Prediction

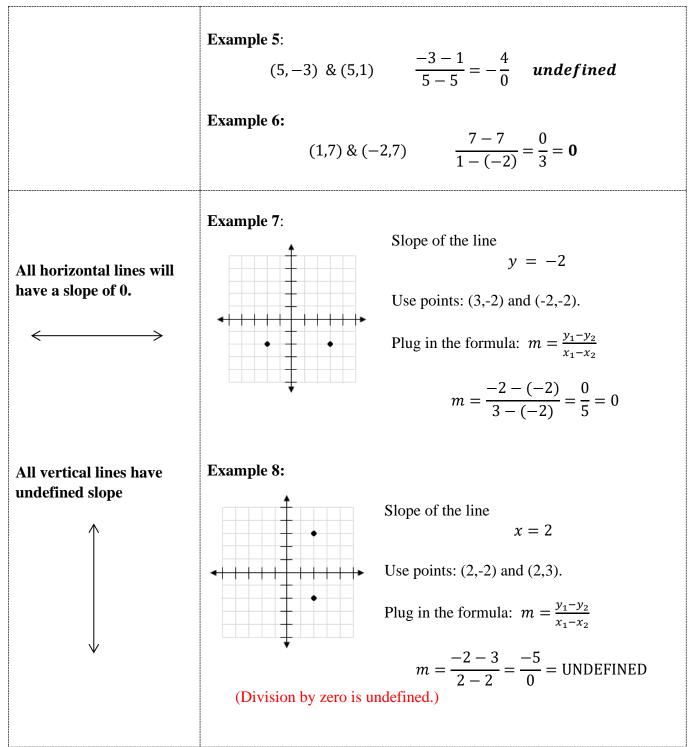
#### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

#### Definitions

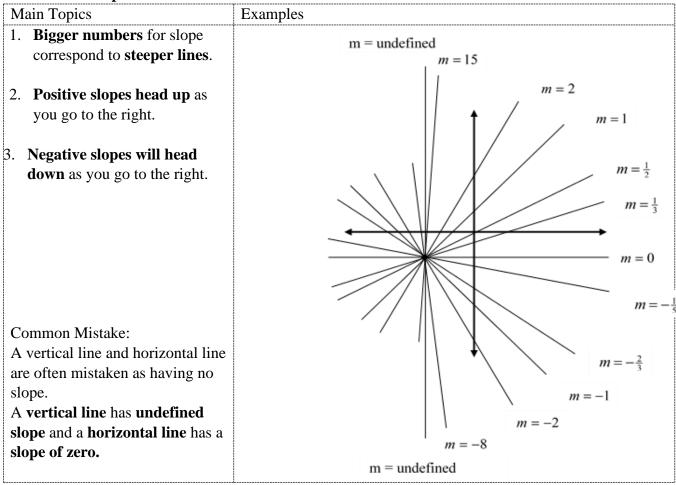


#### CALCULATING SLOPE

Main Topics	Examples				
Formula for slope:	Find the slope between each set of points:				
$m=\frac{y_1-y_2}{x_1-x_2}$	Example 2: (4,3) & (-2,1) $\frac{3-1}{4-(-2)} = \frac{2}{6} = \frac{1}{3}$				
	Example 3: (1,7) & (-2,1) $\frac{7-1}{1-(-2)} = 2$				
	Example 4: (5,-3) & (-2,1) $\frac{-3-1}{5-(-2)} = -\frac{4}{7}$				



#### **Trends with Slope**



#### **Special slope relationships**

Examples			
Example 9:			
Parallel Sl	ope: $\frac{3}{4} \rightarrow$ they have the		
<b>Example 10:</b> Slope: <i>m</i> = 1	Parallel Slope: 1	Perpendicular Slope: -1	
Slope: $m = \frac{5}{8}$	Parallel Slope: $\frac{5}{8}$	Perpendicular Slope: $-\frac{8}{5}$	
-	Parallel Slope: 0	Perpendicular Slope: undefined	
	<ul> <li>Example 9: Slope: m Parallel SI Perpendict</li> <li>Example 10: Slope: m = 1</li> <li>Example 11:</li> </ul>	Example 9: Slope: $m = \frac{3}{4}$ Parallel Slope: $\frac{3}{4} \rightarrow$ they have the Perpendicular Slope: $-\frac{4}{3} \rightarrow$ the set Example 10: Slope: $m = 1$ Parallel Slope: 1 Example 11: Slope: $m = \frac{5}{8}$ Parallel Slope: $\frac{5}{8}$ Example 12:	

#### **Section 3-3 Exercises**

2-4

**1. Solve for m:** -5x + 2m = 13

**2. Solve for y:** 3x - 11y = 5

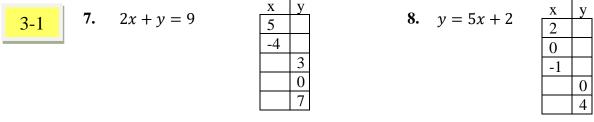
**3.** If grading in a class is set up so that 10% is attendance, 10% is tutoring, 30% homework, and 50% tests, what is a student's grade if he has 80% attendance, 50% tutoring, 50% homework and 80% on tests?

5.

4. Original Price:\$392.50 Discount:20% Final Price: Original Price: Discount: 45% Final Price: \$73.90

6. Four consecutive odd integers add up to 328. What are the four numbers?

#### Fill out the table for each of the following:



#### Find the x and y intercepts. Then graph.

	9.	3x + 2y = 10	10.	y = 2x - 7	11.	$y = \frac{1}{2}x$
3-2	12.	3x + 2y = 10 $4x + y = 8$	13.	$y = -\frac{3}{7}x - 9$	14.	2x - 5y = 12

Graph the following lines, and label three points (your points may be different than mine). 15. x = 4 16. y = 3

#### Find the slope between each pair of points.

2.2	<b>17.</b> (5, -2) (7,3)	<b>18.</b> (4,1) (-5,6)	<b>19.</b> (5, -1) (-3, -8)
3-3	<b>17.</b> $(5, -2)$ $(7,3)$ <b>20.</b> $(7,3)$ $(-2,3)$	<b>21.</b> (-5,2) (4,-3)	<b>22.</b> (-6,1) (-6,5)

**23.** A road rises 400 feet over a horizontal distance of 6,000 feet. What is the slope (or grade) of the road?

#### For each slope, write down the parallel and perpendicular slopes.

**24.** m = 4 **25.**  $m = -\frac{3}{8}$ 

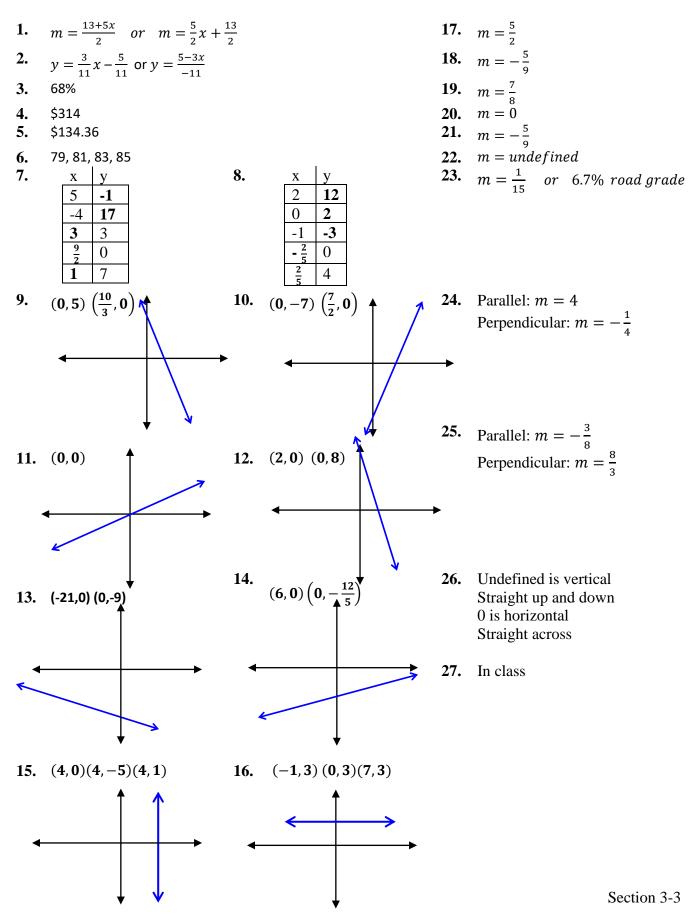
**26.** Explain the difference between a slope of zero and an undefined slope.

Preparation. 27. Find two points of each line and then use those points to find the slope.

$$y = \frac{7}{3}x - 8$$
  $y = \frac{3}{5}x + 4$ 

Section 3-3

#### Section 3-3 Answers



# 132Section 3-4 Slope-Intercept Form

<b>CHAPTER OVERVIEW</b>	(Video Instruction and Solutions Link)
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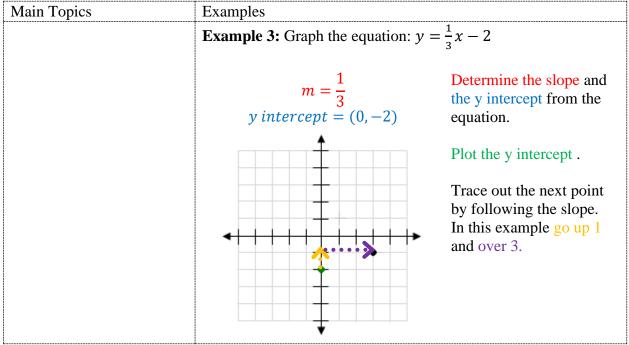
3-1: Coordinates	Graphing Lines
3-2: Intercepts	Vertical and Horizontal Lines
3-3: Slope	Parallel and Perpendicular
3-4: Graphing with slope	Slope Intercept and equation shortcuts
3-5: Writing Equations of Lines	Prediction

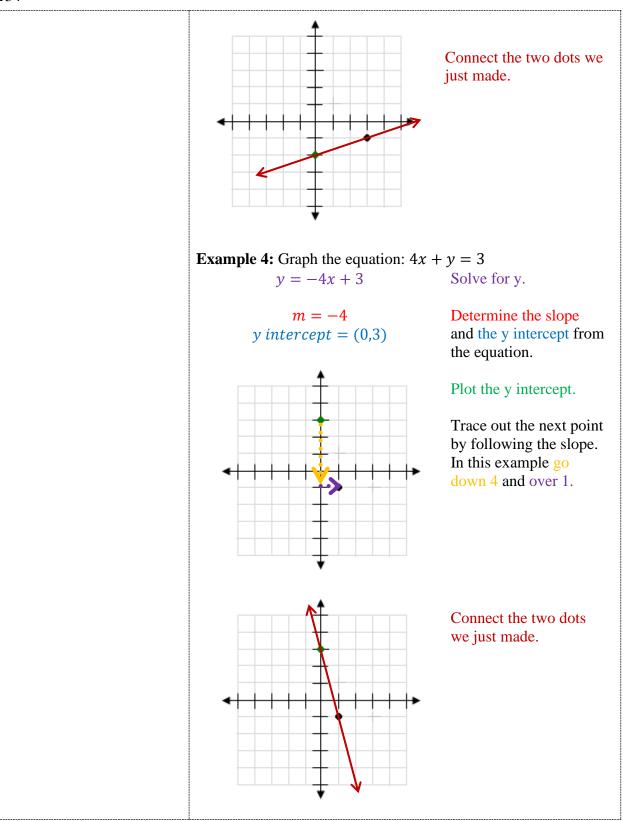
# Slope from Slope-Intercept Form

Main Topics	Examples		
Key Terms			
Slope	Slope $m = \frac{y_1 - y_2}{x_1 - x_2}$ $m = \frac{y \ change}{x \ change}$ $m = \frac{rise}{run}$ $m = \frac{\Delta y}{\Delta x}$		
Slope-intercept form	Slope-Intercept Form $y = mx + b$ . m is the slope b is the y-intercept		
Steps to convert into slope-intercept form:	<b>Example 1:</b> Convert this equation into slope-intercept form: 3x + 4y = 8		
<ol> <li>Get the y's alone on one side.</li> <li>Divide every term by the number attached to the y.</li> </ol>	$3x + 4y = 8$ $-3x - 3x$ $4y = -3x + 8$ $-3x + 4 + 4 + 4$ $y = -\frac{3}{4}x + 2$ $Answer: y = -\frac{3}{4}x + 2$ $Get the y's alone on one side.$ $Divide every term by the number attached to the y.$		

<b>Example 2:</b> Convert this equation into slope-intercept form: x - 2y = 3		
x - 2y = 3 $x - 2y = 3$ $-x - x$ $-2y = -x + 3$	Get the y's alone on one side.	
-2y = -x + 3 -2y = -x + 3 (÷ -2) (÷ -2)(÷ -2)	Divide every term by the number attached to the y.	
$y = \frac{1}{2}x - \frac{3}{2}$		
<b>Answer:</b> $y = \frac{1}{2}x - \frac{3}{2}$		

## Graphing with Slope and Y-intercept





#### **Section 3-4 Exercises**

**1.** Three types of horses are in a local ranch. The number of Arabians is 8 more than twice the number of quarter-horses, and the number of Clydsdales is 50 more than the number of Quarter-horses. There are a total of 282 horses at the ranch. How many of each kind are there?

2. What is the radius of a cone that has Lateral Surface Area of 197.92 in<sup>2</sup> and a slant height of 9 in?

**3.** Solve and graph the solution:  $3x - 1 > \frac{5}{2}x + 9$ 

- 4. Original Price:\$392.50 Tax: 6% Final Price:
- 5. Original Price: Tax: 7% Final Price: \$73.90

#### Fill out the table for each of the following: 6. 2x - 3y = 9



3-3

	•
Х	у
5	
-4	
	3
	0
	7

7.	$y = \frac{7}{2}x + 2$		
		Х	У
		2	
		0	
		-1	
			0
			4

Graph the following lines, and label x and y intercepts (need the same points as my answers).

3_2	8. $5x + 2y = 10$ 11. $x = 10$	<b>9</b> . $y = \frac{4}{7}x - 6$	<b>10</b> . $y = \frac{8}{3}x + 1$
5-2	<b>11</b> . $x = 10$	<b>12</b> . $y = -\frac{3}{7}x + 4$	<b>13</b> . $7x - y = 14$

#### Find the slope between each pair of points.

,	<b>14.</b> (8,-2) (7,3)	<b>15.</b> (8,1) (-5,6)	<b>16.</b> (-3,-1) (-3,-8)
)	<b>17.</b> (7,9) (-2,3)	<b>18.</b> (-5,6) (4,6)	

19. If a road rises 300 feet over a horizontal distance of 3600 feet, what is the road grade?

#### Find the slope and the y-intercept. Then graph the lines.

3-420. y = 6x + 1021. y = 4x + 322.  $y = \frac{1}{2}x - 4$ 23. x = -624.  $y = -\frac{3}{7}x - 2$ 25. 3x - 4y = 1226.  $y = -\frac{5}{3}x + \frac{10}{3}$ 27. x + 4y = -928. y = 7

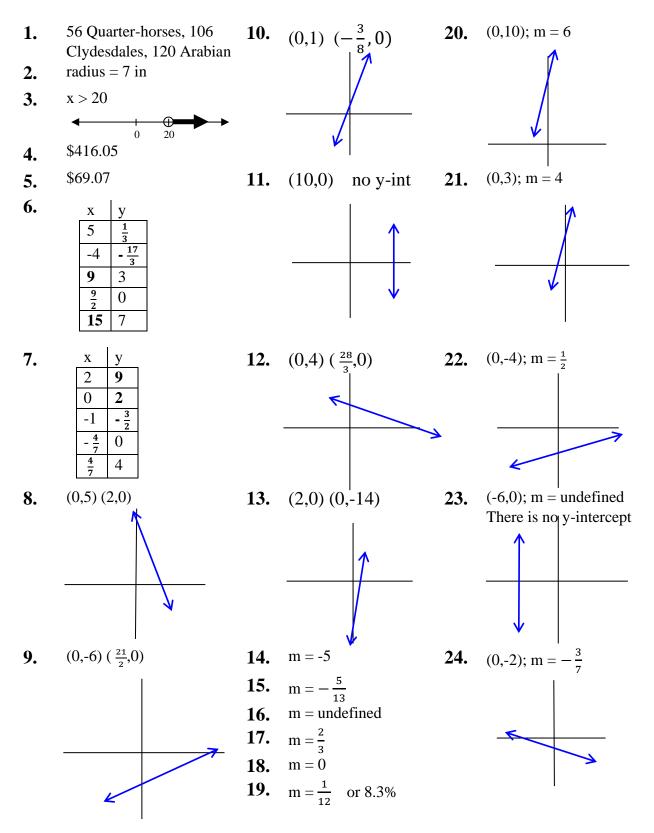
29. What is the slope of a line parallel to  $y = \frac{5}{3}x + 2$ ? 30. What is the slope of a line perpendicular to y = 5?

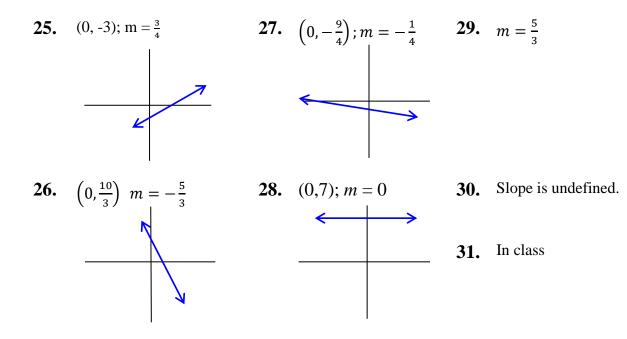
#### Preparation

**31.** Write the equations of three lines that have a slope of  $\frac{2}{7}$ .

## Section 3-4 Answers

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# <sup>138</sup>Section 3-5 Writing Equations

CHAPTER OVERVIEW (Video I	nstruction and Solutions Link)
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3-1: Coordinates	Graphing Lines
3-2: Intercepts	Vertical and Horizontal Lines
3-3: Slope	Parallel and Perpendicular
3-4: Graphing with slope	Slope Intercept and equation shortcuts
3-5: Writing Equations of Lines	Prediction

# Writing Equations

Main Topics	Examples		
Given slope and one point	<b>Example 1:</b> Write the equation of a line that goes through the point (-3, 4)		
Steps:	and has a slope of $-\frac{2}{3}$ .		
1. Write in slope-intercept form a. Fill in slope $(m)$ in $y = mx + b$ .	$y = mx + b$ $4 = \left(-\frac{2}{3}\right)(-3) + b$	Plug the point and the slope into equation.	
b. Fill in <i>x</i> and <i>y</i> using one point.	4 = 2 + b	Solve for b.	
<ul> <li>c. Solve for <i>b</i>.</li> <li>d. Re-write with only <i>x</i> and <i>y</i> as variables.</li> </ul>	b = 2 $y = -\frac{2}{3}x + 2$ <b>Answer:</b> $y = -\frac{2}{3}x + 2$	Write the final equation with slope and with y-intercept.	
Given two points			
Steps: 1. Use the points to find the	<b>Example 2:</b> Write the equation of a line that goes through the points: $(-2, -2)$ and $(8, 4)$ .		
<ul><li>slope.</li><li>Write in slope-intercept form</li><li>a. Fill in slope (<i>m</i>) in</li></ul>	$m = \frac{-2-4}{-2-8} = \frac{-6}{-10} = \frac{3}{5}$ $m = \frac{3}{5}$	Find slope. Remember: $m = \frac{y_1 - y_2}{x_1 - x_2}$	
y = mx + b. b. Fill in <i>x</i> and <i>y</i> using one point.	$y = mx + b$ $4 = \left(\frac{3}{5}\right)(8) + b$	Plug one of the points and the slope into equation.	
<ul> <li>c. Solve for <i>b</i>.</li> <li>d. Re-write with only <i>x</i> and <i>y</i> as variables.</li> </ul>	$4 = \frac{24}{5} + b$	Solve for b.	
	$b = -\frac{4}{5}$ $y = \frac{3}{5}x + \frac{-4}{5}$ Answer: $y = \frac{3}{5}x - \frac{4}{5}$	Write the final equation with slope and with y-intercept.	

Writing Equations of Horizontal Lines	<b>Example 3:</b> Write the equation of the line with slope, $m = 0$ (horizontal), that goes through the point (-3,5).	
Slick note: All horizontal lines have equations that look like	y = mx+b 5 = (0)(-3) + b	Plug one of the points and the slope into equation.
<i>y</i> =	5 = 0 + b	Solve for b.
And since the point in Example 3 has a y value of 5, the whole line must be $y = 5$	b = 5 $y = 0x + 5$ Answer: $y = 5$	Write the final equation with slope and with y-intercept.
Writing Equations of Vertical Lines	<b>Example 4:</b> Write the equation of the line with unthrough the point $(-3,5)$ . y = mx+b	ndefined slope (vertical), and goes Plug one of the points and the
Slick note: All vertical lines have equations that look like x =	5 = (undefined)(-3) + b We are stuck! And we cannot complete	slope into equation.
And since the point in Example 4 has an x value of $-3$ , the whole line must be $x = -3$		

# **Predict Values**

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Main Tonica	Examples		
Main Topics	Examples		
Steps:	<b>Example 5:</b> Two points on a line are $(0, 7)$ and $(6, 2)$ . Follow this same		
1. Use the points to	pattern and predict the y-value when $x=9$ .		
write the equation.	$m = \frac{7-2}{0-6} = -\frac{5}{6}$	Calculate the slope from the	
2. Plug in the new	<b>v v v</b>	two given points.	
value.		Remember: $m = \frac{y_1 - y_2}{x_1 - x_2}$	
	y = mx + b	Plug one of the points and the	
	$7 = \left(-\frac{5}{6}\right)(0) + b$	slope into equation.	
	7 = b	Solve for b.	
	$y = -\frac{5}{6}x + 7$	Write the final equation with	
	V	slope and with y-intercept.	
	$y = -\frac{5}{6}(9) + 7$ $y = -\frac{15}{2} + 7 = -\frac{1}{2}$		
		Plug in $x = 9$	
	$y = -\frac{10}{2} + 7 = -\frac{1}{2}$	1 lug lli x = )	
	Answer: $\left(9, -\frac{1}{2}\right)$		
	<b>Example 6:</b> The target heart rate of a person 20 years old is 150 beats per minute (20,150). The target heart rate of an 80-year old is 105 beats per minute (80,110). Use this information to write an equation of a line and predict the target heart rate for a 30-year old.		
	$m = \frac{150 - 110}{20 - 80} = -\frac{40}{60} = -\frac{2}{3}$	Calculate the slope from the two given points.	
		Remember: $m = \frac{y_1 - y_2}{x_1 - x_2}$	
	y = mx + b	Plug one of the points we have been given.	
	$150 = \left(-\frac{2}{3}\right)(20) + b$	occii given.	
	163.3 = b	Solve for b.	
	$y = -\frac{2}{3}x + 163.3$	Write out the final equation with the slope and with the y-intercept	
		filled in.	
	$y = -\frac{2}{3}(30) + 163.3$	Plug in $x = 30$	
	y = -20 + 163.3 = 143.3		
L	Answer: 143.3 beats per minute	8	

#### **Section 3-5 Exercises**

3-5

#### Fill out the table for each of the following:

3-1
 1. 
$$2x - 5y = 11$$
 x
 y
 2.
  $y = \frac{7}{2}x + 6$ 
 x
 y

  $5$ 
 $-4$ 
 $0$ 
 $-1$ 
 $0$ 
 $-1$ 
 $0$ 
 $3$ 
 $0$ 
 $7$ 
 $4$ 
 $4$ 
 $4$ 
 $1$ 

Graph the following lines, and label x and y intercepts.

**3.** 
$$4x - 2y = 10$$
 **4.**  $y = -\frac{5}{3}x - 6$  **5.**  $y = 5x$ 

#### Find the slope between each pair of points.

3-3	<b>6.</b> (3,-2) (7,3)	<b>7.</b> (9,1) (-7,6)	<b>8.</b> (5,-1) (-3,-8)
3-3	<b>9.</b> (-2,9) (-2,3)	<b>10.</b> (-5,2) (5,6)	<b>11.</b> (19,1) (6,1)

12. Explain the difference between a slope of zero and an undefined slope.

#### Graph the following lines giving one point and the slope (your point may be different than mine).

3-4	<b>13</b> . $-3x + 4y = 10$	<b>14</b> . $y = 2x - 7$	<b>15</b> . $y = \frac{2}{5}x - 4$
	<b>16.</b> y = 17	<b>17.</b> $y = -\frac{3}{7}x - 2$	<b>18</b> . $2x - 6y = 12$

19. Fill out the Slope Monster (on the next page). Record the time it takes you to complete it.

#### Write the equations of the lines with the slopes and points:

- 20. Write an equation of the line that has slope m = -3 and goes through the point (-4,6).
- 21. Write an equation of the line that at has slope  $m = \frac{5}{8}$  and goes through the point (3,6).
- 22. Write an equation of the line that has slope m = 0 and goes through the point (1,-3).
- 23. Write an equation of the line that is vertical and goes through the point (2, -4)
- **24.** Write an equation of the line that goes through (0,1) and (5,-3).
- **25.** Write an equation of the line that goes through (1,7) and (3,11).
- **26.** Two points on a line are (4,7) and (1,-2). Write the equation of the line and then find the y value when x = 9?
- **27.** The number of lung transplants in year 2 after they were possible was 113. In year 12 after they were possible, there were 248. Using the points (2,113) and (12,248). Find the equation of the line and predict how many were performed in year 16.

# **Slope Monster**

Instructions: For each equation, fill in the slope of that equation and either the slope that is perpendicular to that line or parallel to it. Time yourself and write down how long it took you to complete the whole chart.

Equation	Slope	Perpendicular Slope	Equation	Slope	Parallel Slope
2x + 5y = 7			4x - y = 7		
$y=\frac{5}{9}x-4$			y = 2.387x - 4		
5x - 3y = 7			8x - 3y = 12		
$y = \frac{5}{3}x + 4$			-4x + 7y = 19		
<i>x</i> = 13			x = -19		
$y = \frac{8}{3}x - 8$			$y = \frac{8}{7}x - 4$		
y = 5x - 8			y = -3x - 8		
$y = \frac{7}{9}x + 4$			-10x + 6y = 4		
y = -3			<i>y</i> = 15		
$y = -\frac{3}{11}x - 4$			$y = \frac{6}{11}x - 4$		
7x - 3y = 7			2x - 8y = 17		
$y=\frac{2}{9}x-4$			$y = \frac{5}{2}x + 6$		
5x - 3y = 7			y =06x + 4		
4x + 7y = 19			2x - 9y = 19		
x = -3			<i>x</i> = 7		

Time to complete:\_\_\_\_\_

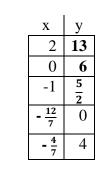
Section 3-5

#### Section 3-5 Answers

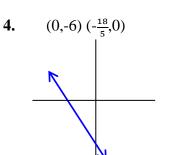
1.

2.

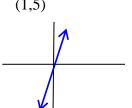
 $\begin{array}{c|ccc}
x & y \\
\hline
5 & -\frac{1}{5} \\
\hline
-4 & -\frac{19}{5} \\
\hline
13 & 3 \\
\hline
\frac{11}{2} & 0 \\
\hline
23 & 7 \\
\end{array}$ 

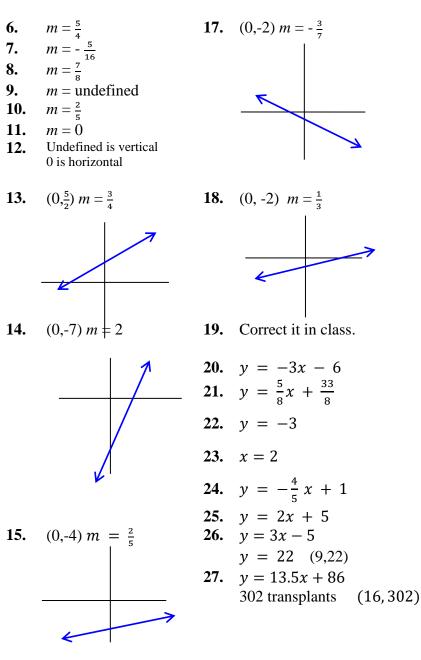


3.  $(0,-5)(\frac{5}{2},0)$ 



5. (0,0) is both intercepts. Graph any other point. (1,5)





**16.** (0,17) m = 0

# **Chapter 3 Review Exercises**

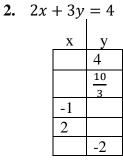
**1.** Create a visual chart of all of the methods, formulas, and examples of finding points and intercepts, graphing lines, finding slope, and writing equations of lines.

3.

#### Fill out the table for each of the following.



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9x - 5y = -160		
	х	У
	-40	
		32
		71.78
	90	
		212

Find the *x*-intercept and *y*-intercept of each of the lines.

3-2

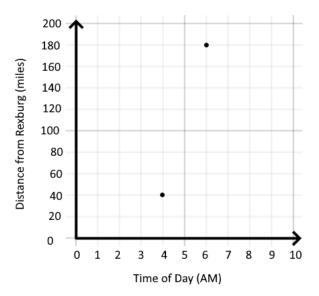
3-3

**4.** 
$$y = .25x - 4$$
 **5.**  $7x - 2y = -3$  **6.**  $x - y = -2$ 

#### Graph each line and find the slope.

**7.** y = -3 **8.** 2x + 5 = 12

**9.** The following graph shows two points for an early morning car trip from Rexburg to Salt Lake. Using the two points, find the average rate of speed of the car.



Find the slope between each pair of points.

**10.** 
$$\left(-3,\frac{2}{3}\right)$$
  $\left(0,\frac{2}{3}\right)$  **11.** (2,-3) (-6,-7)

Chapter 3 Review

Find the slope and y-intercept for each line. Then graph the line.

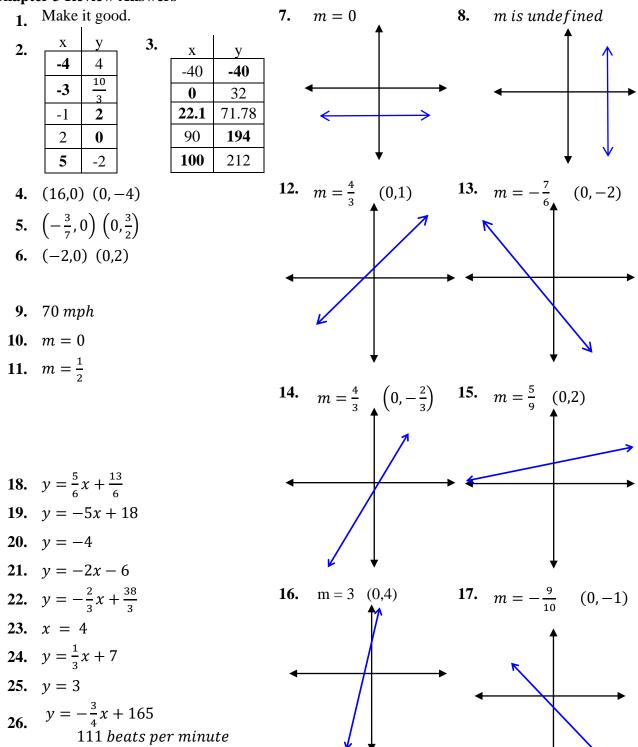
12. 
$$y = \frac{4}{3}x + 1$$
13.  $y = \frac{-7}{6}x - 2$ 14.  $4x - 3y = 2$ 15.  $5x - 9y = -18$ 16.  $y = 3x + 4$ 17.  $y = \frac{-9}{10}x - 1$ 

Write the equation of the line with the given characteristics.

3-518. 
$$m = \frac{5}{6}$$
, goes through (1,3)19.  $m = -5$ , goes through (2,8)20.  $m = 0$ , goes through (2, -4)21.  $\begin{array}{c} Parallel to \ y = -2x + 11, \\ goes through \ (-4,2) \end{array}$ 22.  $\begin{array}{c} Perpendicular to \ y = \frac{3}{2}x - 11, \\ goes through \ (7,8) \end{array}$ 23.  $vertical line going through \ (4,2) \end{array}$ 24.  $contains \ (0,7) and \ (3,8) \end{array}$ 25.  $contains \ (8,3) and \ (-6,3) \end{array}$ 

**26.** Write the equation of the line that represents the target heart rate (y) when compared to age (x) given the points (12, 156) and (48, 129). Then use that line to predict the target heart rate for someone age 72.

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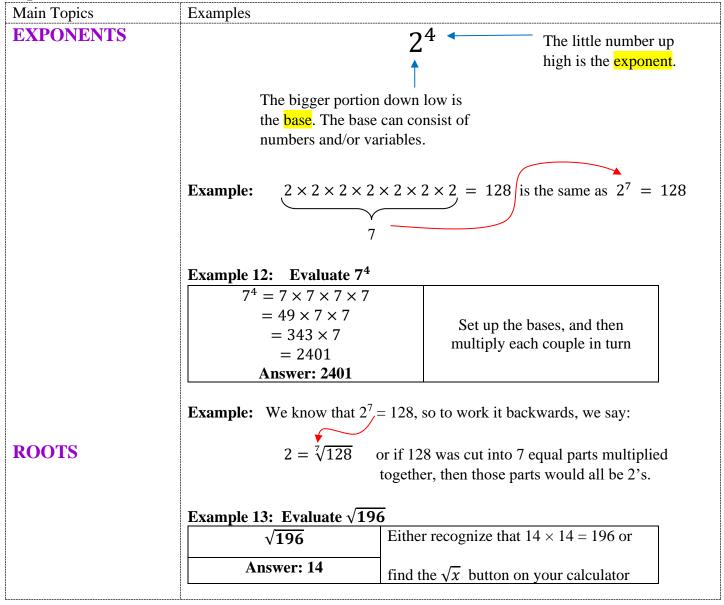


# Section 4-1 Exponents and Rules

4-1: Exponents and Rules	Scientific Notation
4-2: Polynomial Intro	Term, Coefficient, Degree,
Polynomial Addition	Polynomial Subtraction
4-3: Polynomial Multiplication	
4-4: Polynomial Division	

#### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

#### **Exponent Review**



# Exponents

Rule	Examples
One	$7^1 = 7$
Anything to the power of one = itself	
$a^1 = a$	$x^1 = x$
Multiplication	
When expressions with the same base are multiplied, the exponents add.	$x^2 \cdot x^3 = x^5$
$a^m \cdot a^n = a^{m+n}$	$x^3x^7 = x^{10}$
Power	
When we raise a power to a power, the exponents	$(x^2)^3 = x^6$
multiply.	
$(a^m)^n = a^{m \cdot n}$	
Division	
Exponents being divided with the same base are subtracted.	~5
(if $a \neq 0$ )	$\frac{x^5}{x^3} = x^{5-3} = x^2$
	x <sup>2</sup>
$\frac{a^m}{a^n} = a^{m-n}$	
Negative	
All negative exponents can be converted to a positive	
exponent by simply taking the reciprocal.	$3^{-4} = \frac{1}{3^4} = \frac{1}{81}$
$(if a \neq 0)$	3 - 34 - 81
$a^{-m} = \frac{1}{a^m}$	1
$a^m$	$4x^{-3} = \frac{4}{x^3}$
AND	
1 "	$\frac{7}{7} - \frac{7}{7} - 7y^4$
$\frac{1}{a^{-m}} = a^m$	$\frac{7}{y^{-4}} = \frac{7}{1/y^4} = 7y^4$
	, y
Zero exponent	
Anything to the power of $zero = 1$	$7^0 = 1$
(if $a \neq 0$ )	$7^{0} = 1$ $\frac{x^{3}}{x^{3}} = x^{3-3} = x^{0} = 1$
$a^{0} = 1$	$\frac{1}{x^3} = x^{3-3} = x^0 = 1$
Parentheses	$(2x^4)^5 = 32x^{20}$
Exponent applies to everything inside	
	(3) <sup>4</sup> 81
$(ab)^n = a^n b^n \qquad \left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$	$\left(\frac{3}{y}\right)^4 = \frac{81}{y^4}$
	<u> </u>

Using the Laws of Exponents, simplify the following:

PROBLEM	<u>SOLUTION</u>	LAW(S) USED
5 <sup>1</sup>	5	One Rule
<i>x</i> <sup>1</sup>	<i>x</i>	One Rule
$(2x)^0$	1	Zero Rule
$8^3 \cdot 8^{19}$	$8^{3+19} = 8^{22}$	Multiplication Rule
$x^2 \cdot x^7$	$x^{2+7} = x^9$	Multiplication Rule
4 <sup>-2</sup>	$4^{-2} = \frac{1}{4^2} = \frac{1}{16}$	Negative Exponent Rule
$d^{-3} \cdot d^8$	$d^{-3+8} = d^5$ OR $\frac{d^8}{d^3} = d^{8-3} = d^5$	Multiplication Rule or Negative Exponent and Division Rules
$\frac{x^{16}}{x^{16}}$	$x^{16-16} = x^0 = 1$	Division & Zero Rules
$\frac{b^7}{b^5}$	$b^{7-5} = b^2$	Division Rule
$\frac{p^{-2}}{p^{-5}}$	$p^{-2-5} = p^3$ OR $\frac{p^5}{n^2} = p^{5-2} = p^3$	Division Rule or Negative Exponent Rule, then Division Rule
$\frac{x^2}{x^3}$	$\frac{1}{x^{3-2}} = \frac{1}{x^1} = \frac{1}{x}$ OR $x^{2-3} = x^{-1} = \frac{1}{x}$	Division & One Rule or Division, Negative Exponent, & One Rules
$(3x^3)^2$	$3^{1\cdot 2}x^{3\cdot 2} = 3^2x^6 = 9x^6$	Parentheses & Power Rule
$(2x^2y^3z^4)^3$	$2^{1\cdot 3}x^{2\cdot 3}y^{3\cdot 3}z^{4\cdot 3} =$ $2^{3}x^{6}y^{9}z^{12} = 8x^{6}y^{9}z^{12}$	Parentheses & Power Rule
$(5x^2y^{-3})^2$	$5^{1\cdot 2}x^{2\cdot 2}y^{-3\cdot 2} = 5^2x^4y^{-6} = \frac{25x^4}{y^6}$	Power Rule & Negative Exponent Rule

## **Scientific Notation**

Main Topics	Examples		
Sci. Not. ⇒ Decimal	Example 1:		
Multiply or divide by 10.	2.53 X 10 <sup>8</sup> move decimal 8 places 253,000,000		
	Example 2: 4.6 X $10^{-7}$ move 7 places other direction .00000046		
Standard Scientific Notation	All these are the same number:		
leaves one digit left of the	253 X 10 <sup>6</sup>		
decimal.	25.3 X 10 <sup>7</sup>		
	$2.53X  10^8$		
	. 253 X 10 <sup>9</sup>		
	Note that you can always move the decimal <i>left</i> if you move the exponent <i>up</i> and the number will remain unchanged.		
Multiplying and Dividing	Example 3:		
Scientific Notation by hand	$3.1 \times 10^4 \cdot 4 \times 10^8$		
• Powers of 10 follow the rules of			
exponents.	$= 12.4 \times 10^{12}$ Add exponents for powers of 10		
	$= 1.24 \times 10^{13}$ Move decimal left for standard notation		
	Example 4:		
	$7 \times 10^4$		
	$3.5 \times 10^{8}$		
	$= 2 \times 10^{-4}$ Subtract exponents for powers of 10		
Calculator	Become familiar with how your calculator displays and inputs		
Common buttons for scientific notation are	numbers in scientific notation.		
• × 10^	Most calculators will allow you to change the mode, so that all		
• EE	answers, even something like $3 \times 5 = 15$ , will be given in		
	scientific notation: $3 \times 5 = 1.5 \times 10^{1}$ .		

## Section 4-1 Exercises

Find the equation of the given line.

**3-5 1.** 
$$m = -\frac{3}{4}$$
 and goes through (0,2) **2.**  $m = \frac{3}{5}$  and goes through (2,5)

Use positive exponents to express the following.

4-1 3. 
$$\frac{1}{k^{-9}}$$
 4.  $a^5b^{-3}c^{-2}$  5.  $\frac{z^{-1}}{x^{-3}y^{-12}}$ 

Use negative exponents to express the following.

6. 
$$\frac{1}{x^2}$$
 7.  $\frac{3}{B^5}$  8.  $\frac{1}{4^2}$ 

Simplify each expression.

10.  $\frac{p^8}{p^3}$ 11.  $x^9x^{-2}$ **9.**  $t^4 \cdot t^5$ 13.  $(5r^3)^2$ 14.  $2a^4 \cdot 9a^2$ 12.  $(y^5)^6$ 16.  $\frac{Q^{-8}}{Q^{-12}}$ 19.  $\frac{8x^{10}}{2x^7}$ 15.  $(g^{-8})^7$ 17.  $\frac{m^5}{m^{-2}}$ 18.  $\frac{8x^7}{2x^{10}}$ **20.**  $3^5 \cdot 3^3$ **21.**  $\left(\frac{2}{c^8}\right)^{-3}$ 22.  $\left(\frac{m^4}{n^{-3}}\right)^2$ 23.  $\left(\frac{6k^{-5}j^3}{k^5j^2}\right)^{-4}$ 25.  $\frac{17^{38}}{17^{40}}$ 26.  $\left(\frac{5x^3y^8}{x^{14}y^{-3}}\right)^{-2}$ **24.** 5<sup>-2</sup>

Convert into decimal notation.

**27.**  $5.30 \times 10^9$  **28.**  $3.14 \times 10^{-11}$ 

#### Convert into scientific notation.

**29.** 2,000,000 **30.** .000082

## Multiply. Write the answer in scientific notation.

**31.**  $4.2 \times 10^{12} \cdot 1.8 \times 10^{-4}$  **32.**  $3.02 \times 10^{-8} \cdot 7.3 \times 10^{-5}$ 

#### Divide. Write the answer in scientific notation.

<b>33.</b> $\frac{8 \times 10^7}{10^7}$	34.	$5.7 \times 10^{-7}$	35.	$2.7 \times 10^{13}$	
55.	$4 \times 10^{5}$	57.	3×10 <sup>4</sup>	55.	9×10 <sup>-5</sup>

#### Preparation

**36.** After reading some of 4.2, classify each of the following as a monomial, binomial, trinomial. **a)** x + 3m **b)** x + 2y + z **c)**  $5x^2yz$ 

## Section 4-1 Answers

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1.	$y = -\frac{3}{4}x + 2$ or $3x + 4y = 8$	22.	$m^8n^6$
2.	$y = \frac{3}{5}x + \frac{19}{5}$ or $3x - 5y = -19$	23.	$\frac{k^{40}}{1296j^4}  or \ \frac{k^{40}}{6^4j^4}$
3.	<i>k</i> <sup>9</sup>		$\frac{1}{25}$ or . 04
4.	$\frac{a^5}{b^3c^2}$	25.	$\frac{1}{289}$
	$\frac{x^3y^{12}}{z}$	26.	$\frac{x^{22}}{25y^{22}}$
	$x^{-2}$	27.	5,300,000,000
7.	3 <i>B</i> <sup>-5</sup>	28.	.000 000 000 031 4
0	?	20	2 × 10 <sup>6</sup>
	4 <sup>-2</sup>	29.	$2 \times 10^{6}$
8. 9.			$2 \times 10^{6}$ $8.2 \times 10^{-5}$
9.	<i>t</i> <sup>9</sup>	30.	
9. 10. 11.	t <sup>9</sup> p <sup>5</sup> x <sup>7</sup>	30. 31.	$8.2 \times 10^{-5}$
9. 10. 11.	t <sup>9</sup> p <sup>5</sup>	<ul><li>30.</li><li>31.</li><li>32.</li></ul>	$8.2 \times 10^{-5}$ $7.56 \times 10^{8}$
9. 10. 11. 12.	t <sup>9</sup> p <sup>5</sup> x <sup>7</sup>	<ol> <li>30.</li> <li>31.</li> <li>32.</li> <li>33.</li> </ol>	$8.2 \times 10^{-5}$ 7.56 × 10 <sup>8</sup> 2.2046 × 10 <sup>-12</sup>
<ol> <li>9.</li> <li>10.</li> <li>11.</li> <li>12.</li> <li>13.</li> </ol>	t <sup>9</sup> p <sup>5</sup> x <sup>7</sup> y <sup>30</sup>	<ol> <li>30.</li> <li>31.</li> <li>32.</li> <li>33.</li> <li>34.</li> </ol>	$8.2 \times 10^{-5}$ 7.56 × 10 <sup>8</sup> 2.2046 × 10 <sup>-12</sup> 2 × 10 <sup>2</sup>
<ol> <li>9.</li> <li>10.</li> <li>11.</li> <li>12.</li> <li>13.</li> </ol>	t <sup>9</sup> p <sup>5</sup> x <sup>7</sup> y <sup>30</sup> 25r <sup>6</sup> 18a <sup>6</sup>	<ol> <li>30.</li> <li>31.</li> <li>32.</li> <li>33.</li> <li>34.</li> <li>35.</li> </ol>	$8.2 \times 10^{-5}$ 7.56 × 10 <sup>8</sup> 2.2046 × 10 <sup>-12</sup> 2 × 10 <sup>2</sup> 1.9 × 10 <sup>-11</sup>

- **17.** *m*<sup>7</sup>
- 18.  $\frac{4}{x^3}$
- **19.**  $4x^3$
- **20.** <sup>38</sup> or 6561
- 21.  $\frac{c^{24}}{8}$

# Section 4-2 Introduction to Polynomials, Add and Subtract

4-1: Exponents and Rules	Scientific Notation
4-2: Polynomial Intro	Term, Coefficient, Degree,
Polynomial Addition	Polynomial Subtraction
4-3: Polynomial Multiplication	
4-4: Polynomial Division	

#### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

#### **Polynomials and Terms**

i orynomiais and	
Main Topics	Examples
Polynomial	"Poly" means many, and "nomial" means number or term, so a polynomial is something with many terms.
Term	Terms are separated by plus (+) and minus (-) signs. Hence $7x - 5y$ has two terms, and $x^2 + 5x - 6$ has three terms
	The sign before the term always goes with it. Hence the two terms in $7x - 5y$ are $7x$ and $-5$ , and the three terms in $x^2 + 5x - 6$ are $x^2$ , $5x$ , and $-6$ .

The family of polynomials includes the monomials, binomials, and trinomials. Monomials, binomials, and trinomials are all polynomials with either one, two, or three terms respectively:

MONOMIAL	BINOMIAL	TRINOMIAL
Mono = One Nomial = Term(s) "One Term"	Bi = Two Nomial = Term(s) "Two Terms"	Tri = Three Nomial = Term(s) "Three Terms"

## **Polynomials**

Main Topics	Examples
Polynomial Parts	Example 1:
Coefficient: Number in each term.	List the terms, coefficients and degrees of each term. Then
	find the degree of the polynomial.
	$-3x^5y^2 + 2x^4 + 5$
	Three terms = trinomial
	Leading term: $-3x^5y^2$
	• Leading coefficient: -3
Degree of Term: Exponent (total of	• Degree: 7
exponents) on variable of the term.	

	Second term: 2x <sup>4</sup> • Coefficient: 2 • Degree: 4
Degree of Polynomial: Largest degree of all terms.	Last term (Constant term): 5 • Coefficient: 5 • Degree: 0 Degree of polynomial: 7

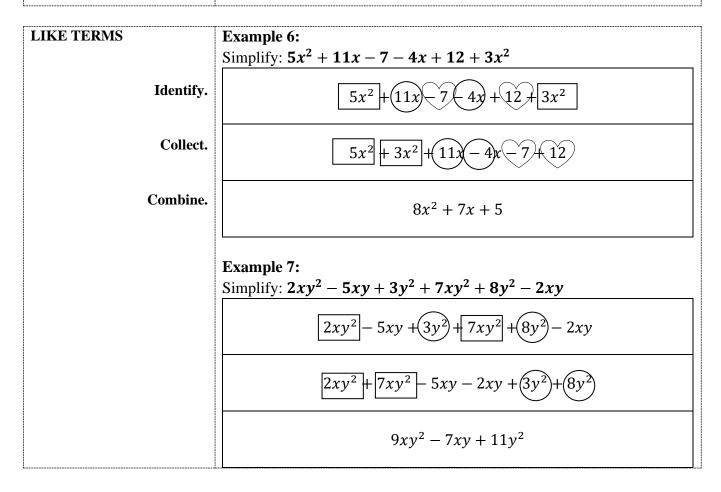
# Polynomial Etiquette: Descending Order

Main Topics	Examples
Main Topics Descending Order largest to smallest degree.	Examples It is common practice, though not right or wrong, to write all answers to polynomial problems in descending order. Example 2: Write in descending order. $4x^5 - 3x - 10 + 9xy^2 - 7xy + 2x^7$
	Answer: $2x^7 + 4x^5 + 9xy^2 - 7xy - 3x - 10$ Example 3: Write in descending order. $2x^3 - 12x + 9x^4 - 7$
	Answer: $9x^4 + 2x^3 - 12x - 7$

# **Evaluating Polynomials**

Main Topics	Examples
	Example 4:
Everywhere there's an x	Evaluate the polynomial $2x^2 - 3x + 5$ , when $x = -1$
you'll <b>substitute</b> in a -1	
	$2x^2 - 3x + 5$
	$2(-1)^2 - 3(-1) + 5$
	2(1) - 3(-1) + 5
You'll now <b>simplify</b> by	2 + 3 + 5
applying the order of	10
operations:	

]	Example 5:
	Evaluate the polynomial $x^2 - 2xy + 3y^2$ , when $x = 2$ and $y = -1$
	$\frac{x^2-2xy+3y^2}{3}$
	$(2)^2 - 2(2)(-1) + 3(-1)^2$
	4 - 2(2)(-1) + 3(1)
	4 + 4 + 3
	11



## **Polynomial Addition and Subtraction**

Main Topics	Examples
Addition	Example 8:
Combine like terms.	$(5x^4 - 3x^2 + 10) + (9x^4 + 4x^2 - 3)$
	$5x^4 - 3x^2 + 10 + 9x^4 + 4x^2 - 3$
	$5x^4 - 3x^2 + 10 + 9x^4 + 4x^2 - 3$
	$14x^4 + x^2 + 7$

	Example 9: $(3q^2 + 7q^3 - q) + (8q - 6q^3)$ $q^3 + 3q^2 + 7q$
Subtraction Distribute the negative. Combine like terms.	Example 10: $(5x^4 - 3x^2 - 10) - (9x^4 + 4x^2 - 3)$ $5x^4 - 3x^2 - 10 - 9x^4 - 4x^2 + 3$ $5x^4 - 3x^2 - 10 + 9x^4 - 4x^2 + 3$ $-4x^4 - 7x^2 - 7$ Example 11: $(5p^3 - 7p + 2) - (5p - 9p^3 - 3)$ $5p^3 - 7p + 2 - 5p + 9p^3 + 3$ $14p^3 - 12p + 5$
Common Mistake Confusing the rules of exponents with combing like terms.	Example 12: $3x^{6} + 5x^{6} = 8x^{6}$ not $3x^{6} + 5x^{6} = 8x^{12}$ Correct. Incorrect.

# Section 4-2 Exercises Simplify.

**4-1 1.**  $(5a)^{-3}$  **2.**  $(2x^{-3}y^{-8})^6$  **3.**  $\left(\frac{9k^{-5}k^3}{h^7}\right)^{-2}$ 

**4.** Express in scientific notation: 15,966,000,000,000

5. Express in decimal form:  $2.97 \times 10^{-9}$ 

#### Perform the indicated operation.

**6.** 
$$5.3 \times 10^{-4} \cdot 1.01 \times 10^8$$
 **7.**  $\frac{1.8 \times 10^{-8}}{6 \times 10^{-6}}$  **8.**  $\frac{9.9 \times 10^{-7}}{3.3 \times 10^4}$ 

Classify the following as monomials, binomials, trinomials.( If none of them, write "polynomial")

4-29. 
$$x^2 - 10x + 25$$
10.  $18a^4b^3yz^9$ 11.  $-2a(b^6c) - xy$ 12.  $a^4 + a^2b^2 + ab^2 - b^3 + 5$ 

Identify each term. Name the coefficient and degree of each term, as well as the degree of the polynomial.

**13.** 9 + 3k **14.**  $x^2 + 8x + 16$  **15.**  $13x^3 + x^2 + 5x + 3$  **16.**  $-14b - 2b^7 + 3$ 

Write in descending order.

**17.** 
$$s + 7 + 3s^2$$
 **18.**  $3x^2 + 5 + x^4 + 2x^3 + 4x$ 

**Evaluate.** 

**19.**  $x^2 - 10x + 25$ <br/>when x = 4**20.**  $3a^4 + 4a^2 - 10a - 19$ <br/>when a = -5**21.**  $a^4 + a^2b^2 + ab^2 - b^3 + 5$ <br/>when a = -1 and b = 3**22.**  $x^3 - 3x^2y + xy^2 + y$ <br/>when x = 2 and y = -4

#### Simplify. Write your answer in descending order.

**23.**  $5x^2 + 3x + x - 9$  **24.**  $4x - 6x^5 + 17x + 15x^5 + 3x - x^3$ 

**25.**  $b^{19} - 4b^{14} + 5b^{20} - 2b^{14}$  **26.**  $(4k - 12k) + 5k^2 - 4$ 

**27.** 
$$-x^8 - 5xy + 4xy^2 - 9x^3y + x^8$$
**28.**  $\frac{7}{2}y^2 + x^4 - \frac{3}{2}y^2 + \frac{1}{3}x^3 + 7y$ **Add the polynomials.30.**  $(4a) + (2a - 5)$ **31.**  $(-7x^2 + 5y - 17) + (3x^2 - 4x + 12y)$ **32.**  $(5x^4 - x^3 + 3x^2 - 5) + (4x^4 + 4x^3 + x)$ 

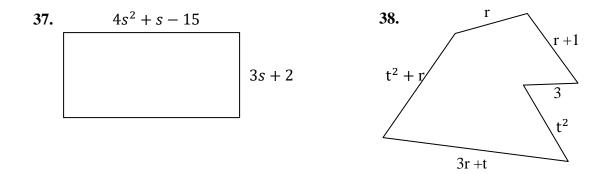
Subtract the polynomials.

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**33.** (5x+2) - (4x+3) **34.**  $(3x^2 - x + 7) - (9x^2 + x + 8)$ 

**35.** 
$$(4y^7 + x^2 + 6y) - (6y^7 - 5y^5 + 11x^2 - y + 17)$$
 **36.**  $(6a^3 - b^3 + b^2) - (-a^3 + 2b^3 - b^2)$ 

#### Find a polynomial that describes the perimeter of these shapes.



### **Preparation:**

1-3

**39.** Match the following three equations with the property that is being used.

a. $9(x-2) = 9x - 18$	Commutative Addition
b. 3ab + 4t = 4t + 3ab	Associative Multiplication
c. $2(x5) = (2x)5$	Distributive

Section 4-2 Answers

1. 
$$\frac{1}{125a^3}$$

2. 
$$\frac{64}{x^{18}y^{48}}$$

3. 
$$\frac{n - \kappa}{81}$$

- 4. 1.5966  $\times 10^{13}$
- **5.** .0000000297

6.  $5.353 \times 10^4$ 

- 7.  $3 \times 10^{-3}$
- 8.  $3 \times 10^{-11}$
- 9. Trinomial
- **10.** Monomial
- **11.** Binomial
- 12. Polynomial
- 13. 9: coefficient = 9, degree = 03k: coefficient = 3, degree = 1degree of polynomial = 1
- 14.  $x^2$ : c = 1, d = 2
  - 8*x*: c = 8, d = 1
  - 16: c =16, d = 0

degree of polynomial = 2

**15.**  $13x^3$ : c = 13, d = 3

$$x^2$$
: c = 1, d = 2

$$5x: c = 5, d = 1$$

3: c = 3, d = 0

degree of polynomial = 3

**16.**  $-2b^7$ : c = -2, d = 7 -14b: c = -14, d = 1 3: c = 3, d = 0 degree of polynomial = 7 **17.**  $3s^2 + s + 7$  18.  $x^4 + 2x^3 + 3x^2 + 4x + 5$ **19.** 1 **20.** 2006 **21.** -21 **22.** 84 23.  $5x^2 + 4x - 9$ 24.  $9x^5 - x^3 + 24x$ 25.  $5b^{20} + b^{19} - 6b^{14}$ **26.**  $5k^2 - 8k - 4$ 27.  $-9x^3y + 4xy^2 - 5xy$ **28.**  $x^4 + \frac{1}{3}x^3 + 2y^2 + 7y$ **29.** 4x + 3**30.** 6a - 5**31.**  $-4x^2 - 4x + 17y - 17$ 32.  $9x^4 + 3x^3 + 3x^2 + x - 5$ 33. x - 134.  $-6x^2 - 2x - 1$ **35.**  $-2v^7 + 5v^5 - 10x^2 + 7v - 17$ **36.**  $7a^3 - 3b^3 + 2b^2$ 37.  $8s^2 + 8s - 26$ **38.**  $2t^2 + t + 6r + 4$ **39.** In class.

# Section 4-3 Polynomial Multiplication

	,
4-1: Exponents and Rules	Scientific Notation
4-2: Polynomial Intro	Term, Coefficient, Degree,
Polynomial Addition	Polynomial Subtraction
4-3: Polynomial Multiplication	
4-4: Polynomial Division	

## CHAPTER OVERVIEW (Video Instruction and Solutions Link)

## Type 1: Monomials $\times$ Monomials

Main Topics	Examples
	<b>Example 1:</b> Multiply $(4x)(5x)$
Steps	
1. Multiply	$4 \cdot x \cdot 5 \cdot x$
numbers with	$4 \cdot 5 \cdot x \cdot x$
numbers	$20x^2$
(coefficients).	<b>Example 2:</b> Multiply $(-4.5)(0.2)$
2. Multiply like	$(-4x^5)(6x^2)$
	$(-4)(6) x^5 \cdot x^2$
variables with	$-24x^{5+2}$
like variables	$-24x^{7}$
(x's with x's, y's with y's).	Answer: $-24x^7$
	Example 3: Multiply
	$(4xy^2)(-2x^3y)$
	$(4)(-2)  x \cdot x^3  y^2 \cdot y$
	$-8x^{1+3}y^{2+1}$
	$-8x^4y^3$
	Answer: $-8x^4y^3$
	Example 4: Multiply
	$(-2y^2)(6y^3)(-4y^5)$
	$\begin{array}{c} (-2)(6)(-4) y^2 \cdot y^3 \cdot y^5 \\ 48y^{2+3+5} \end{array}$
	$48y^{10}$
	Answer: $48y^{10}$

Main 7	Topics	Examples			
Steps:		<b>Example 5:</b> Multiply $3x(5x)$			
1. Multiply the				tribute the monomial to the	
	monomial (the		polynomial.		
	distributor) times	(3x)(5x) + (3x)(-4)		ltiply $3x$ to each term in the	
	each term in the		poly	ynomial.	
	polynomial.	$2 \Gamma n n + 2(-4) n$	Nor	whendle each (mono)y(tomo)	
2.	Format it such that	$3 \cdot 5 x \cdot x + 3(-4) x$		w handle each (mono)×(term). pplify if needed.	
	you have:	$15x^2 - 12x$	SIII	ipiny in needed.	
	(mono)×(term) +	Answer: $15x^2 - 12x$			
	$(mono) \times (term) +$				
	keeping the sign of each term with it	<b>Example 6:</b> Multiply $-4x(-$	-r —	4)	
	in the parentheses.	-4x(-x-4)	λ	Distribute the $(-4x)$ , not just the	
3.	Combine like terms			(4x).	
0.	and simplify.	(Aw)(w) + (Aw)(A			
	1 2	(-4x)(-x) + (-4x)(-4x)(-4x)(-4x)(-4x)(-4x)(-4x)(-4x)	•)		
		( A)( 1) = a + (A)(A)	)	Multiply graph and times graph and	
		$\left  (-4)(-1)x \cdot x + (-4)(-4) \right $	:) x	Multiply numbers times numbers and like terms times like terms.	
		$4x^2 + 16x$		and like terms times like terms.	
		Answer: $4x^2 + 16x$			
		<b>Example 7:</b> Multiply $2x^2(3x)$	$x^{2} -$	6x + 8)	
		$2x^2(3x^2-6x+8)$		$anno \times (any polynomial)$	
			111	(any porynolinal)	
		$(2x^2)(3x^2) + (2x^2)(-6x)$	)		
		$+(2x^2)(8)$			
		(2)(3) $x^2 \cdot x^2$	N/	Iultiply numbers times	
		$(2)(3) x \cdot x + (2)(-6) x^2 \cdot x$		umbers and like terms times	
				ke terms.	
		$\frac{+(2)(8) x^2}{6x^4 - 12x^3 + 16x^2}$			
		Answer:			
		$6x^4 - 12x^3 + 16x^2$			
		<u> </u>			

# **Type 2: Monomials** × **Polynomial**

# **Type 3: Binomials × Binomials**

Main Tonice	Evamples			
	Examples			
Steps: 1. SUPER	<b>Example 8:</b> Multiply $(x + 3)(x - 7)$			
Distribute.	(x+3)(x-7) binomial × binomial			
		Multiply each term in the 1 <sup>st</sup> set of		
	x(x-7) + 3(x-7)	parentheses by each term in the 2 <sup>nd</sup> set of parentheses.		
	(x)(x) + (x)(-7) + (3)(x) + (3)(-7)	Format as (mono)×(term) + (mono)×(term) +		
	$x^2 - 7x + 3x - 21$	Multiply each term.		
	$x^2 - 4x - 21$	Combine like terms to simplify.		
	<b>Example 9:</b> Multiply $(4x - 2)(2x - 3)$	)		
	(4x-2)(2x-3)			
		Everything in first set of parentheses goes to everything in the second set		
	$8x^2 - 12x - 4x + 6$	Simplify		
	$8x^2 - 16x + 6$			
	Answer: $8x^2 - 16x + 6$			
Extra Information				
FOIL		nonic device (tool for memorization).		
TOIL	It is no different than the rule: <b>everything in the 1<sup>st</sup> parentheses goes to</b> <b>everything in the 2<sup>nd</sup> parentheses</b> where			
		b(c+d) = ac + ad + bc + bd		
	(u + b)(c + u) = u(c + u) +			
	$\mathbf{F} = \mathbf{First}, \mathbf{O} = \mathbf{Outst}$	ide, I = Inside, L = Last		
	First terms $= a \cdot c$ , Outside terms $= a \cdot a$	l, Inside terms = $b \cdot c$ , and Last terms = $b \cdot c$		
		d		
	Hence, <i>ac</i> +	-ad + bc + bd.		
BOX Polynomial multiplication can also be visualized by a <b>box</b> with one polynomial on one other on another side. The area is the multiplication. <b>Example 9 (again):</b> $4x -2$				
	Example 9 (again): $4x -2$ $2x 8x^2 -4x$ -3 -12x +6			
	And combine like terms to get $8x^2 - 16x$	<b>:</b> + <b>6</b> .		

Type 4:	Anv	Poly	nomial	x	Anv	Polv	nomial
турс т.	<b>1 1 1 1</b>	I UI	nonnai	~	<b>I MII </b>	I UIJ	nomai

Main Topics	Examples		
SUPER Distribute	Example 10: Multiply		
$(x-2)(x^{2}-5x-x)(x^{2}-5x-x)(x^{2}-5x+6) - 2(x)(x^{2}) + (x)(-5x) + (x)(6) + (-2)(x^{2})(x^{2})(x^{2}) + (x)(-5x) + (x)(6) + (-2)(x^{2})(x^{2})(x^{3}-5x^{2}+6x-2x^{2}+x)(x^{3}-5x^{2}+6x-2x^{2}+x)(x^{3}-5x^{2}+6x-2x^{2}+x)(x^{3}-5x^{2}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3}-5x^{3}+16x-x)(x^{3}-5x^{3}-5x^{3$	$x^{2} - 5x + 6)$ (x) + (-2)(-5x) + (-2)(6) (x) - 10x - 12 (-12)	Everything in the 1 <sup>st</sup> ( ) goes to Everything in the 2 <sup>nd</sup> ( ) Follow ( <b>mono</b> )×( <b>term</b> ) +format Multiply the ( <b>mono</b> )×( <b>mono</b> )'s Use symbol method for like terms Combine like terms	
	<b>Example 11:</b> $(2x^2 - 5x^2)$	$(x^2 + 1)(x^2 + 5x - 1)$	
Slick Note: You could stack them so the like terms are above each other: $(2x^2 - 5x + 1)(x^2 + 5x - 1)$ $2x^2(x^2 + 5x - 1) - 5x(x^2 + 5x - 1) + 1(x^2 + 5x - 1)$			
$2x^{4} + 10x^{3} - 2x^{2} -5x^{3} - 25x^{2} + 5x +x^{2} + 5x - 1 2x^{4} + 5x^{3} - 26x^{2} + 10x - 1$	$2x^{4} + 10x^{3} - 2x^{2} - 5x^{3} - 25x^{2} + 5x + x^{2} + 5x - 2x^{4} + 5x^{3} - 26x^{2} + 10x - 1$		
$2x + 5x^{2} - 20x + 10x - 1$	Answer: $2x^4$ +	$-5x^3 - 26x^2 + 10x - 1$	
(Binomial) <sup>2</sup>	x <sup>2</sup> - x Example 13:	$(x + 3)^{2} + 3)(x + 3) + 3x + 3x + 9$ + 3x + 3x + 9 + 6x + 9 (3x - y)^{2}	
	$(3x)$ $9x^2 -$	(3x - y) -y)(3x - y) $3xy - 3xy + y^{2}$ $^{2} - 6xy + y^{2}$	

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Common Mistake	People often take $(x + 3)^2$ and incorrectly say the answer is $x^2 + 9$
This mistake is called the <i>Freshman's Dream</i> .	1. They apply the Law of Exponent Power Rule from Section 4.1 which states that everything in the parentheses receives the power. This is only true for monomials, and we have a binomial.
	2. When they do this they just square the x and square the 3 to get $x^2 + 9$ <u>an incorrect answer</u>
	3. It is critical to remember that anything being squared is really that thing times itself, i.e.
	$(x+3)^2 = (x+3)(x+3)$
	Even the Power Rule is just a short cut around this fact,
	i.e. $(3x)^2 = (3x)(3x)$ .

4-1 **1.** 
$$\frac{kx^2gf^{-1}}{x^{-3}f^2}$$
 **2.**  $\left(\frac{1}{4a^2b^{-3}}\right)^{-1}$ 

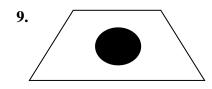
Perform the indicated operation. Write your answer in both scientific notation and decimal form.

**3.** 
$$1.23 \times 10^{-3} \cdot 4.36 \times 10^{4}$$
 **4.**  $\frac{4.36 \times 10^{3}}{5.02 \times 10^{-2}}$  **5.**  $\frac{6.02 \times 10^{23}}{4.8 \times 10^{25}}$ 

Identify each term. Name the coefficient and degree of each term, as well as the degree of the polynomial.

**6.** 
$$4q^3 - 2q^2 + 3q - 2$$
 **7.**  $3p^2 + 4p$  **8.**  $3j^3 - 5$ 

The area of the black circle is  $6y^2 - 2y + 3$ . The area of the trapezoid is  $-2y^2 + 4y + 11$ . Find the area of the white section between the black circle and the outer trapezoid.



Perform the indicated operations.

4-210. 
$$-2x + (3x - 4)$$
11.  $-(3x + 4) - (2x^2 + x)$ 12.  $3z^3 - (2z^2 + 7z^3) + \frac{1}{2}z^2$ 13.  $3m(k^2 - 2m^2 + 1)$ 4-314.  $(3s - 1)(s + 4)$ 15.  $(s^2 - 2)(s + 2)$ 16.  $(a + b)(2a^2 + a - 3)$ 17.  $(c^2 - 2c + 1)(2c^2 + c - 3)$ 

#### Perform the indicated operations.

18. 
$$(x-3)(x+3)$$
19.  $(2x+1)(2x-1)$ 20.  $(3mn-1)(3mn+1)$ 21.  $(3a+4b)(3a-4b)$ 22.  $(k^3-3)(k^3+3)$ 23.  $(3x+1)^2$ 24.  $(2x-1)^2$ 25.  $(k+2)^2$ 26.  $(z^2-1)^2$ 27.  $(k^3+2m)^2$ 

Preparation: After reading some of 4.4, simplify the following.

**28.** 
$$\frac{(8y^2+4)}{2}$$
 **29.**  $(6x^3-2x^2+x) \div x$ 

## 166 Section 4-3 Answers

1. 
$$\frac{kx^5g}{f^3}$$
  
2.  $\frac{4a^2}{b^3}$   
3.  $5.3628 \times 10^1$ ,  $53.628$   
4.  $8.685 \times 10^4$ ,  $86852.59$   
5.  $1.254 \times 10^{-2}$ ,  $.01254$   
6.  $4q^3$ : coefficient = 4, degree = 3;  
 $-2q^2$ : coefficient = -2, degree = 2  
 $3q$ : coefficient = -2, degree = 1  
 $-2$ : coefficient = -2, degree = 0  
degree of polynomial = 3  
7.  $3p^2$ : c = 3, d = 2  
 $4p$ : c = 4, d = 1  
degree of polynomial = 2  
8.  $3j^3$ : c = 3, d = 3  
 $-5$ : c = -5, d = 0  
degree of polynomial = 3  
9.  $-8y^2 + 6y + 8$   
10.  $x - 4$   
11.  $-2x^2 - 4x - 4$   
12.  $-4z^3 - \frac{3}{2}z^2$   
13.  $-6m^3 + 3mk^2 + 3m$   
14.  $3s^2 + 11s - 4$   
15.  $s^3 + 2s^2 - 2s - 4$   
16.  $2a^3 + a^2 - 3a + 2a^2b + ab - 3b$   
17.  $2c^4 - 3c^3 - 3c^2 + 7c - 3$   
18.  $x^2 - 9$   
19.  $4x^2 - 1$ 

20.  $9m^2n^2 - 1$ 21.  $9a^2 - 16b^2$ 22.  $k^6 - 9$ 23.  $9x^2 + 6x + 1$ 24.  $4x^2 - 4x + 1$ 25.  $k^2 + 4k + 4$ 26.  $z^4 - 2z^2 + 1$ 27.  $k^6 + 4k^3m + 4m^2$ 28. In class. 29. In class.

Section 4-3

# Section 4-4 Polynomial Division

1: Exponents and Rules	Scientific Notation
2: Polynomial Intro	Term, Coefficient, Degree,
Polynomial Addition	Polynomial Subtraction
3: Polynomial Multiplication	
4: Polynomial Division	

## CHAPTER OVERVIEW (Video Instruction and Solutions Link)

# **Type 1: Polynomials** ÷ **Monomials**

Main Topics	Examples
<ol> <li>Steps:         <ol> <li>Place the monomial under each term in the polynomial.</li> <li>Simplify each new term of (monomial/monomial) dividing numbers with numbers and like variables with like variables. Use the law of</li> </ol> </li> </ol>	<b>Example 1:</b> Divide $\frac{35x^5-20x^3}{5x^3}$ $\frac{35x^5}{5x^3} - \frac{20x^3}{5x^3}$ Place the monomial under each term in the polynomial $\frac{35}{5x^3} - \frac{20}{5x^3}$ Simplify each new term. Divide numbers with numbers and like variables with like variables. $7x^2 - 4x^0$ Using the quotient rule (4.1) we subtract top-bottom exponents $7x^2 - 4$ The zero rule says $x^0 = 1$ and we know anything times $1 =$ 's itselfAnswer: $7x^2 - 4$
exponents.	Example 2: Divide: $(24a^6 - 48a^5 + 10a^4) \div (4a^4)$ $\frac{24a^6}{4a^4} - \frac{48a^5}{4a^4} + \frac{10a^4}{4a^4}$ Place the monomial under each term in the polynomial.
	$\frac{24}{4}a^{6-4} - \frac{48}{4}a^{5-4} + \frac{10}{4}a^{4-4}$ Simplify each new term. $6a^2 - 12a^1 + \frac{5}{2}a^0$ Reduce them as much as possible. $6a^2 - 12a + \frac{5}{2}$ In simplifying, use the zero and one rule for exponents if needed.Answer: $6a^2 - 12a + \frac{5}{2}$

<b>Example 3:</b> Divide $\frac{15x^{10}y^7 - 8x^6y^3 + 3x^2y^3}{3x^2y^3}$	$\frac{18x^4y - 3x^2y}{y}$
$\frac{15x^{10}y^7}{3x^2y} - \frac{8x^6y^3}{3x^2y} + \frac{18x^4y}{3x^2y} - \frac{3x^2y}{3x^2y}$	Place the monomial under each term in the polynomial.
$\frac{15}{3}x^{10-2}y^{7-1} - \frac{8}{3}x^{6-2}y^{3-1} + \frac{18}{3}x^{4-2}y^{1-1} - \frac{3}{3}x^{2-2}y^{1-1}$	Simplify each new term.
$5x^8y^6 - \frac{8}{3}x^4y^2 + 6x^2y^0 - 1x^0y^0$	Not all fractions reduce completely
$5x^8y^6 - \frac{8}{3}x^4y^2 + 6x^2 - 1$	Use the Zero and One Rule
Answer: $5x^8y^6 - \frac{8}{3}x^4y^2 + 6x^2 - 1$	
	1

# Long Division (for more than 1 term)

Main Topics	Examples				
Long-hand	Example 5: Divide $(8x^3 - 34x^2 + 43x - 77) \div (2x - 7)$ $ \begin{array}{r} 4x^2 - 3x + 11 \\ 2x - 7  8x^3 - 34x^2 + 43x - 77 \\ \underline{8x^3 - 28x^2} \\ -6x^2 + 43x \\ \underline{-6x^2 + 21x} \\ 22x - 77 \\ \underline{22x - 77} \\ 0 \end{array} $				
	0				
	Answer: $4x^2 - 3x + 11$				
Special Consideration Add in missing terms	<b>Example 6:</b> Divide $(12x^3 - 5x - 33) \div (2x - 3)$				
Add in missing terms	$6x^2 + 9x + 11$				
	$2x-3$ $12x^3 + 0x^2 - 5x - 33$				
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$				
	$\frac{18x^2 - 5x}{18x^2 - 27x}$				
	22x - 33				
	$\frac{22x-33}{0}$				
	Answer: $6x^2 + 9x + 11$				

#### Section 4-4 Exercises Simplify.

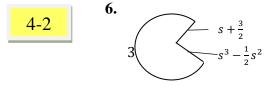
**1.** 
$$a^2 e^3 i^{-2} o^0 u^{-2} a^3 e^{-4} i^{-2} o^{-2} u^4$$
 **2.**  $e^2 i^{-3} e^4 i^{-2} o^3$  **3.**  $\frac{r^2 a^{-3} c e^2}{c^4 a r^{-1}}$ 

10.

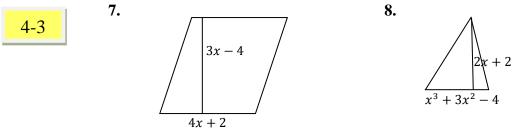
Simplify. Write your answer in descending order.

**4.** 
$$\frac{3}{(s+1)^{-2}}$$
 **5.**  $-j + 4j^2 - 3j - 1 + \frac{1}{j^{-1}}$ 

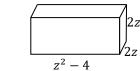
Find a polynomial that describes the perimeter of the shape.

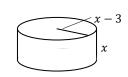


Find a polynomial that describes the area of these shapes.



Find a polynomial that describes the volume of these shapes.





#### Perform the indicated operations

9.

11.  $4x + 2x^2 + x - 2x^2 + 5x - 3x^2$ 13.  $4y + 3y^2x + y(4yx + 5)$ 15.  $8g(3h^3 + 9h - 12)$ 17.  $(7a^2 + 3)(2a^2 + 3a + 6)$ 19.  $(8f^2 + 6)(8f^2 - 6)$ 21.  $(7x + 1)^2$ 

12. 
$$z^{3} + 4z^{2} - 12z - (-z^{3} + z - 3z^{2})$$
  
14.  $-12m(6m^{3} - 8m^{2} + m - 12)$   
16.  $(3p + 4)(p - 4)$   
18.  $(\frac{1}{2}b + 1)(\frac{1}{2}b - 1)$   
20.  $(m^{2}n^{2} + 1)(m^{2}n^{2} - 1)$   
22.  $(w^{2}x^{2} - y^{2}z^{2})^{2}$ 

#### Perform the indicated operations.

4-4  
23. 
$$9m^4 \div (3m)$$
  
25.  $(2x^2y + 3xy + y^2 - 2) \div (2x)$   
27.  $(4b^{13} - 9b^8 - 3b^5) \div (3b^3)$   
29.  $(18x^2 - 23x - 6) \div (2x - 3)$ 

24.  $(6x^2 + 12x) \div (3x)$ 26.  $(-56y^4 + 44y^3 + 64y^2 - 16y) \div (8y)$ 28.  $(-6y^5 - 3y^3 + y) \div (2y)$ 30.  $(18x^3 - 5x + 2) \div (3x + 2)$ 

## 170 Section 4-4 Answers

section	4-4 Allowel 5		
1.	$\frac{a^5u^2}{ei^4o^2}$	22.	$w^4x^4 - 2w^2x^2y^2z^2 + y^4z^4$
2.	$\frac{e^6 o^3}{i^5}$	23.	3 <i>m</i> <sup>3</sup>
3.	$\frac{r^3e^2}{a^4c^3}$	24.	2x + 4
4.	$3s^2 + 6s + 3$	25.	$xy + \frac{3}{2}y + \frac{y^2}{2x} - \frac{1}{x}$
5.	$4j^2 - 3j - 1$	26.	$-7y^3 + \frac{11}{2}y^2 + 8y - 2$
6.	$s^3 - \frac{1}{2}s^2 + s + \frac{9}{2}$	27.	$\frac{4}{3}b^{10} - 3b^5 - b^2$
7.	$12x^2 - 10x - 8$	28.	$-3y^4 - \frac{3}{2}y^2 + \frac{1}{2}$
8.	$x^4 + 4x^3 + 3x^2 - 4x - 4$	29.	9x + 2
9.	$4z^4 - 16z^2$	30.	$6x^2 - 4x + 1$
10.	$\pi(x^3 - 6x^2 + 9x)$ or		
	$\pi x^3 - 6\pi x^2 + 9\pi x$		
11.	$-3x^2 + 10x$		
12.	$2z^3 + 7z^2 - 13z$		
13.	$7y^2x + 9y$		
14.	$-72m^4 + 96m^3 - 12m^2 + 144m$		
15.	$24gh^3 + 72gh - 96g$		
16.	$3p^2 - 8p - 16$		
17.	$14a^4 + 21a^3 + 48a^2 + 9a + 18$		
18.	$\frac{1}{4}b^2 - 1$		
19.	$64f^4 - 36$		
20.	$m^4 n^4 - 1$		
21.	$49x^2 + 14x + 1$		

### **Chapter 4 Review Exercises**

1. Create a visual chart of all the methods, formulas, and examples of how to work with exponents and polynomials.

Simplify or evaluate.

4

-1  
2. 
$$3^2 \cdot 3^{-4}$$
  
3.  $\left(\frac{2}{3}\right)^2$   
4.  $\frac{m^{-2}a^2t^{-3}h^{-3}}{h^2a^{-7}p^2p^{-3}y^2}$   
5.  $\frac{g^4m^3}{(a^{-2}gm^2)^{-1}}$   
6.  $\left(\frac{4xy^3}{3x^2y^{-5}z^3}\right)^{-2}$   
7.  $\left(\frac{2a^{-5}b^4c^{-1}}{a^{-2}b^9}\right)^4$ 

Perform the operation and write your answer in scientific form. Round to three decimal places.

8. 
$$\frac{6.3781 \times 10^3}{1.989 \times 10^{30}}$$
 9.  $\frac{1.51 \times 10^{-7}}{5.002 \times 10^{-5}}$ 

Evaluate the polynomials at the given values.

**4-2 10.** 
$$a^2 - 3a + 2$$
, for  $a = 5$  **11.**  $x^3 + 2x^2 - 4x$ , for  $x = -3$ 

Add or subtract the polynomials. Write answer in descending order.

**12.** 
$$(-3y^2 + 7) + (y^2 + 2y - 6)$$
  
**13.**  $(4x^3 - 1 + x + 3x^2) + (x^2 - x + 5)$   
**14.**  $(3j^4 - j + 2j^2) - (-j^2 + 4j + j^4)$   
**15.**  $(-3p - 9p^2) - (-12p^2 - 5p + 4)$ 

Perform the indicated operations.

16.

18.

20.

22.

24.

26.

28.

30.

4-3

$$(3x)(x-5)$$
17.  $(-\frac{1}{2}a)(4a^2+6a-2)$  $(5d^2-1)(3d+1)$ 19.  $(6e+4)(-5e+3)$  $(g-7)(g+6)$ 21.  $(hi+2)(i-3h)$  $(j+2k)(k^2-2j)$ 23.  $(2l-3)(2l+3)$  $(4m^3-2)(4m^3+2)$ 25.  $(n^6+3y^3)(n^6-3y^3)$  $(5p^2+1)^2$ 27.  $(-q+2)^2$  $(2r+2s)^2$ 29.  $(t+3)(t^2-3t-4)$  $(u^2+u^3)(u^3-u^2+u-1)$ 31.  $(2x^4+7x^3-x)(x^2+3x+2)$ 

Divide the polynomials.

#### 4-4

32. 
$$(-80w^6 + 35w^5 - 50w^4) \div (10w^4)$$
 33.  $(33x^2)$   
34.  $(24y^3 - 2y^2) \div (2y)$  35.  $(8ab)$ 

**3.** 
$$(33x^3 - 18x^2 + 3x) \div (3x)$$
  
**5.**  $(8abz^3 - 2jz^4 + z^5) \div (z^3)$ 

Chapter 4 Review

## **Chapter 4 Review Answers**

Cnapt	er 4 Review Answers		
1.	Make it neat, thorough, and organized.	26.	$25p^4 + 10p^2 + 1$
2.	$\frac{1}{9}$	27.	$q^2 - 4q + 4$
3.	$\frac{4}{9}$	28.	$4r^2 + 8rs + 4s^2$
4.	$\frac{a^9p}{m^2t^3h^5y^2}$	29.	$t^3 - 13t - 12$
5.	$\frac{g^5m^5}{a^2}$	30.	$u^{6} - u^{2}$
6.	$\frac{9x^2z^6}{16y^{16}}$	31.	$2x^6 + 13x^5 + 25x^4 + 13x^3 - 3x^2 - 2x$
7.	$\frac{16}{a^{12}h^{20}c^4}$	32.	$-8w^2 + \frac{7}{2}w - 5$
8.	$3.207 \times 10^{-27}$	33.	$11x^2 - 6x + 1$
9.	$3.019 \times 10^{-3}$	34.	$12y^2 - y$
10.	12	35.	$8ab - 2jz + z^2$
11.	3		
12.	$-2y^2 + 2y + 1$		
13.	$4x^3 + 4x^2 + 4$		
14.	$2j^4 + 3j^2 - 5j$		
15.	$3p^2 + 2p - 4$		
16.	$3x^2 - 15x$		
17.	$-2a^3 - 3a^2 + a$		
18.	$15d^3 + 5d^2 - 3d - 1$		
19.	$-30e^2 - 2e + 12$		
20.	$g^2 - g - 42$		
21.	$hi^2 - 3h^2i + 2i - 6h$		
22.	$2k^3 + jk^2 - 4jk - 2j^2$		
23.	$4l^2 - 9$		
24.	$16m^6 - 4$		
25.	$n^{12} - 9y^6$		

# Section 5-1 Factoring: Method 1 and 2 (GCF and Grouping)

THE 5 METHODS of FACTORING				
Method	<b>Type of Polynomial used on:</b>			
1: Greatest Common Factor (GCF)	All			
2: Grouping	4 Terms			
3: $ax^2 + bx + c$ , where $a = 1$	Trinomials, where $a = 1$			
4: $ax^2 + bx + c$ , where $a \neq 1$ $ac - method$	Trinomials, where $a \neq 1$			
5: Special Cases	Binomials & Perfect Squares			

## CHAPTER OVERVIEW (Video Instruction and Solutions Link)

#### WHEN TO TRY EACH METHOD:

Polynomial	Factoring Methods Possible		
$y^3 + 4y^2 + 2y + 8$	Method 1: Greatest Common Factor Method 2: Grouping		
$x^2 + 6x + 9$	Method 1: Greatest Common Factor Method 3: $ax^2 + bx + c$ , where $a = 1$		
$16x^2 - 16x + 4$	Method 1: Greatest Common Factor Method 4: $ax^2 + bx + c$ , where $a \neq 1$		
$54x^3 - 6x$	Method 1: Greatest Common Factor Method 5: Special Cases (because it's a binomial)		
$x^2 - 5x + 6$	Method 1: Greatest Common Factor Method 3: $ax^2 + bx + c$ , where $a = 1$		
$2c^3 + 8c^2 - 6c - 12$	Method 1: Greatest Common Factor Method 2: Grouping		
$36a^2 - 25$	Method 1: Greatest Common Factor Method 5: Special Cases (because it's a binomial)		
$35x^3 + 42x^2 - 14x - 77xy - 14y + 7$	Method 1: Greatest Common Factor (only method because it has 6 terms)		
$6y^2 + 25y + 25$	Method 1: Greatest Common Factor Method 4: $ax^2 + bx + c$ , where $a \neq 1$		

PRIME: A polynomial that cannot be factored is called **prime.** (Just like a number that cannot be factored.)

Main Topics	Examples		
Greatest Common Factor	<b>Example 1:</b> Identify the GCF of the following: 18, 30, 42		
Largest number that will go			
into all terms	Factors of 18: 1, 2, 369, 18		
	Factors of 30: 1, 2, 3, 5 6 10, 15, 30		
	Factors of 42: 1, 2, 3, 6, 7, 14, 21, 42		
	GCF = 6		
	<b>Example 2:</b> Identify the GCF of the following:		
	$10x^2y, 20x^2, 35x^2y^2$		
	Factors of 10: 1, 2(5,10		
	Factors of 20: 1, 2, 4 5, 10, 20		
	Factors of 35: 1,57, 35		
	x² is also common		
Prime	$GCF = 5x^2$		
Can't be factored	Example 3:		
	These are prime polynomials.		
	$2x + 7$ $4x - 19$ $9y^2 + 20$		
	Example 4: Factor		
	3a-6b		
	GCF = 3		
	3(a-2b)		
Steps			
1. Identify GCF.	Example 5: Factor		
2. Un-Distribute.	4x - 5xy		
a. Place GCF outside.	GCF = x		
b. Divide each term by GCF.	x(4-5y)		
	Example 6: Factor		
	$15x^3 - 5x^2 + 30xy$		
	GCF = 5x		
	$5x(3x^2 - x + 6y)$		
	Example 7: Factor		
	Example 7: Factor $21x^2y + 35xy^2 - 7xy$		
	GCF = 7xy		
	7xy(3x+5y-1)		
[			

Method 1 – Greatest Common Factor

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# Method 2 – Grouping – 4 terms

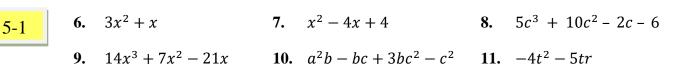
Main Topics	Examples
	Example 7: Factor
	$x^3 + 4x^2 + 3x + 12$
Steps	
1. Chop the 4 terms in half	$\underbrace{x^3 + 4x^2}_{+3x + 12}$
Separate into two binomials.	
	$x^2(x+4) + 3(x+4)$
2. Pull GCF out of each half.	
	$(x+4)(x^2+3)$
3. Pull out identical pieces	
from both halves.	Example 8: Factor
	$2x^3 + 10x^2 - 3x - 15$
	$23 + 10^2$ $2 15$
	$2x^3 + 10x^2$ $-3x - 15$
	$2x^2(x+5) - 3(x+5)$
	22 (2 + 3) 3(2 + 3)
	$(x+5)(2x^2-3)$
	Example 9: Factor
	7xy + 28x + y + 4
	$\underbrace{7xy+28x}_{+y+4}$
	7x(y+4) + (y+4)
	7x(y+4) + (y+4)
	(y+4)(7x+1)
	Example 10: Factor
	$2x^3y + 16x^2y + 6xy + 48y$
Use Method 1 first if possible.	
Ose Method I first if possible.	GCF = 2y
	$2y(x^3 + 8x^2 + 3x + 24)$
Then use Grouping on	$\frac{x^{3} + 8x^{2} + 3x + 24}{x^{2}(x + 8) + 3(x + 8)}$ $\frac{x^{2}(x + 8) + 3(x + 8)}{(x + 8)(x^{2} + 3)}$
remaining 4 terms.	$x^3 + 8x^2$ $3x + 24$
	$x^{2}(x \pm 9) \pm 2(x \pm 9)$
	x (x + 0) + 3(x + 0)
	$(x+8)(x^2+3)$
	Answer: $2y(x+8)(x^2+3)$

## 176 Section 5-1 Exercises

Perform the indicated operations.

4-3  
1. 
$$3a(4b^2 - a)$$
  
3.  $(x + 1)(x^2 - 3x - 4)$   
4.  $(-x + 1)(3x - 7)$   
5.  $(-4m^3 - 16m^2 + 6m) \div (-2m)$   
Identify which method(s) you should try in factoring the following polynomials (refer back to the

Identify which method(s) you should try in factoring the following polynomials (refer back to the beginning of section 5-1).



Identify the greatest common factor between the terms.

12.	18, 24, 48	13.	$3x, 9x^2, 6$	14.	$-14s^3, -7s$
15.	$a^2b$ , $-bc$ , $3bc^2$	16.	$125x^3$ , $50x^2$ , $10x$	17.	y <sup>4</sup> , 4y <sup>3</sup> , 2y <sup>2</sup> , 8y

Factor the following by pulling out the greatest common factor if there is one. If not, the expression is prime.

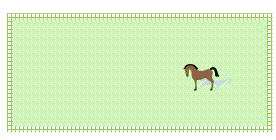
18.	9k + 3	19.	$-18y^5 - 6y$
20.	$2x^4 - 3y^2 + 7y$	21.	$-z^2 - 7a - 2$
22.	$-12a^3b + 8a^2b^2 - 16ab^2$	23.	$19xy^2 - 38xy + 57y$
24.	$2a^2x^4 + 6a^2x^3 - 10ax^3$	25.	$-39s^5 - 18s^3 - 81s$

#### Factor the following by grouping if possible. $26 - 3x^3 - 9x^2 + 4x - 12$

26. 
$$3x^3 - 9x^2 + 4x - 12$$
27.  $-2x^3 - 2x^2 - 3x - 3$ 28.  $4x^3 - 20x^2 - 6x + 10$ 29.  $x^3 + 5x^2 - 2x - 10$ 30.  $a^2x + 5a^2 + bx + 5b$ 31.  $8x^3 + 18x^2 - 20xy - 45y$ 32.  $x^3 + 3x^2 - 12x - 36$ 33.  $-4d^3 + 2d^2y - 6dy + 3y^2$ 34.  $x^3 + x^2 - x - 1$ 

#### Story Problem.

**35.** This pasture has an area described by the polynomial,  $10x^3 + 4x^2 - 15x - 6$ . Its length and width are described by binomials. Find a pair of binomials that will give the given area.



#### Preparation.

**36.** Multiply the following.a. (x + 7)(x + 5)b. (x + 2)(x + 8)c. (x + 9)(x + 3)d. (x + 5)(x + 4)

**37.** Given binomials like those in #36, notice that all the answers simplified to trinomials. Describe how to obtain the middle term of those trinomials.

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Section 5-1 Answe
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Section 5-1 Answers			
1.	$12ab^2 - 3a^2$		
2.	$x^2 + 8x + 16$		
3.	$x^3 - 2x^2 - 7x - 4$		
4.	$-3x^2 + 10x - 7$		
5.	$2m^2 + 8m - 3$		
6.	Method 1: Greatest Common Factors		
	Method 5: Special Cases		
7.	Method 1: Greatest Common Factors		
	Method 3: $ax^2 + bx + c$ , where $a = 1$		
8.	Method 1: Greatest Common Factors		
	Method 2: Grouping		
9.	Method 1: Greatest Common Factors		
	Method 4: $ax^2 + bx + c$ , where $a \neq 1$		
10.	Method 1: Greatest Common Factors		
	Method 2: Grouping		
11.	Method 1: Greatest Common Factors		
	Method 5: Special Cases		
12.	6		
13.	3		
14.	-7s		
15.	b		
16.	5 <i>x</i>		
17.	у		
18.	3(3k + 1)		
19.	$-6y(3y^4+1)$ or $6y(-3y^4-1)$		
20.	prime		
21.	$-1(z^2 + 7a + 2)$		

**22.**  $-4ab(3a^2 - 2ab + 4b)$  or  $4ab(-3a^2 + 2ab - 4b)$ 

23. 19y(xy - 2x + 3)**24.**  $2ax^{3}(ax + 3a - 5)$ **25.**  $-3s(13s^4 + 6s^2 + 27)$ **26.**  $(x-3)(3x^2+4)$ 27.  $(x+1)(-2x^2-3)$ **28.**  $2(2x^3 - 10x^2 - 3x + 5)$ Not factorable by grouping **29.**  $(x^2 - 2)(x + 5)$ **30.**  $(a^2 + b)(x + 5)$ **31.**  $(2x^2 - 5y)(4x + 9)$ 32.  $(x^2 - 12)(x + 3)$ **33.**  $(-2d + y)(2d^2 + 3y)$ 34.  $(x+1)(x^2-1)$ **35.** side 1:  $(2x^2 - 3)$ *side* 2:(5x + 2)**36.** In class. 37. In class.

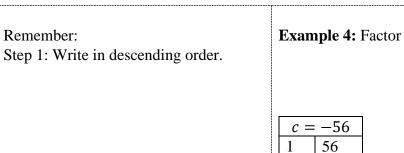
# Section 5-2 Factoring: Trinomial Fast

THE 5 METHODS of FACTORING			
Method	<b>Type of Polynomial used on:</b>		
1: Pull out the Greatest Common Factor (GCF)	All		
2: Grouping	4 Terms		
3: $ax^2 + bx + c$ , where $a = 1$	Trinomials, where $a = 1$		
4: $ax^2 + bx + c$ , where $a \neq 1$ $ac - method$	Trinomials, where $a \neq 1$		
5: Special Cases	Binomials & Perfect Squares		

## CHAPTER OVERVIEW (Video Instruction and Solutions Link)

# Method 3 - $x^2 + bx + c$ – Trinomial Fast

Main Topics	Examples	
Steps1. Write in descending order.2. Find factors of c,3. That add to b.4. $(x )(x )$ .	<b>Example 1:</b> Factor	$x^2 + 12x + 35$
	<b>Example 2:</b> Factor	(x+5)(x+7)
Note that negatives can work.		$x^2 - 12x + 35$
	Example 3: Factor	(x-5)(x-7)
	$     \boxed{\begin{array}{c} c = 56 \\ 1 \\ 2 \\ 2 \\ 38 \\ \end{array}} $	$x^2 - 18x + 56$
	-4 -14 7 8	(x-4)(x-14)



In Ex 5 and Ex 6, we see that the

(including the sign.

numbers must multiply to *c* exactly

(including the sign) and add to *b* exactly

2

1

-2

3 5

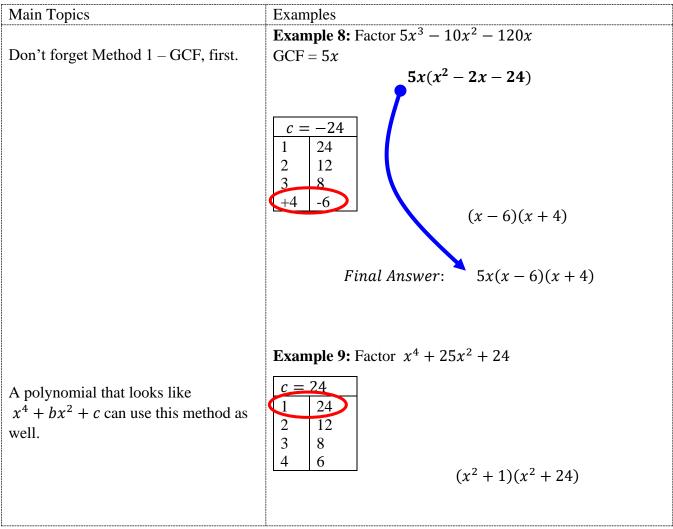
1

5

 $x - 56 + x^2$  $x^2 + x - 56$ 56 28 14 +8(x - 7)(x + 8)Example 5: Factor  $x^2 + 13x - 30$ c = -3030 +1510 6 (x-2)(x+15)Example 6: Factor  $x^2 - 13x + 30$ *c* = 30 30 15 -10 6 (x-3)(x-10)

Example 7: Factor  $x^2 - 10x - 24$ c = -2424 -12 +23 8 6 4 (x+2)(x-12)

#### Watch Out



## Section 5-2 Exercises

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Identify the greatest common factor between the terms.

**1.** 24, 96, 336**2.** 120, 480, 960**3.** 77, 154, 968**4.** 
$$-13b^2$$
,  $-12ab$ ,  $-25b^2$ **5.**  $12a^2$ ,  $16a^2$ ,  $96a^2$ **6.**  $14m^2n$ ,  $28mn^2$ ,  $77m^2$ 

Factor the following by pulling out the greatest common factor if possible.

7. 
$$-3x^2 + 6x^2y - 27x^3$$
8.  $7xy^2 - 2xy + 4x^2y + 2x^2y^2$ 9.  $12p^{24} + 56p^2 - 48s$ 10.  $3r^2 + 27r^3 - 33r^4$ 

Factor the following by grouping if possible.

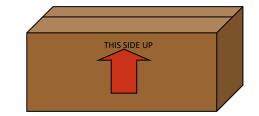
11. 
$$28x^3 - 12x^2 + 7x - 3$$
12.  $6x^3 + 3x^2 + 2x + 1$ 13.  $x^3 - 3x^2 + x - 3$ 14.  $16x^3 + 52x^2 - 52x - 169$ 15.  $2a^2x - 2a^2y + 3bx - 3by$ 16.  $2x^3 + 2x^2y - 3x - 3y$ 17.  $x^3 - 3x^2 - 9x + 27$ 18.  $x^4 + 4x^3 + 2x + 8$ 

Factor the following using the  $ax^2 + bx + c$ , where a = 1 method.

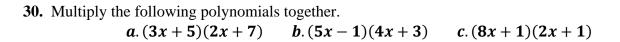
5-2	19.	$x^2 + 2x - 24$	20.	$x^2 + 11x + 18$
	21.	$x^2 - 8x + 15$	22.	$x^2 - x - 20$
	23.	$x^2 + 16x + 63$	24.	$x^2 - 4x - 60$
	25.	$3x^2 + 27x + 24$	26.	$x^2 - 7x - 60$
	27.	$x^2 + 6x - 27$	28.	$7x^2 - 7x - 14$

#### Story problem.

**29.** This box's volume is described by the polynomial  $4x^3 - 12x^2 - 72x$ . Its height is described by a monomial and its length and width are described by binomials. Find a solution set using prime factors.



**Preparation:** The following are trinomials in the form  $ax^2 + bx + c$  where  $a \neq 1$ .

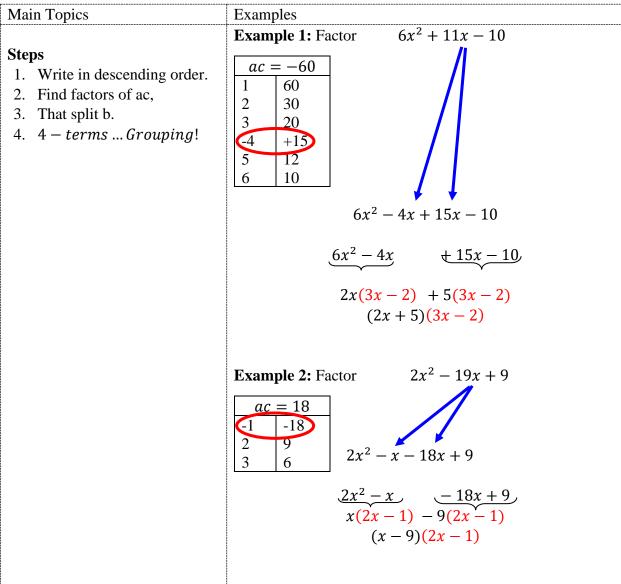


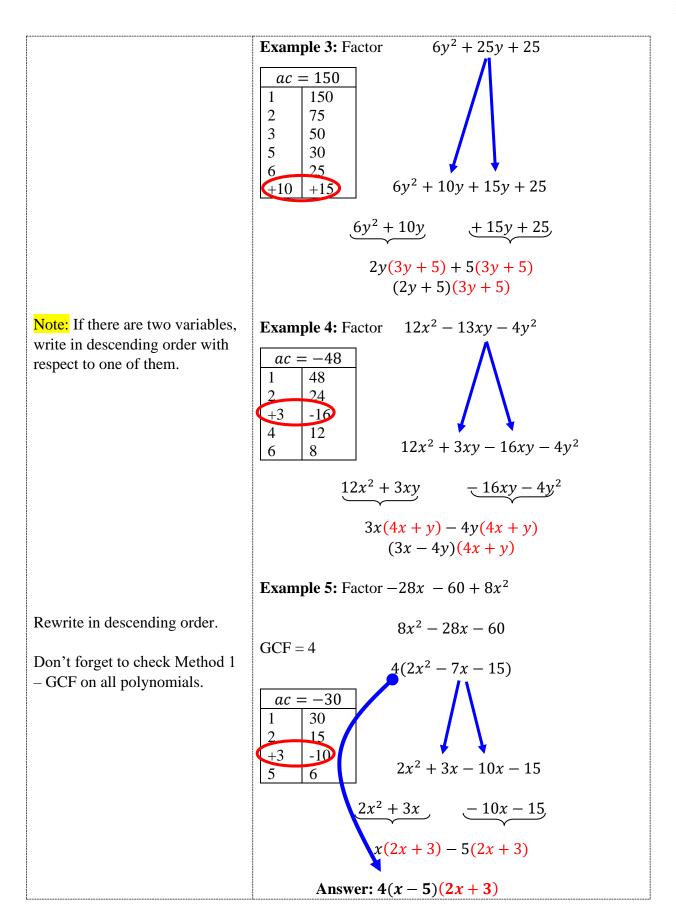
Section	on 5-2 Answers
1.	24
2.	120
3.	11
4.	-b or $b$
5.	$4a^2$
6.	7 <i>m</i>
7.	$-3x^2(1-2y+9x)$ or $3x^2(-1+2y-9x)$
8.	xy(7y-2+4x+2xy)
9.	$4(3p^{24} + 14p^2 - 12s)$
10.	$3r^2(1+9r-11r^2)$
11.	$(7x-3)(4x^2+1)$
12.	$(3x^2 + 1)(2x + 1)$
13.	$(x^2 + 1)(x - 3)$
14.	$(4x^2 - 13)(4x + 13)$
15.	$(2a^2+3b)(x-y)$
16.	$(2x^2-3)(x+y)$
17.	$(x^2 - 9)(x - 3)$
18.	$(x^3 + 2)(x + 4)$
19.	(x+6)(x-4)
20.	(x+9)(x+2)
21.	(x-3)(x-5)
22.	(x-5)(x+4)
23.	(x+9)(x+7)
24.	(x-10)(x+6)
25.	3(x+8)(x+1)
26.	(x-12)(x+5)
	(x+9)(x-3)
28.	7(x-2)(x+1)
29.	height: 4x
	length and width: $(x + 3)$ and $(x - 6)$
30.	In class

### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

THE 5 METHODS of FACTORING					
Method	<b>Type of Polynomial used on:</b>				
1: Pull Out the Greatest Common Factor (GCF)	All				
2: Grouping	4 Terms				
3: $ax^2 + bx + c$ , where $a = 1$	Trinomials, where $a = 1$				
4: $ax^2 + bx + c$ , where $a \neq 1$ ac – method	Trinomials, where $a \neq 1$				
5: Special Cases	Binomials & Perfect Squares				

## Method 4 - $ax^2 + bx + c$ - ac method





#### **Section 5-3 Exercises**

Identify the greatest common factor between the terms.

**5-1 1.** 14, 49, 112 **2.** 
$$15x$$
,  $39xy$ ,  $52x$  **3.**  $45j^2k$ ,  $-80j^2k^3$ ,  $105k^2$ 

Factor the following by pulling out the greatest common factor.

4.  $49x^5 + 21x^3 - 14x^2$ 5.  $24x^3y^3 + 96x^2y^3 - 72x^3y^2$ 6.  $15x^2y^3z^2 - 12x^2y^3z + 9x^2y^3$ 7.  $18p^3 - 6p^2 + 14p^4 + 2rs$ 

Factor the following by grouping if possible.

8. 
$$8x^3 + 2x^2 - 12x - 15$$
9.  $3x^3 - 15x^2 + 5x - 25$ 10.  $2x^3 + 3x^2 + 2x + 3$ 11.  $x^3 + x^2 - x - 1$ 

Factor the following using the  $ax^2 + bx + c$ , where a = 1 method.

5	-2
_	

12. $x^2 - 5x - 84$	<b>13.</b> $x^2 - x - 6$
14. $x^2 - 2x - 35$	<b>15.</b> $x^2 - 15x + 54$
<b>16.</b> $x^2 - 18x + 81$	<b>17.</b> $x^2 - 8x - 33$

Factor the following using the  $ax^2 + bx + c$ , where  $a \neq 1$  method.

5-3		$10x^2 - 7x - 6$		$8x^2 + 2x - 3$
	20.	$3 + 16x + 5x^2$	21.	$2m^2 + 11m + 12$
	22.	$2x^2 - 5x - 25$	23.	$6x^2 + 25xy + 14y^2$
	24.	$2s^2 - 21s + 40$	25.	$-6 + 16x^2 + 20x$
	26.	$5x^2 - 14xy - 3y^2$	27.	$7y^2 - 30y + 8$

#### **Preparation: Multiply.**

4-3

28. (x-5)(x+5)

**29.** 
$$(a+b)^2$$

#### **Section 5-3 Answers**

- **1.** 7 **2.** *x* **3.** 5k 4.  $7x^2(7x^3 + 3x - 2)$ 5.  $24x^2y^2(xy+4y-3x)$ 6.  $3x^2y^3(5z^2-4z+3)$ 7.  $2(9p^3 - 3p^2 + 7p^4 + rs)$ 8. Not factorable by Grouping 9.  $(3x^2 + 5)(x - 5)$ 10.  $(x^2 + 1)(2x + 3)$ 11.  $(x^2 - 1)(x + 1)$ 12. (x-12)(x+7)13. (x-3)(x+2)14. (x-7)(x+5)15. (x-9)(x-6)16. (x-9)(x-9) or  $(x-9)^2$ 17. (x - 11)(x + 3)18. (5x-6)(2x+1)**19.** (2x-1)(4x+3)**20.** (5x+1)(x+3)**21.** (2m+3)(m+4)22. (2x+5)(x-5)23. (3x+2y)(2x+7y)24. (2s-5)(s-8)**25.** 2(4x-1)(2x+3)26. (5x + y)(x - 3y)27. (y-4)(7y-2)28. In class.
- **29.** In class.

# 188Section 5-4 Factoring: Special Cases

THE 5 METHODS of FACTORING					
Method	<b>Type of Polynomial used on:</b>				
1: Pull Out the Greatest Common Factor (C.F.)	All				
2: Grouping	4 Terms				
3: $ax^2 + bx + c$ , where $a = 1$	Trinomials, where $a = 1$				
4: $ax^2 + bx + c$ , where $a \neq 1$ $ac - method$	Trinomials, where $a \neq 1$				
5: Special Cases	Binomials & Perfect Squares				

## CHAPTER OVERVIEW (Video Instruction and Solutions Link)

# 2-Terms, Difference of Squares

2- I CI IIIS, DITICI CIICC OI Squa	
Squares	Squares of numbers to recognize:
	$1^2 = 1$ $8^2 = 64$
	$2^2 = 4$ $9^2 = 81$
	$3^2 = 9$ $10^2 = 100$
	$4^2 = 16$ $11^2 = 121$
	$5^2 = 25$ $12^2 = 144$
	$6^2 = 36$ $13^2 = 169$
	$7^2 = 49$ $14^2 = 196$
Difference means subtraction.	Example 1: Factor
Difference means subtraction.	$25x^2 - 16$
	237 10
	square difference square
$A^2 - B^2 =$	
(A+B)(A-B)	$25x^2 = (5x)^2 \qquad 16 = 4^2$
	(5x+4)(5x-4)
	Example 2: Factor
	$49x^2 - 9$
	$49x^2 = (7x)^2 \qquad 9 = 3^2$
	(7x+3)(7x-3)
1	

	<b>Example 3:</b> Factor $121x^2 - 36y^2$
	$121x^2 = (11x)^2 \qquad 36y^2 = (6y)^2$
	(11x + 6y)(11x - 6y)
	<b>Example 4:</b> Factor $4x^2 - 81y^2$
Difference of squares: $A^2 - B^2 =$	$4x^2 = (2x)^2 \qquad 81y^2 = (9y)^2$
$A^2 - B^2 = (A+B)(A-B)$	(2x+9y)(2x-9y)
	<b>Example 5:</b> Factor $100t^2 - 1$
	$100t^2 = (10t)^2$ $1 = (1)^2$
	(10t + 1)(10t - 1)
	<b>Example 6:</b> Factor $y^4 - 1$
	$y^4 = (y^2)^2$ $1 = (1)^2$
	$(y^2 + 1)(y^2 - 1)$
	another difference of squares
	Answer: $(y^2 + 1)(y + 1)(y - 1)$

# Sum of Squares is Prime

Sum means addition.	Example 7: Factor
	$x^2 + 9$
$A^2 + B^2$ is prime.	Prime.
(cannot be factored)	
	Example 8: Factor
Why? Look at the possibilities.	$25x^2 + 64$
• $(A+B)(A-B) = A^2 - B^2$	Prime.
• $(A+B)(A+B) = A^2 + 2AB + B^2$	
• $(A - B)(A - B) = A^2 - 2AB + B^2$	Example 9: Factor
None work.	$36x^2 + 49$
	Prime.

# Perfect square trinomial

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Checklist to recognize a Perfect Square Trinomial. Tri- nomialPerfect SquaresMiddle term = 2ABLast term is positivePerfect Square Trinomia $16y^2 + 24y + 9$ Image: Colspan="3">NoImage: Colspan="3">No $16y^2 + 24y + 9$ Image: Colspan="3">NoYES $16y^2 + 25y + 9$ Image: Colspan="3">NoNO $4x^2 + 12x + 9$ Image: Colspan="3">NoNO $4x^2 + 12x - 9$ Image: Colspan="3">NoNO $4x^2 + 12x - 9$ Image: Colspan="3">NONO $x^2 - 20x + 100$ Image: Colspan="3">NONO $x^2 + 20x - 100$ Image: Colspan="3">NONO $x^2 + 20x + 96$ Image: Colspan="3">NONO $x^2 + 20x + 96$ Image: Colspan="3">NONO $x^2 + 20x + 96$ Image: Colspan="3">NOFactor a perfect square $A^2 + 2AB + B^2 =$ Image: Colspan="3">Example 10: Factor	Identify	a perfect square					
POLYNOMIALIni- nomialEnds = Perfect SquaresMiddle term = 2ABLast term is positiveSquare Trinomia $16y^2 + 24y + 9$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $16y^2 + 25y + 9$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $16y^2 + 25y + 9$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $16y^2 + 25y + 9$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $4x^2 + 12x + 9$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $4x^2 + 12x - 9$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $4x^2 + 12x - 9$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $4x^2 + 12x - 9$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $x^2 - 20x + 100$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $x^2 + 20x - 100$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $x^2 + 20x + 96$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $x^2 + 20x + 96$ Image: SquaresImage: SquaresImage: SquaresImage: SquaresImage: Squares $x^2 + 20x + 96$ Image: SquaresImag			Checklist	to recognize a			
$16y^2 + 24y + 9$ YES $16y^2 + 25y + 9$ NO $4x^2 + 12x + 9$ NO $4x^2 + 12x - 9$ NO $4x^2 + 12x - 9$ NO $4x^2 + 12x - 9$ NO $x^2 - 20x + 100$ NO $x^2 + 20x - 100$ NO $x^2 + 25x + 100$ NO $x^2 + 20x + 96$ NO         NO       NO $x^2 + 20x + 96$ NO         NO       NO         NO       NO $x^2 + 20x + 96$ NO         NO       NO         NO       NO         NO       NO $x^2 + 20x + 96$ NO         NO       NO         NO       NO $x^2 + 20x + 96$ NO         NO       NO         NO       NO         NO       NO $x^2 + 20x + 96$ NO         NO       NO $x^2 + 88x + 121$	POLYNOMIAL			Perfect			
$10y + 25y + y$ $10$ $10$ $10$ $10$ $10$ $4x^2 + 12x - 9$ $10$ $10$ $10$ $10$ $10$ $10$ $4x^2 + 12x - 9$ $100$ $10$ $100$ $100$ $100$ $100$ $x^2 - 20x + 100$ $100$ $100$ $100$ $100$ $100$ $100$ $x^2 + 20x - 100$ $100$ $100$ $100$ $100$ $100$ $100$ $x^2 + 25x + 100$ $100$ $100$ $100$ $100$ $100$ $100$ $x^2 + 20x + 96$ $100$ $100$ $100$ $100$ $100$ $100$ Example 10: Factor         Tector $16x^2 + 88x + 121$	-	$16y^2 + 24y + 9$	1	1	1	1	YES
$4x^2 + 12x - 9$ $\checkmark$ $\checkmark$ NO       NO $4x^2 + 12x - 9$ $\checkmark$ $\checkmark$ $\checkmark$ NO       NO $x^2 - 20x + 100$ $\checkmark$ $\checkmark$ $\checkmark$ $\checkmark$ YES $x^2 + 20x - 100$ $\checkmark$ $\checkmark$ $\checkmark$ NO       NO $x^2 + 25x + 100$ $\checkmark$ $\checkmark$ NO       NO       NO $x^2 + 20x + 96$ $\checkmark$ NO       NO       NO       NO         Factor a perfect square       Example 10: Factor $16x^2 + 88x + 121$ $16x^2 + 88x + 121$		$16y^2 + 25y + 9$	1	1	NO	1	NO
4x + 12x - 9       Image: Constraint of the second		$4x^2 + 12x + 9$	-	1		1	YES
$x^2 + 20x - 100$ $\checkmark$ $\checkmark$ NO       NO $x^2 + 25x + 100$ $\checkmark$ $\checkmark$ NO $\checkmark$ NO $x^2 + 25x + 100$ $\checkmark$ $\checkmark$ NO $\checkmark$ NO $x^2 + 20x + 96$ $\checkmark$ NO       NO $\checkmark$ NO         Factor a perfect square		$4x^2 + 12x - 9$	1	1	1	NO	NO
x + 20x - 100 $x = 100$ $x = 1000$ <th< td=""><td></td><td><math>x^2 - 20x + 100</math></td><td>1</td><td>1</td><td>✓</td><td>1</td><td>YES</td></th<>		$x^2 - 20x + 100$	1	1	✓	1	YES
$x + 23x + 100$ $\checkmark$ $\land$		$x^2 + 20x - 100$	1	1	✓	NO	NO
$x + 20x + 90$ $\blacksquare$ Example 10: FactorExample 10: FactorFactor a perfect square $16x^2 + 88x + 121$	5	$x^2 + 25x + 100$	1	1	NO	1	NO
<b>Factor a perfect square</b> $16x^2 + 88x + 121$		$x^2 + 20x + 96$	1	NO	NO	-	NO
$(A+B)(A+B) = 16x^2 = (4x)^2   121 = (11)^2   88 = 2(4)(11) (4x+11)^2$	A2 + 2AB + B2 = (A + B)(A + B) =			$16x^2 = (4$	$(x)^2$ 121 =	= (11) <sup>2</sup> 88 =	2(4)(11)
<b>Example 11:</b> Factor $25x^2 - 90x + 81$ <b>Note:</b> If you find a trinomial	Note: If :	you find a trinomia		mple 11: Facto		90x + 81	
isn't a perfect square, try Method 3 or 4 to see if it will $25x^2 = (5x)^2$ $81 = (-9)^2 - 90 = 2(5)(-9)$	-	1	:11	$25x^2 = (5x)^2 \qquad 81 = (-9)^2 \qquad -90 = 2(5)(-9)$			
factor another way. $(5x - 9)^2$				$(5x - 9)^2$			
<b>Example 12:</b> Factor $9x^2 - 42x + 49$			Exa	mple 12: Facto		2 <i>x</i> + 49	
$9x^2 = (3x)^2$ $49 = (-7)^2 - 42 = 2(3)(-7)$				$9x^2 = (3x)$	49 = (-	$(-7)^2 - 42 =$	2(3)(-7)
$(3x-7)^2$					(3 <i>x</i> -	- 7) <sup>2</sup>	

#### **Section 5-4 Exercises**

Factor the following by pulling out the greatest common factor if possible.

**5-1 1.** 
$$8x^6 - 48x^3 + 64x^4$$
 **2.**  $3j^2kb^3 - 2j^3k^5b^2 + 5j^3k^2b - 7j^3k^3b^3$ 

Factor the following by grouping if possible.

**5-1 3.** 
$$12k^{3}b + 15kb + 8k^{2} + 10$$
 **4.**  $84m^{3}n^{2} + 35m^{2}n^{2} - 12m - 5$ 

Factor the following using the  $ax^2 + bx + c$ , where a = 1 method.

**5-2 5.** 
$$x^2 - 2x - 63$$
 **6.**  $x^2 + 20x + 75$ 

Factor the following using the  $ax^2 + bx + c$ , where  $a \neq 1$  method.

**5-3 7.** 
$$12x^2 + 7x - 10$$
 **8.**  $-14x^2 + 17x + 6$ 

#### Story problem.

9. An alien spaceship has traveled  $10x^2 + 19x - 15$  miles from their home planet. Their speed and time can both be represented by binomials. Find two suitable binomials that will represent them. (Recall that d = rt, and you have been given distance.)



Determine if the following are differences of squares, then factor. If unfactorable, explain why.



**10.** 
$$x^2 - 36$$
  
**12.**  $4x^2 - 9$ 

14. 
$$-25 + 4y^2$$

**16.** 
$$27 - 3m^2$$

**18.** 
$$2x^2 - 1$$

11. $16y^4 + 9$ 13. $54x^2 - 24$ 15. $25g^8 - 81$ 17. $y^5 + 4y$ 19. $16x^2 - 49$ 

Determine if the following are perfect square trinomials. If they are, factor using method 5. If they are not or you are unsure, use method 3 or 4.

20.	$x^2 + 10x + 25$	21.	$4x^2 - 12x + 9$
22.	$3x^2 + 5x - 2$	23.	$6x^2 - 84x + 294$
24.	$9y^4 - 66y^2 + 121$	25.	$2m^2 + 16m + 32$
26.	$4x^2 - 16x + 16$	27.	$4x^2 + 30x - 100$

Preparation: The following polynomials have been factored already. Determine if they are completely factored. If not, finish factoring the polynomials.

28.	$4(x^2 - 6x + 9)$	29.	$(x^2 + 4)(x^2 - 4)$
30.	$3(m-8)^2$	31.	$7(100y^4 - 16)$

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#### **Section 5-4 Answers**

- $8x^3(x^3 + 8x 6)$ 1.  $j^{2}kb(3b^{2}-2jk^{4}b+5jk-7jk^{2}b^{2})$ 2.  $(3kb + 2)(4k^2 + 5)$ 3. 4.  $(7m^2n^2-1)(12m+5)$ (x-9)(x+7)5. 6. (x+5)(x+15)7. (3x-2)(4x+5)8. (-2x+3)(7x+2) or (-7x-2)(2x-3) or -(2x-3)(7x+2)9. rate: (2x + 5) time: (5x - 3) or rate: (5x - 3) time: (2x + 5)10. (x+6)(x-6)**11.** Prime. (It is prime because a *sum* of squares is not factorable.) 12. (2x+3)(2x-3)13. 6(3x+2)(3x-2)14. (2y+5)(2y-5)15.  $(5g^4 + 9)(5g^4 - 9)$ 16. 3(3+m)(3-m)17.  $y(y^4 + 4)$ **18.** Prime. (It is prime because 2 is not a perfect square.) **19.** (4x+7)(4x-7)**20.**  $(x+5)^2$ 21.  $(2x-3)^2$ 22. (x+2)(3x-1)23.  $6(x-7)^2$ 24.  $(3y^2 - 11)^2$ 25.  $2(m+4)^2$ 26.  $4(x-2)^2$ 27. 2(2x-5)(x+10)28. In class. **29.** In class. 30. In class.
  - **31.** In class.

# <sup>194</sup> Section 5-5 Factoring (All together)

THE 5 METHODS of FACTORING			
Method	<b>Type of Polynomial used on:</b>		
1: Pull out the Greatest Common Factor (GCF)	All		
2: Grouping	4 Terms		
3: $ax^2 + bx + c$ , where $a = 1$	Trinomials, where $a = 1$		
4: $ax^2 + bx + c$ , where $a \neq 1$	Trinomials, where $a \neq 1$		
5: Special Cases	Binomials & Perfect Squares		

### CHAPTER OVERVIEW (Video Instruction and Solutions Link)

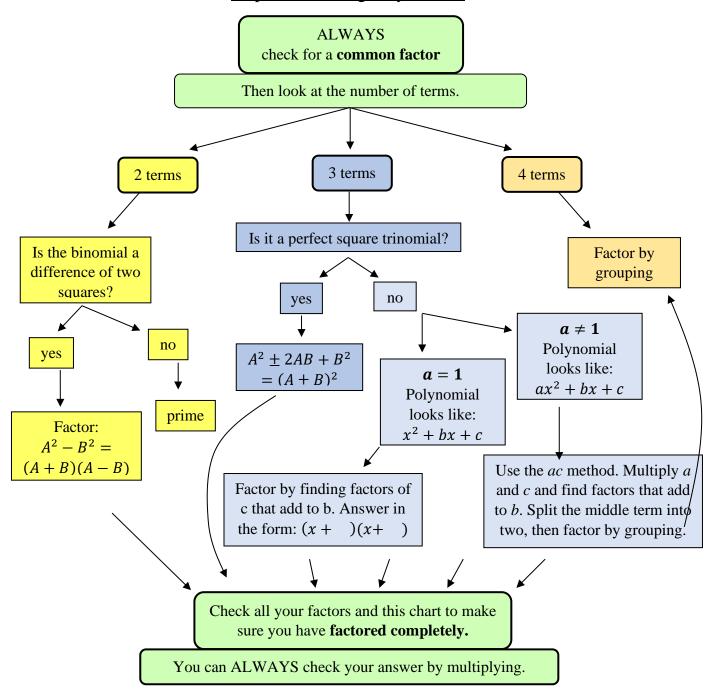
#### **REVIEW FROM SECTION 5-1: WHEN TO TRY EACH METHOD:**

Polynomial	Factoring Methods Possible			
$y^3 + 4y^2 + 2y + 8$	Method 1: Pull out Greatest Common Factor Method 2: Grouping			
$x^2 + 6x + 9$	Method 1: Pull out Greatest Common Factor Method 3: $ax^2 + bx + c$ , where $a = 1$			
$16x^2 - 16x + 4$	Method 1: Pull out Greatest Common Factor Method 4: $ax^2 + bx + c$ , where $a \neq 1$			
$54x^3 - 6x$	Method 1: Pull out Greatest Common Factor Method 5: Special Cases (because it's a binomial)			
$x^2 - 5x + 6$	Method 1: Pull out Greatest Common Factor Method 3: $ax^2 + bx + c$ , where $a = 1$			
$2c^3 + 8c^2 - 6c - 12$	Method 1: Pull out Greatest Common Factor Method 2: Grouping			
$36a^2 - 25$	Method 1: Pull out Greatest Common Factor Method 5: Special Cases (because it's a binomial)			
$35x^3 + 42x^2 - 14x - 77xy - 14y + 7$	Method 1: Pull out Greatest Common Factor (only method because it has 6 terms)			
$6y^2 + 25y + 25$	Method 1: Pull out Greatest Common Factor Method 4: $ax^2 + bx + c$ , where $a \neq 1$			

Notice that you may be using a couple of different methods on each problem.

We have learned several methods of factoring, and each method is used in different circumstances. If you are unsure what to do when factoring a polynomial, this chart will be helpful.

Steps to Factoring Polynomials



# 196 Factoring All Together

<b>Example 1:</b> Factor: $2x^2 + 36x + 154$	
Check for a common factor. How many terms? Is it a perfect square trinomial? What is the first coefficient? $(a = 1 \text{ or } a \neq 1)$ Factor – find factors of <i>c</i> that add to <i>b</i> . Check – can any of the factors be factored? Answer: $2(x + 1)$	<ul> <li>2(x<sup>2</sup> + 18x + 77)</li> <li>Three terms</li> <li>Not a perfect square trinomial</li> <li>a = 1, polynomial looks like x<sup>2</sup> + bx + c.</li> <li>c = 77 = 11 × 7; b = 18 = 11 + 7 Factored form: (x + 11)(x + 7)</li> <li>No, all factors are now prime.</li> <li>1)(x + 7)</li> </ul>
<b>Example 2:</b> Factor: $36y^2 - 36y + 9$	
Check for a common factor. How many terms? Is it a perfect square trinomial?	<ul> <li>9(4y<sup>2</sup> - 4y + 1)</li> <li>Three terms</li> <li>Yes, it follows the form A<sup>2</sup> + 2AB + B<sup>2</sup> where A = 2y and B = -1</li> </ul>
Factor knowing that $A^2 \pm 2AB + B^2 = (A + B)^2$ .	• $9(2y-1)^2$
Check – can any of the factors be factored? Answer: 9(2)	<ul> <li>The factors are 9 and (2y - 1).</li> <li>(2y - 1) is prime.</li> <li>y - 1)<sup>2</sup></li> </ul>
Example 3: Factor: $36x^3 + 72x^2 - x - 2$	
Check for a common factor. How many terms?	• Nope • Four terms – Grouping $36x^3 + 72x^2 - x - 2$ $36x^2(x+2) - 1(x+2)$
Look harder. Is there more that can be done? Yes. The first binomial is a difference of squares	$(36x^2 - 1)(x + 2)$ • $(36x^2 - 1)(x + 2)$
Factor knowing that $A^2 - B^2 = (A + B)(A - B)$ .	• $(36x^2 - 1)(x + 2)$ • $(6x + 1)(6x - 1)(x + 2)$
Check – can any of the factors be factored?	<ul> <li>(6x + 1)(6x - 1)(x + 2)</li> <li>Nope. We are now done</li> </ul>
Answer: $(6x + 1)(6x)$	(x-1)(x+2)

#### **Section 5-5 Exercises**

Factor the following. If non-factorable label as prime.

5-5	1.	$1 - y^2$	2.	$2x^2 - 8x + 8$
	3.	$13x + 2 + 18x^2$	4.	$81 + x^4$
	5.	$-2s^2 + 21s - 40$	6.	$6x^2 + 25xy + 14y^2$
	7.	$-5x + 2x^4 + 2x^2 - 5x^3$	8.	$x^2 - y^2$
	9.	$16b^2 - 9b$	10.	$4x^2 + 30x - 100$
	11.	$28x^2 + 65x + 28$	12.	$4a^5 + 16$
	13.	$x^3 + 3x^2 - 4x - 12$	14.	$r^3 + r^2 - 4r - 4$
	15.	$2x^3y + 4x^2y - 30xy$	16.	$16z^3 + 48z^2 + 36z + 108$
	17.	$4x^5 + 12x^4 - 4x^3 + 12x^2$	18.	$3x^2 + 5x - 17$
	19.	$x^8 - 81$	20.	$12x^3y - 27xy^3$
	21.	$x^2 - 3x - 18$	22.	$y^8 - k^{12}$
	23.	$16a^2 + 40a + 25$	24.	$z^4 + 8z^2 + 16$
	25.	$2\pi r^2 - 2\pi$	26.	$9x^2 + 3x$
	27.	$4b^2 + 256$	28.	$18x^3 + 54x^2 + 6x + 18$

#### **Story Problems.**

**29.** A billboard along the side of I-15 has an area represented by the polynomial  $9y^8 - 100$ . Find 2 binomials that represent the length and width of billboard. Recall that  $Area = (length) \times (width)$ .

**30.** A telephone booth with a square bottom has a volume of  $175x^3 + 140x^2 + 28x$ . Its height is represented by a monomial and its length and width by binomials. Find a monomial and two binomials that will represent these three dimensions.

#### **Preparation:**

**31.** Solve the following equations for the variable:

**a.** 
$$x^2 = 4$$
 **b.**  $25 - y^2 = 0$ 





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#### Section 5-5 Answers

```
1. (1+y)(1-y)
 2. 2(x-2)^2
 3. (2x+1)(9x+2)
 4. Prime
 5. (-2s+5)(s-8) or (2s-5)(-s+8)
 6. (3x + 2y)(2x + 7y)
 7. x(x^2+1)(2x-5)
 8. (x+y)(x-y)
 9. b(16b - 9)
10. 2(2x-5)(x+10)
11. (4x+7)(7x+4)
12. 4(a^5 + 4)
13. (x+2)(x-2)(x+3)
14. (r-2)(r+2)(r+1)
15. 2xy(x-3)(x+5)
16. 4(4z^2+9)(z+3)
17. 4x^2(x^3 + 3x^2 - x + 3)
18. Prime
19. (x^4 + 9)(x^2 + 3)(x^2 - 3)
20. 3xy(2x - 3y)(2x + 3y)
21. (x+3)(x-6)
22. (y^4 + k^6)(y^2 + k^3)(y^2 - k^3)
23. (4a + 5)^2
24. (z^2 + 4)^2
25. 2\pi(r+1)(r-1)
26. 3x(3x+1)
27. 4(b^2 + 64)
28. 6(3x^2 + 1)(x + 3)
29. side 1: 3y^4 + 10
    side 2: 3y^4 - 10
30. height: 7x
    base length: 5x + 2
    base width: 5x + 2
31. In class.
```

# Section 5-6 Solving Polynomial Equations

CHAPTER OVERVIEW (Video Instruction and THE 5 METHODS of FAC	ן		
Method	<b>Type of Polynomial used on:</b>		
1: Pull out the Greatest Common Factor (GCF)	All		C.I
2: Grouping	4 Terms		Solve Polynomial
3: $ax^2 + bx + c$ , where $a = 1$	Trinomials, where $a = 1$		Equations
4: $ax^2 + bx + c$ , where $a \neq 1$	Trinomials, where $a \neq 1$		
5: Special Cases	Binomials & Perfect Squares		

#### CUADTED OVEDVIEW (Video Inst ..... 10.1.4

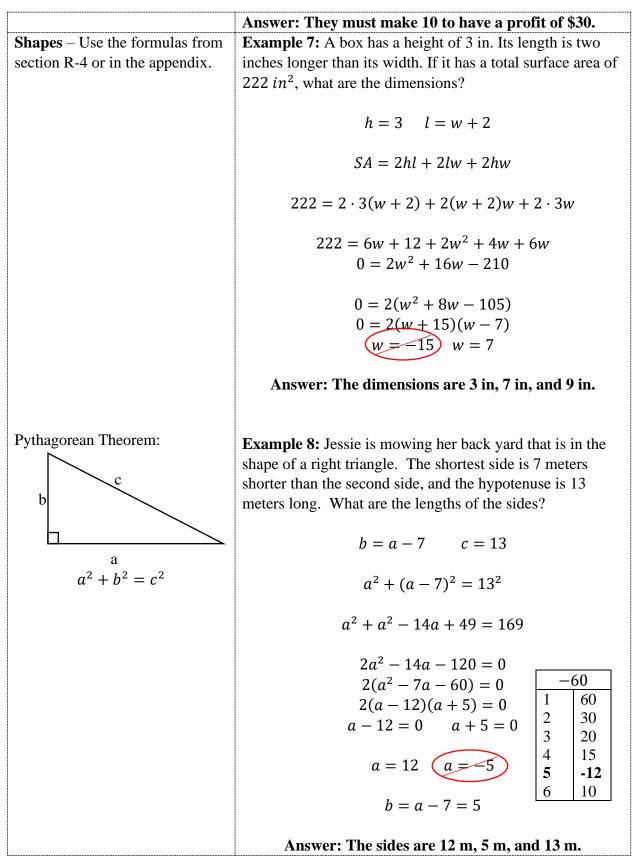
# **Polynomial Equations**

Main Topics	Examples				
Multiplication with 0	$5 \cdot 0 = 0$ $73 \cdot 0 = 0$ $0 \cdot (-371) = 0$ $0 \cdot x = 0$				
• Easiest multiplication					
ever	3x = 0 $57y = 0$ $97(m - 7) = 0$				
	x = 0 $y = 0$ $m - 7 = 0m = 7$				
• If the answer is 0, then one of the factors has to	(x-3)(2x+5)(x+7)(3x-11) = 0				
be 0.	x - 3 = 0 $2x + 5 = 0$ $x + 7 = 0$ $3x - 11 = 0$				
	$x = 3$ $x = -\frac{5}{2}$ $x = -7$ $x = \frac{11}{3}$				
Factor to Solve	Example 1:				
1. Get = $0$ .	$2x^2 - 10x = 0$				
2. Factor.	2x(x-5) = 0				
3. Set each factor $= 0$ .	2x = 0  x - 5 = 0				
	x = 0 $x = 5$				
	Example 2:				
	$x^2 - 7x = 18$				
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$				
	$\begin{array}{ c c c } \hline 3 & 6 \\ \hline & (x-9)(x+2) = 0 \\ \hline \end{array}$				

	x = 9, -2
Factor to Solve	Example 3:
1. Get = $0$ .	$6x^2 - 10 = -11x$
2. Factor.	
3. Set each factor $= 0$ .	$6x^2 + 11x - 10 = 0$
	ac = -60
	1 60
	2 30
	3 20
	-4 +15
	5 12
	$\begin{bmatrix} 6 & 10 \end{bmatrix}$
	$6x^2 - 4x + 15x - 10 = 0$
	2x(3x-2) + 5(3x-2) = 0
	(2x+5)(3x-2) = 0
	$x = -\frac{5}{2}, \frac{2}{3}$
	23
	Example 4:
	$49x^2 = 56x - 16$
	$49x^2 - 56x + 16 = 0$
	$(7x-4)^2 = 0$
	7 hannene turies a "deuble rest"
	$x = \frac{1}{4}$ happens twice, a "double root"
	Example 5:
	$25x^2 - 49 = 0$
	(5x - 7)(5x + 7) = 0
	(5x - 7)(5x + 7) = 0 $x = \frac{7}{5}, -\frac{7}{5} = \pm \frac{7}{5}$
[	<u> </u>

# **Word Problems**

Main Topics	Exam	Examples				
Formulas	Exam	<b>Example 6:</b> The profit of a small company when they				
Plug in the given data.	make	make x thingamabobs is $P = 2x^2 - 17x$ . How many will				
	they n	they need to make to get a profit of \$30?				
			$30 = 2x^2 - 17x$			
	ac =	= -60	$0 = 2x^2 - 17x - 30$			
1. Get = $0$ .	1	60	$0 = 2x^2 - 20x + 3x - 30$			
2. Factor.	2	30	0 = 2x(x - 10) + 3(x - 10)			
3. Set each factor $= 0$ .	3	-20	0 = (2x + 3)(x - 10)			
	4	15				
	5	5 12 3 10				
	6	10	$x = -\frac{1}{2}$ $x = 10$			
L						



#### 202 Section 5-6 Exercises

Factor the following.

5-6

5-51. 
$$4x^2 + 36x$$
2.  $r^2 - 64$ 3.  $x^2 + 4x + 4$ 4.  $5x^2 - 4x - 1$ 5.  $x^2 - 25$ 6.  $x^3 + 5x^2 - 9x - 45$ 7.  $-6 + 16a^2 + 20a$ 8.  $x^3 - 3x^2 + 2x$ 9.  $2x^3 + x^2 - 98x - 49$ 10.  $x^2 + 16x + 63$ 11.  $25x^2 - 100x + 100$ 12.  $x^2 + 8x - 48$ 

The following are identical to the previous twelve problems, except that they are now equations. Now that you have factored them, solve for the variable.

13.	$4x^2 + 36x = 0$	14.	$r^2 - 64 = 0$
15.	$x^2 + 4x + 4 = 0$	16.	$5x^2 - 4x - 1 = 0$
17.	$x^2 - 25 = 0$	18.	$x^3 + 5x^2 - 9x - 45 = 0$
19.	$-6 + 16x^2 + 20x = 0$	20.	$x^3 - 3x^2 + 2x = 0$
21.	$2x^3 + x^2 - 98x - 49 = 0$	22.	$x^2 + 16x + 63 = 0$
23.	$25x^2 - 100x + 100 = 0$	24.	$x^2 + 8x - 48 = 0$

Factor the following and solve for the variable.

$4x^2 + 16x + 16 = 0$	26.	$x^2 = 9$
$x^2 - 14x + 14 = -35$	28.	$y^2 + 16 = 0$
$3x^2 - 36 = 3x$	30.	$x^2 - 169 = 0$
$4x^2 + 36x - 15 = 25$	32.	$x^3 + 3x^2 - 4x - 12 = 0$
$100x^2 + 80x + 16 = 0$	34.	$x^2 - 4 = 0$
$6x^2 = -36x - 54$	36.	$x^2 - x - 20 = 0$
	$x^{2} - 14x + 14 = -35$ $3x^{2} - 36 = 3x$ $4x^{2} + 36x - 15 = 25$ $100x^{2} + 80x + 16 = 0$	$x^2 - 14x + 14 = -35$ 28. $3x^2 - 36 = 3x$ 30. $4x^2 + 36x - 15 = 25$ 32. $100x^2 + 80x + 16 = 0$ 34.

#### **Story Problems.**

**37.** The energy of an object is dependent on its mass and can be described by the following equation:  $E = 2m^2 - 12m$ , where *E* stands for energy and *m* stands for mass. If the energy of the object is 14 units, what is the mass of the object?

**38.** The area of a window is  $192 \text{ in}^2$ . The width of the window is four inches more than half the length of the window. What are the dimensions of the window?

**39.** A cone has a surface area of  $36\pi$  cm<sup>2</sup> and a slant height of 9 cm. What is the radius of the cone? (See section 2.2 for formulas)

**40.** Jefferson's back yard is in the shape of a right triangle. One leg of the triangle is seven feet longer than the other, with a hypotenuse of 17 feet. What are the lengths of the two legs?

**41.** Carl is building a right triangle hot tub that has a leg ten feet more than twice the other leg. The hypotenuse is 25 feet. What are the lengths of the two legs?

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#### Section 5-6 Answers

1.	4x(x+9)	28.	No solution
2.	(r+8)(r-8)	29.	x = -3, 4
3.	$(x+2)^2$	30.	x = -13, 13
4.	(5x+1)(x-1)	31.	x = -10, 1
5.	(x+5)(x-5)	32.	x = -3, -2, 2
6.	(x + 5)(x - 3)(x + 3)	33.	x = -2/5
7.	2(4a-1)(2a+3)	34.	x = -2, 2
8.	x(x-2)(x-1)	35.	x = -3
9.	(2x+1)(x-7)(x+7)	36.	<i>x</i> = −4, 5
10.	(x+9)(x+7)	37.	m = 7
11.	$25(x-2)^2$	38.	l = 16 in, $w = 12$ in
12.	(x + 12)(x - 4)	39.	r = 3  cm
13.	x = -9, 0	40.	8 feet, 15 feet
14.	<i>r</i> = −8,8	41.	7 feet, 24 feet
15.	x = -2		
16.	$x = -\frac{1}{5}, 1$		
18			
17.	x = -5, 5		

19.  $a = -\frac{3}{2}, \frac{1}{4}$ 

**20.** x = 0, 1, 2

21.  $x = -7, -\frac{1}{2}, 7$ 

22. x = -9, -7

**24.** x = -12, 4

**23.** *x* = 2

**25.** x = -2

**27.** x = 7

**26.** x = -3, 3

#### **Chapter 5 Review Exercises**

**1.** Create a visual chart of all of the methods, formulas, and examples from studying how to factor polynomials.

#### Identify the greatest common factor between the terms.

**5-1 2.** 112, 148, 246 **3.**  $3j^2$ ,  $5j^2aj^3$ ,  $4j^3y$  **4.**  $12m^4n^2p^4$ ,  $24m^3n^3p^4$ ,  $30m^3n^2p^5$ 

Factor the following by grouping.

5.  $6x^3 + 10x^2 + 3x + 5$ 6.  $21x^3 - 14x^2 - 12x + 8$ 7.  $5ax^3 + 20a^2x^2 + 3x + 12a$ 8.  $28x + 7x^3 + 4 + x^2$ 

#### Factor the following using method 3 or method 4.



#### Factor the following using method 5.

15. 
$$-x^2 + 64$$
16.  $x^2 + 2x + 1$ 17.  $49x^2 - 28x + 4$ 18.  $x^4y^2 - 9z^2$ 19.  $-16x^2 - 4$ 20.  $8y^2 + 72y + 162$ 

#### Factor the following.

5-4

5 - 5

**21.** 
$$18x^2 + 24x + 8$$
**22.**  $x^2 + 7x - 18$ **23.**  $-18x^3 + 15x^2 + 24x - 20$ **24.**  $-20x^2 - 19x - 3$ **25.**  $-3a^2xy + 3b^2xy$ **26.**  $x^2 - 15x + 56$ **27.**  $x^2 - 23x + 132$ **28.**  $x^2 - 4x - 45$ 

29.	$14x^3 + 16x^2 + 35x + 40$	30.	$-4x^2 + 52x - 168$
31.	$24m^3 - 6m^2n - 63mn^2$	32.	$49x^2 - 121$
33.	$35x^4y^2 + 42x^4y + 15x^3y^2 + 18x^3y$	34.	$4x^2 - 36xy + 81y^2$

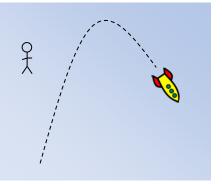
#### Solve for the variable by factoring.

		4

**35.** 
$$x^2 - 13x + 22 = -20$$
**36.**  $-6x^2 - 11x + 10 = 0$ **37.**  $-5x^3 - 10x^2 = 5x$ **38.**  $4x^3 + 16x^2 - x - 4 = 0$ **39.**  $100 - x^2 = -21$ **40.**  $4x^3 + 4x^2 - 25x = 25$ 

#### **Story Problems.**

**41.** Henry stands on a platform and shoots a rocket in his  $10^{\text{th}}$  grade science class. He found that the motion of the rocket can be described by the equation  $y = 60 + 28x - x^2$ , where y is the vertical distance and x is the horizontal distance traveled. If this trajectory equation were to be graphed, find **the x-intercepts** of the equation. (Fun fact: The positive x-intercept is how far away from the platform the rocket hits the ground!)



**42.** A triangle has an area of 14 square inches. The height of the triangle is three inches more than the base. What are the base and height of the triangle?

**43.** Jill has a small treasure box that is 6 inches long. It can hold a volume of 72 inches cubed, and the width of the box is 5 inches less than twice the height of the box. What are the dimensions of the box?

**44.** Jessie is mowing her back yard that is in the shape of a right triangle. The shortest side is 7 meters shorter than the second side, and the hypotenuse is 13 meters long. What are the lengths of the two sides?

#### **Chapter 5 Review Answers**

- **1.** This is your last one; make it good
- **2.** 2
- **3.** *j*<sup>2</sup>
- 4.  $6m^3n^2p^4$
- 5.  $(2x^2 + 1)(3x + 5)$
- 6.  $(7x^2 4)(3x 2)$
- 7.  $(5ax^2 + 3)(x + 4a)$
- 8.  $(x^2 + 4)(7x + 1)$
- 9. (x+1)(2x+1)
- **10.** 3(x-7)(x+3)
- 11. 2(x+4)(x+12)
- 12. (2x+5)(7x-3)
- **13.** -4(x-3)(x+9) or equivalent
- 14. 7(x-3)(x-2)
- 15. (8+x)(8-x)
- 16.  $(x+1)^2$
- 17.  $(7x-2)^2$
- **18.**  $(x^2y + 3z)(x^2y 3z)$
- **19.**  $-4(4x^2 + 1)$ , not a special case
- **20.**  $2(2y+9)^2$
- **21.**  $2(3x+2)^2$
- **22.** (x+9)(x-2)
- **23.**  $(-3x^2+4)(6x-5)$
- **24.** -1(5x+1)(4x+3) or equivalent
- 25. -3xy(a+b)(a-b) or equivalent
- **26.** (x-7)(x-8)
- **27.** (x 11)(x 12)

**28.** 
$$(x-9)(x+5)$$

- **29.**  $(2x^2 + 5)(7x + 8)$
- **30.** -4(x-7)(x-6)

- **31.** 3m(4m 7n)(2m + 3n)
- **32.** (7x 11)(7x + 11)
- **33.**  $x^3y(7x+3)(5y+6)$
- **34.**  $(2x 9y)^2$
- **35.** x = 6, 7

36. 
$$x = -\frac{3}{2}, \frac{2}{3}$$

- 37. x = -1,0
- **38.**  $x = -4, -\frac{1}{2}, \frac{1}{2}$
- **39.** x = -11, 11
- 40.  $x = -\frac{5}{2}, -1, \frac{5}{2}$
- **41.** (-2, 0), (30, 0)
- **42.** base = 4 inches, height = 7 inches
- **43.** height = 4 inches, width = 3 inches
- **44.** 5 meters, 12 meters

# <sup>208</sup> Beginning Algebra Final Review Exercises

Find the prime factorization for each number.

**1.** 27

Ch. R/1

**2.** 360

Find the lowest common multiple for each set of numbers.

Evaluate.

5. 
$$V = \frac{1}{3}\pi r^2 h$$
 when  $r = 4$  in.,  $h = 3$  in.  
6.  $3x^2 - 12x - 6$ , when  $x = -2$   
7.  $\left| -\frac{12}{4} \right|$   
8.  $-\frac{4}{18} - \left( -\frac{2}{9} \right)$ 

Simplify.

9. 
$$2[3(y+2)-2(4y-5)]-14$$
 10.  $\frac{20(8-3)-4|3-10|}{-10(-2)^2-2(5+2)}$ 

Solve.

Ch. 2

11.	2 - 5(x + 5) = 3(x - 2) - 1	12.	$\frac{5}{3} + \frac{2}{3}x = 6$
13.	-5x + 7 = 5x - 10(x + 1)	14.	$6x - 10 \le 7x + 5$
15.	2 is what percent of 40?	16.	Solve for $c$ in $x = \frac{a+b+c}{3}$

- **17.** Selene wants to buy a paddleboard for \$468. The tax will be 8%. How much will she pay total?
- **18.** The interior angles of a certain triangle have the following relationship: the second angle is three times the first angle and the third angle is 15° less than the first angle. Find the measure of all three angles.

#### Graph the following linear equations.

Ch. 3	<b>19.</b> $y = 2x - 4$	<b>20.</b> $6x - 2y = 18$
	<b>21.</b> $2x + 6 = 14$	<b>22.</b> <i>y</i> = -2.5

Write the equations of the lines with the following characteristics.

**23.** m = -1, goes through (-2,5) **24.** Goes through (2,1) and (4,0)

Write the following numbers in Scientific Notation.

Ch. 425. 678,100,00026. 0.000036Simplify.27. 
$$3^{-8} \cdot 3^7$$
28.  $\left(\frac{2a^2}{3b^4}\right)^{-2}$ 29.  $\left(\frac{4x^4y}{8x^{-3}yz^2}\right)^3$ 30.  $\frac{g^4m^3}{a^{-2}gm^7}$ Evaluate.31. Evaluate  $3x^3 - x^2 - x + 9$  when  $x = -2$ .

Multiply.

**32.** 
$$(6x - 2y)(5x^2 - 3y)$$
**33.**  $(5x^3 - 7x)^2$ **34.**  $(t+3)(t^2 - 3t - 4)$ **35.**  $(2h+3)(2h-3)$ 

Divide.

**36.** 
$$(18x^6 - 27x^5 - 3x^3) \div (9x^3)$$

Factor Completely.

Ch. 5	37.	$x^{6} - x^{5} - 30x^{4}$	38.	$m^2 + 5m + mt + 5t$
	39.	16x <sup>8</sup> - 81	40.	$12a^2 + 84ab + 147b^2$

Solve.

- **41.**  $3x^2 + 8x = 9 + 2x$
- **42.** The height of a sail on a sailboat is 3 feet greater than the length of its "foot" (the base of the sail). The hypotenuse of the triangle formed by the sail is 15 feet long. Find the height of the sail and the length of its foot.
- **43.** A rectangular picture is three times as long as it is wide. The area of the picture is 588 in.<sup>2</sup> Find the dimensions of the picture.
- **44.** The product of two consecutive integers is 55 more than their sum. Find the integers. (Hint: There will be two sets of integers in the answer negative integers and positive integers.)
- **45.** What are the x-intercepts of the graph of  $y = x^2 + x 12$ ?

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#### **Final Review Answers**

**1.**  $27=3^3$ **2.**  $360 = 2^3 \cdot 3^2 \cdot 5$ **3.** 144 **4.** 60 5. 50.27  $in^3$ . **6.** 30 **7.** 3 **8.** 0 **9.** -10y + 18 $-\frac{4}{3}$ 10. **11.** x = -2**12.**  $x = \frac{13}{2}$  or 6.5 **13.** No Solution **14.**  $x \ge -15$ **15.** 5% **16.** c = 3x - a - b**17.** \$505.44 **18.** 1*st*: 39, 2*nd*: 117, 3*rd*: 24 19. 20. 21.

22.	
	y = -x + 3
24.	$y = -\frac{1}{2}x + 2$
	$6.781 \times 10^{8}$ $3.6 \times 10^{-5}$
27.	$\frac{1}{3}$
28.	
29.	$\frac{x^{21}}{8z^6}$
30.	$\frac{g^3a^2}{m^4}$
31.	-17
32.	$30x^3 - 18xy - 10x^2y + 6y^2$
33.	$25x^6 - 70x^4 + 49x^2$
34.	$t^3 - 13t - 12$
35.	$4h^2 - 9$
36.	$2x^3 - 3x^2 - \frac{1}{3}$
	$\frac{3}{x^4(x-6)(x+5)}$
	(m+5)(m+t)
39.	$(2x^2 - 3)(2x^2 + 3)(4x^4 + 9)$
40.	$3(2a+7b)^2$
41.	x = -3, 1
42.	foot = 9 ft., height = $12$ ft.
43.	width = $14$ in., length = $42$ in.
44.	Negative integers: -7, -6
	Positive integers: 8, 9

**45.** (-4, 0) and (3, 0)

# Shape Formulas

	1	
	P = 2l + 2w	<b>P</b> is the Perimeter
		<i>l</i> is the length
W		<b>w</b> is the width
		A is the Area
Rectangle	A = lw	
b	P = 2a + 2b	<b>P</b> is the Perimeter
a	·	<b>a</b> is a side length
h	A = bh	<b>b</b> is the other side length
· · · · · · · · · · · · · · · · · · ·		A is the Area
Parallelogram		
		<b>P</b> is Perimeter
b		<b>b</b> is the little base
	$P = b + a + B + d$ $A = \frac{1}{2}h(B + b)$	<b>B</b> is the Big base
a h d	1	<b>a</b> is a leg
	$A = \frac{1}{2}h(B + b)$	<b>d</b> is a leg
В	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	A is the Area
Trapezoid		
	$P = s_1 + s_2 + s_3$	<b>P</b> is the Perimeter
h	1 = 51 + 52 + 53	
		St is the lateride ate
	1	$S_1$ is the 1st side, etc
b b	$A = \frac{1}{2}bh$	
Triangle	2 2 2 2	A is the Area
		<b>a</b> is one angle
b		
	a + b + c = 180	<b>b</b> is another angle
		C
		<b>c</b> is another angle
a		
Triangle		
	SA = 2lw + 2wh + 2lh	<i>l</i> is the length
	$\begin{bmatrix} 511 \\ -2tw \\ 1 \\ 2wit \\ 1 \\ 2tit $	<b>h</b> is the height
h		
		<b>w</b> is the width
w		
l	V = lwh	<b>SA</b> is the Surface Area
Rectangular Solid		V is Volume
L	1	

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	$C = 2\pi r$	<b>C</b> is the Circumference or Perimeter
r		$\pi$ is a number, about 3.14159 it has a button on your calculator
	$A = \pi r^2$	<b>r</b> is the radius of the circle
Circle		A is the area inside the circle
-r	$LSA = 2\pi rh$	<b>LSA</b> is Lateral Surface Area = Area just on the sides
h	$SA = 2\pi rh + 2\pi r^2$	<b>h</b> is the height
		SA is total Surface Area
	2.	$\pi$ is a number, about 3.14159 it has a button on your calculator
Cylinder	$V = \pi r^2 h$	<b>r</b> is the radius of the circle
		V is Volume
$\wedge$	$LSA = \pi rl$	<b>h</b> is the height
h		<b>r</b> is the radius of the circle
		<i>l</i> is the slant height
	$SA = \pi r^2 + \pi r l$	$\pi$ is a number, about 3.14159 it has a button on your calculator
Cone	$V = \frac{1}{3}\pi r^2 h$	SA is total Surface Area
		<b>LSA</b> is Lateral Surface Area = Area just on the sides
		<b>V</b> is the Volume
	$SA = 4\pi r^2$	<b>r</b> is the radius
r	$V = \frac{4}{3}\pi r^3$	<b>SA</b> is the Surface Area
	$V = 4 \pi m^3$	
	$v = \frac{1}{3}\pi r^{2}$	<b>V</b> is the Volume
Sphere		